

Basic Electrical Engineering

(2)

Current: It is defined as the rate of flow of electrical charge with respect to time which is given by

$$\Rightarrow \boxed{I = \frac{dQ}{dt}}$$

its unit is : Amperce (A)

Electric potential:

The virtue of work can possible done due to accumulation of electrical charges is called electric potential.

It is given by

$$\boxed{V = \frac{\text{Work}}{\text{Charge}} \text{ or } \frac{W}{Q}}$$

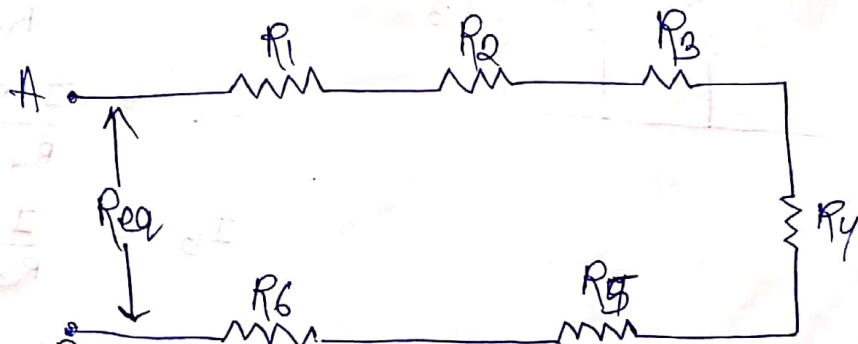
its unit is volt (V).

Resistance :-

It is a physical property of matter that opposes the flow of electric current through it this is called resistance.

It's unit is ohm (Ω).

Series Combination of Resistance:



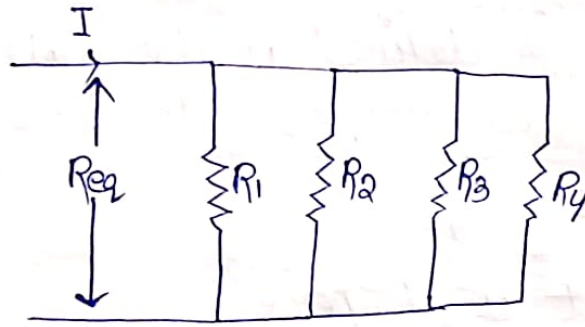
$$R_{eq} = R_1 + R_2 + R_3 + R_4 + R_5 + R_6$$

Parallel combination of Resistance:-

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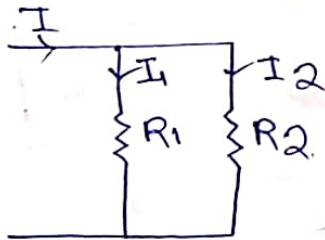
$$\frac{I}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}$$

$$R_{eq} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}}$$



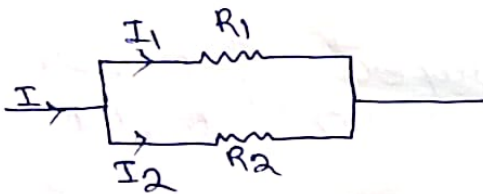
Current Division:

current division is only applicable in parallel combination.



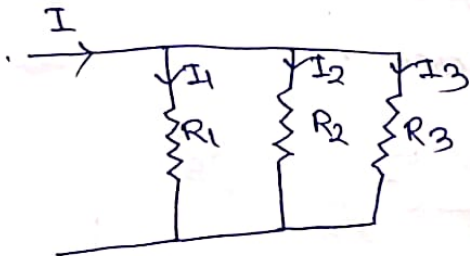
$$I_1 = \frac{I \times R_2}{R_1 + R_2}$$

$$I_2 = \frac{I \times R_1}{R_1 + R_2}$$



$$I_1 = \frac{I \times R_2}{R_1 + R_2}$$

$$I_2 = \frac{I \times R_1}{R_1 + R_2}$$



$$I_1 = \frac{I \times R_{eq}}{R_1 + R_{eq}}$$

$$I_2 = \frac{I \times R_{eq}}{R_2 + R_{eq}}$$

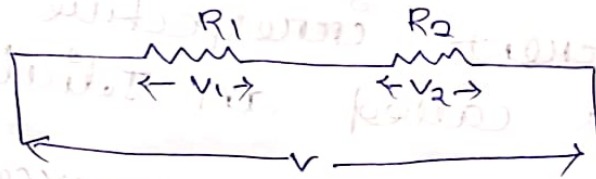
$$I_3 = \frac{I \times R_{eq}}{R_3 + R_{eq}}$$

Voltage Division:

Voltage division is only applicable in series combination (3)

$$V_1 = \frac{V \times R_1}{R_1 + R_2}$$

$$V_2 = \frac{V \times R_2}{R_1 + R_2}$$

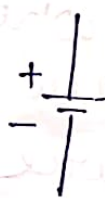


Ideal Voltage Source:

A voltage source that maintains constant terminal voltage irrespective of variation in the load current is called an ideal voltage source.

Its internal resistance doesn't exist or is treated as zero.

Symbol



DC voltage source

efficiency is 100%

(~) AC voltage source

Practical Voltage Source:

A voltage source in which internal resistance is not zero is called as practical voltage source.

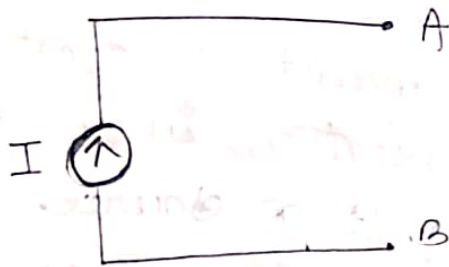


Symbol.

4) Ideal Current Source.

A current source that maintenance constant output current irrespective of variation in load is called an Ideal Current Source.

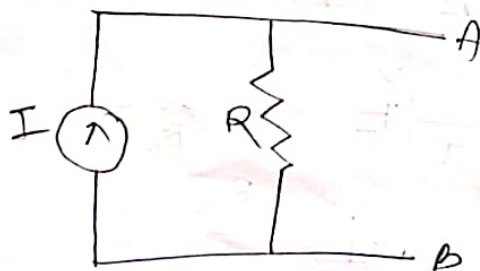
For ideal current source internal resistance R has a very high value tending to infinite.



Practical Current Source

A current source in which internal resistance has a finite value is treated as a Practical Current source.

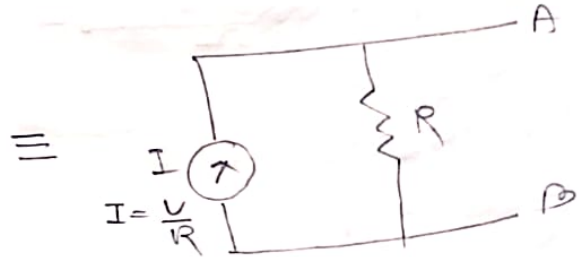
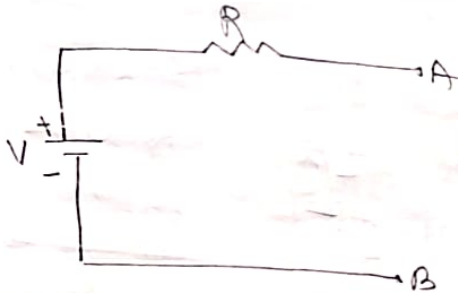
[A current source and resistance always connect in parallel.



[Ammeter connected in parallel.
Volt meter connected in series.

⑤ A voltage source and resistance always connected in series.

Source Conversion



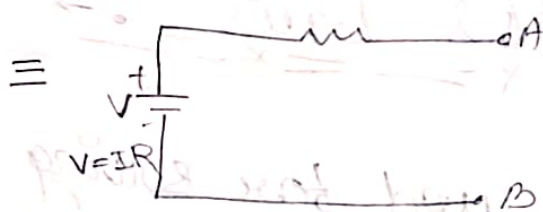
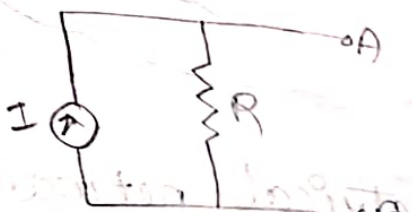
$$V = IR$$

$$\Rightarrow I = \frac{V}{R}$$

* Replacing a practical voltage source by an equivalent practical current source or vice versa is known as source conversion.

* The magnitude of current source will be

$$\boxed{I = \frac{V}{R}}$$

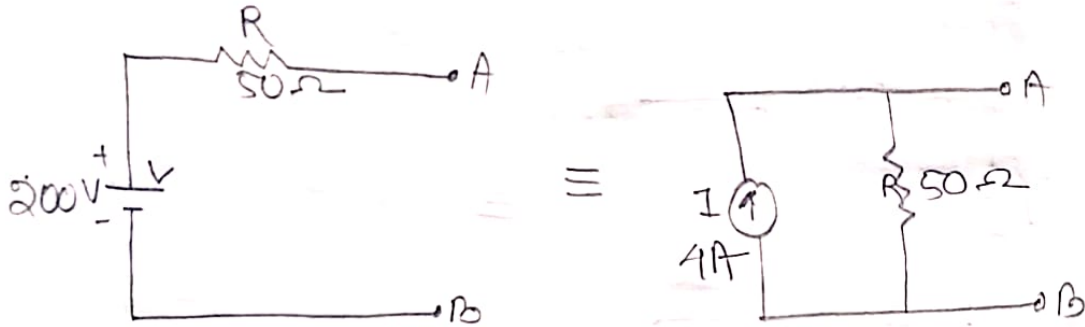


* The magnitude of voltage source will be

$$\boxed{V = IR}$$

⑥ Problem 1: By drawing proper circuit diagram Explain the source conversion if the given data are $V = 200V$ and $R = 50\Omega$?

Ans



Here $V = 200V$

and $R = 50\Omega$

from Ohm's Law $\Rightarrow V = IR$

$$\text{so } I = \frac{V}{R}$$

$$= \frac{200}{50}$$

$$= 4A$$

Kirchoff's Laws \Rightarrow

- * It is used for solving electrical network problems.
- * These laws are useful for determining the currents and voltages in different sections of electrical networks when circuit contains one or more active elements (voltage source & current source) and number of passive

Elements (Resistance, Inductance, Capacitance)

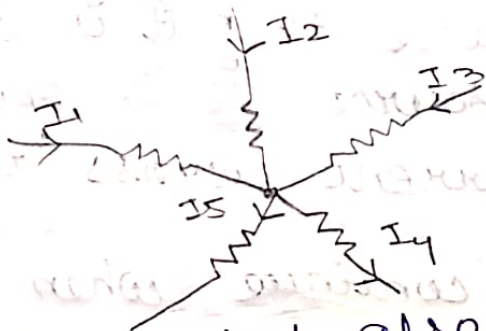
(7)

* Kirchhoff's Law is of two types

1. Kirchhoff's Current Law (KCL)
2. Kirchhoff's Voltage Law (KVL)

Kirchhoff's Current Law

Defⁿ:- It is otherwise known as junction Law. This law states that at a given instant the algebraic sum of all currents meeting at a given node and ~~go over~~ over a junction in a network is zero.



$$I_1 + I_2 + I_3 - I_4 - I_5 = 0$$
$$\rightarrow I_1 + I_2 + I_3 = I_4 + I_5 \quad \text{--- (1)}$$

from eqⁿ (1) KCL also states that the algebraic sum of all the currents meeting at a node or a junction at a given instant is equal to be algebraic sum of all the currents leaving the same node or junction.

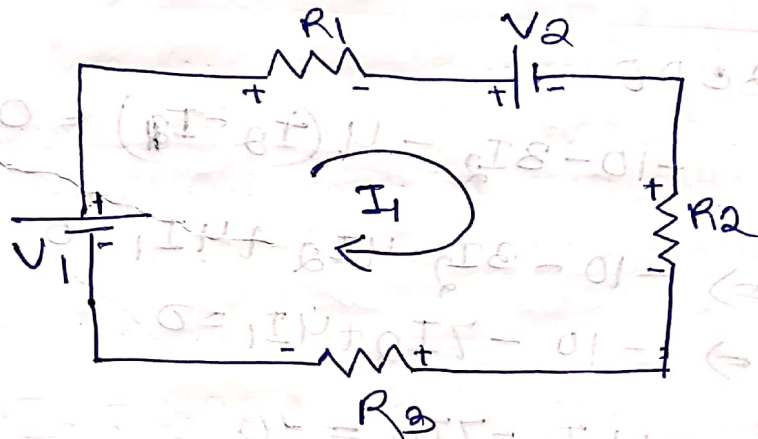
from eqⁿ KCL

From

Kirchhoff's Voltage Law (KVL)

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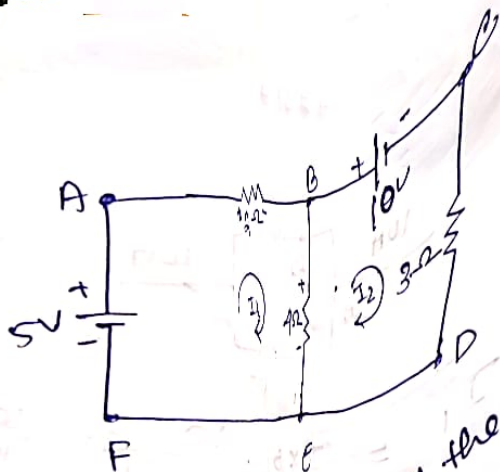
It states that the algebraic sum of voltages around a closed path of any electrical network at a given instant is zero.



$$+V_1 - IR_1 - V_2 + IR_2 - IR_3 = 0$$

$$\Rightarrow V_1 - V_2 = IR_1 + IR_2 + IR_3 \quad \dots (1)$$

From the eqn (1) the alternative statement of KVL which says that the algebraic sum of all source voltages at a given instant is equal to the algebraic sum of all voltage drops across the passive elements in any closed loop of a network.



find the currents flowing in all the
and voltage drop across the 4Ω
applying KVL.

In ABEF loop

$$5V - 2I_1 - 4(I_1 - I_2) = 0$$

$$\Rightarrow 5V - 2I_1 - 4I_1 + 4I_2 = 0$$

$$\Rightarrow 5V - 6I_1 + 4I_2 = 0$$

$$\Rightarrow 4I_2 - 6I_1 = -5 \quad (1)$$

Again In BCDE

$$-10 - 3I_2 - 4(I_2 - I_1) = 0$$

$$\Rightarrow -10 - 3I_2 - 4I_2 + 4I_1 = 0$$

$$\Rightarrow -10 - 7I_2 + 4I_1 = 0$$

$$\Rightarrow 4I_1 - 7I_2 = 10$$

Solving

(1) & (2)

$$4I_1 - 6I_2 = -5$$

$$-4I_1 + 4I_2 = -10$$

$$-2I_2 = -15$$

$$\Rightarrow I_2 = \frac{15}{2} = 7.5A$$

$$6I_1 - 4 \times (-1.53) = 5$$

$$\Rightarrow 6I_1 + 6.12 = 5$$

$$\Rightarrow 6I_1 = -1.12$$

$$\Rightarrow I_1 = -0.18 \text{ A}$$

at a given instant is 2020

$$I_2 = -1.53 \text{ A (from D to C)}$$

$$I_1 = -0.18 \text{ A (from B to A)}$$

$$I_2 - I_1 = -1.53 + 0.18 = -1.35 \text{ A (from B to E)}$$

$$\text{voltage drop across } 4\Omega = -1.35 \times 4 = -5.40 \text{ V}$$

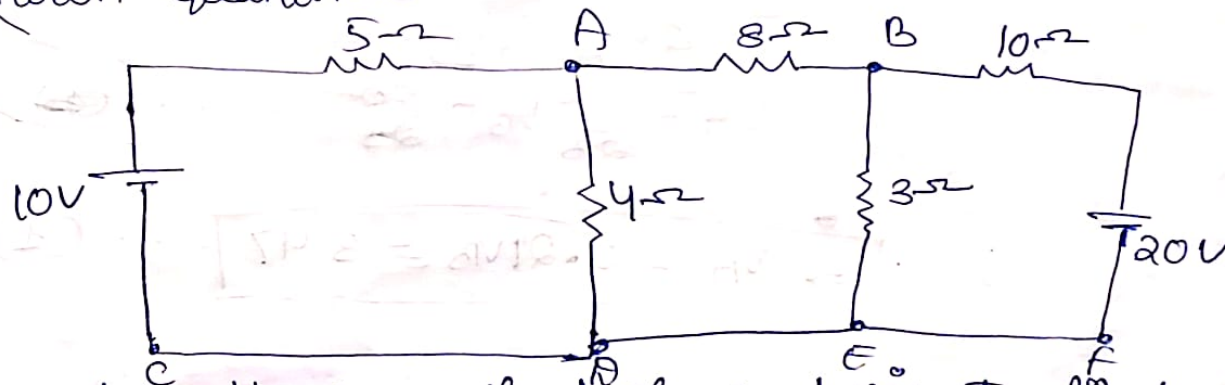
At. 27.08.19

Nodal Analysis

The node equation method is ~~best~~ based directly on Kirchhoff's current law.

The advantage is that a minimum number of equations needed to be written to determine the unknown quantities

Q11.

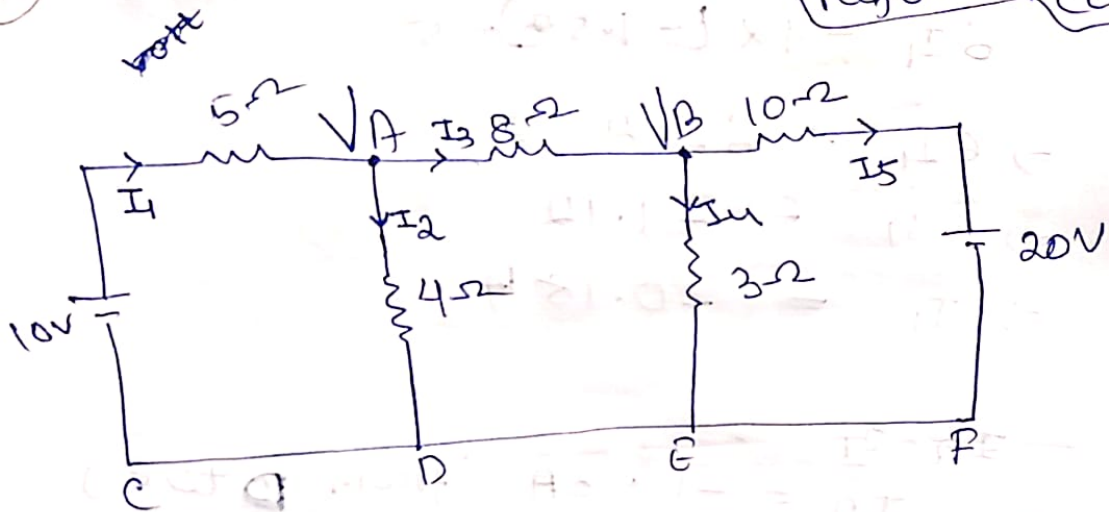


Apply the node voltage method of analysis to find
 a) The voltage across terminal A and B.
 b) Current through 8Ω resistor of the circuit in the fig.

Ans

(16)

reference node (C, D, E, F)



Step 1

considering node 1: VA

Applying Kirchhoff's current law at node 1, VA

$$I_1 = I_2 + I_3$$

$$\Rightarrow \frac{10 - V_A}{5} = \frac{V_A}{4} + \frac{V_A - V_B}{8}$$

$$\Rightarrow \frac{10 - V_A}{5} = \frac{2V_A + V_A - V_B}{8}$$

$$\Rightarrow 80 - 8V_A = 15V_A - 5V_B$$

$$\Rightarrow 80 = 23V_A - 5V_B$$

$$\Rightarrow V_A - \frac{5}{23}V_B = \frac{80}{23}$$

$$\Rightarrow V_A - 0.217V_B = 3.47 \quad \dots (1)$$

Step-2

Handwritten scribbles

Considering node 2, V_B

$$I_3 = I_4 + I_5$$

applying KCL at node 2, V_B

$$I_3 = I_4 + I_5$$

$$\Rightarrow \frac{V_A - V_B}{8} = \frac{V_B}{3} + \frac{V_B + 20}{10}$$

$$\Rightarrow \frac{V_A - V_B}{8} = \frac{10V_B + 3V_B + 60}{30}$$

$$\Rightarrow \frac{V_A - V_B}{8} = \frac{13V_B + 60}{30}$$

$$\Rightarrow 30V_A - 30V_B = 104V_B + 480$$

$$\Rightarrow 30V_A - 30V_B - 104V_B + 480 = 0$$

$$\Rightarrow 30V_A + 134V_B + 480 = 0$$

$$\Rightarrow V_A + \frac{134}{30}V_B + \frac{480}{30} = 0$$

$$\Rightarrow V_A + 4.46V_B + 16 = 0$$

$$\Rightarrow V_A - 4.46V_B = -16 \dots (2)$$

Solving eqn (1) & (2)

$$\begin{array}{r} V_A - 0.21V_B = 3.47 \\ (-) V_A + 4.46V_B = -16 \\ \hline 4.25V_B = 19.47 \end{array}$$

$$\Rightarrow V_B = \frac{19.47}{4.25} = 4.58 \text{ V}$$

$$V_A - 0.21 \times 4.58 = 3.47 \quad (\text{Putting value } V_B \text{ in eqn 1})$$

$$\Rightarrow V_A - 0.961 = 3.47$$

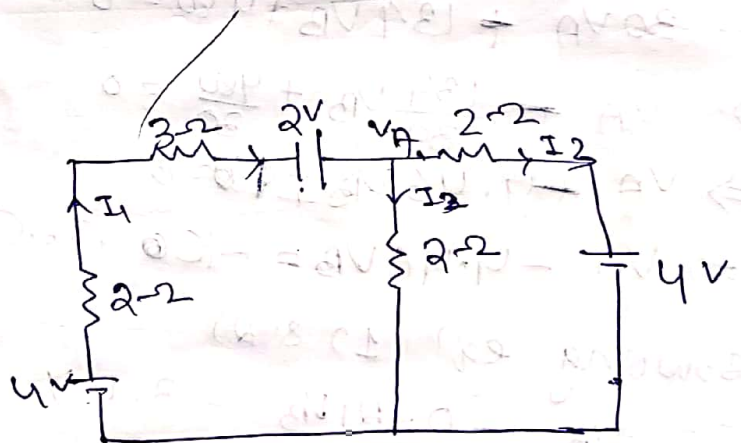
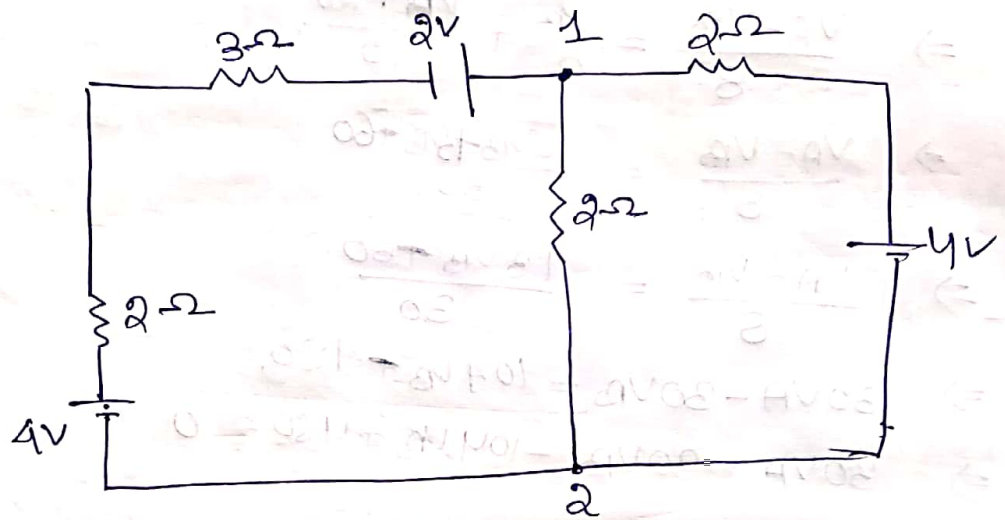
$$\Rightarrow V_A = 4.431 \text{ V}$$

$$V_{AB} = V_A - V_B = 4.431 - 4.58 = -0.14 \text{ V}$$

$$V_{BA} = 0.14V$$

$$b) \text{ current across the } 8\Omega = \frac{0.14}{8} \\ = 0.017A$$

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$$I_1 = I_2 + I_3$$

$$\Rightarrow \frac{4+2-V_A}{3+2} = \frac{V_A}{2} + \frac{V_A-4}{2}$$

$$\Rightarrow \frac{6-V_A}{5} = \frac{V_A + V_A - 4}{2}$$

$$\Rightarrow \frac{6-V_A}{5} = V_A - 2$$

$$\Rightarrow 6 - V_A = 5V_A - 10$$

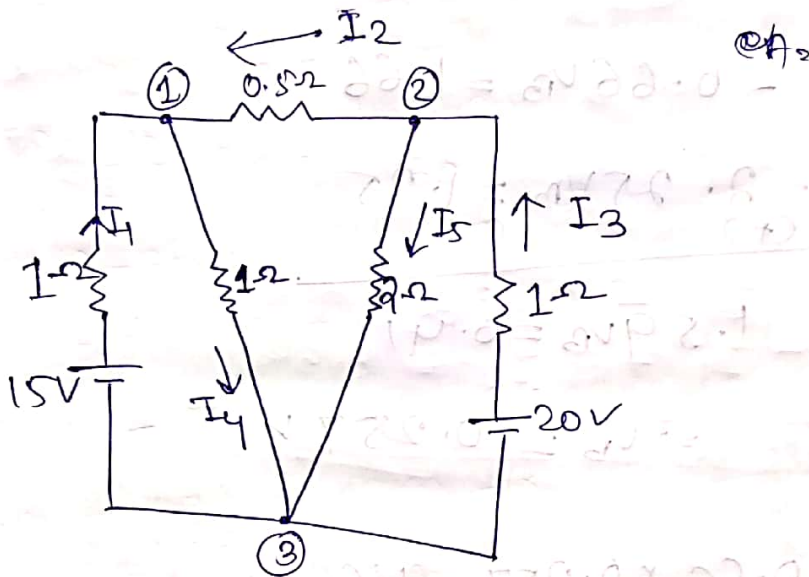
$$\Rightarrow 6 \text{ VA} = 16$$

$$\Rightarrow V_A = 2.66 \text{ V}$$

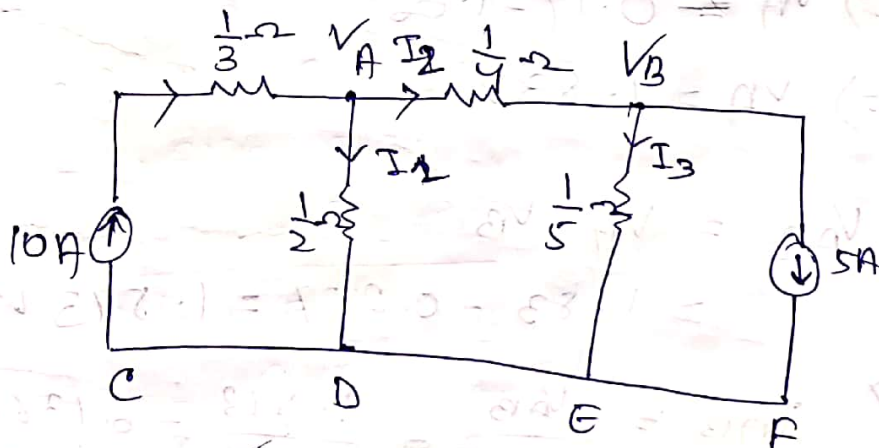
current through $3\text{-}\Omega$ is I_1

$$I_1 = \frac{6 - V_A}{5} = \frac{6 - 2.66}{5} = \frac{3.34}{5} = 0.66 \text{ A}$$

3)



4)



$$10 = \frac{V_A}{\frac{1}{2}} + 4V_A - 4V_B$$

$$\Rightarrow 10 = 2V_A + 4V_A - 4V_B$$

$$\Rightarrow 10 = 6V_A - 4V_B$$

$$\Rightarrow V_A = 0.66V_B \Rightarrow V_A - 0.66V_B = 0.66$$

Considering V_B

$$I_2 = I_3 + 5$$

$$\Rightarrow 4V_A - 4V_B = 5V_B + 5$$

$$\Rightarrow 4V_A = 9V_B + 5$$

$$\Rightarrow V_A - 2.25V_B = 1.25 \quad \text{--- (1)}$$

$$V_A - 0.66V_B = 1.66$$

$$\begin{array}{r} \leftarrow V_A - 2.25V_B = 1.25 \\ \leftarrow \end{array}$$

$$1.59V_B = 0.41$$

$$\Rightarrow V_B = 0.257 \text{ V}$$

$$V_A - 0.66 \times 0.257 = 1.66$$

$$\Rightarrow V_A = 0.17 = 1.66$$

$$\Rightarrow V_A = 1.83 \text{ V}$$

$$\text{a) } V_{AB} = V_A - V_B$$

$$= 1.83 - 0.257 = 1.573 \text{ V}$$

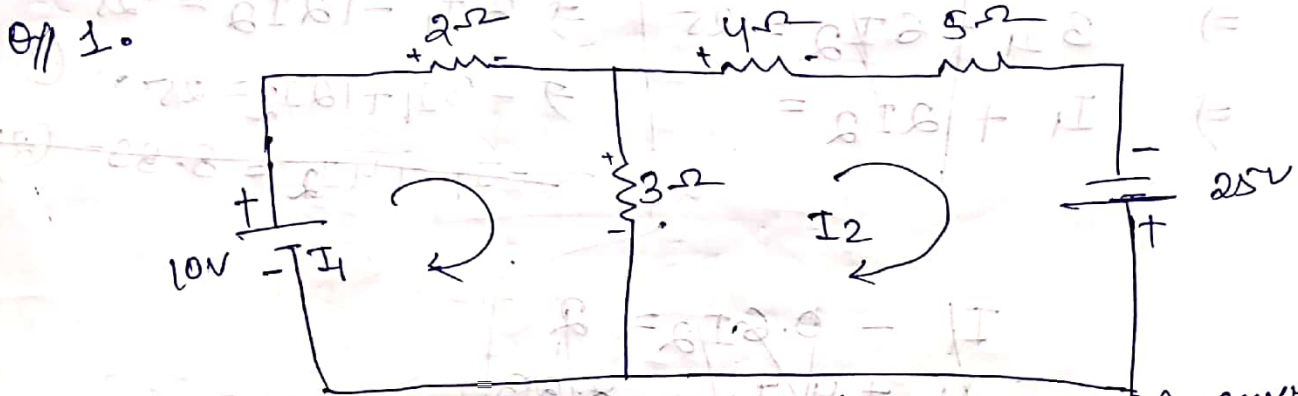
$$\text{b) } I_{AB} = \frac{V_{AB}}{0.25} = \frac{1.573}{0.25} = 6.136 \text{ A}$$

(A → B)

Mesh Analysis

St. 29.08.18

* This method is effective for finding the branch currents and voltages across elements of an electrical network by the way of finding currents for each closed loops (mesh).
 * It is applicable base Kirchoff's voltage law.



Apply the mesh current method to find the current through 3Ω and 4Ω resistor of the given circuit.

Ans Applying KVL for loop (1)

$$+10 - I_1 R_1 - 3(I_1 - I_2) = 0$$

$$\Rightarrow -10 - 2I_1 - 3I_1 + 3I_2 = 0$$

$$\Rightarrow 10 - 5I_1 + 3I_2 = 0$$

$$\Rightarrow -5I_1 + 3I_2 + 10 = 0$$

$$\Rightarrow 5I_1 - 3I_2 = 10 \quad \dots \text{--- (1)}$$

$$\Rightarrow I_1 - \frac{3}{5}I_2 - 2 = 0$$

$$\Rightarrow I_1 - 0.6I_2 - 2 = 0$$

$$\Rightarrow I_1 - 0.6I_2 = 2 \quad \dots \text{--- (2)}$$

Applying for loop-2

$$+25 - 3(I_2 - I_1) - 4I_2 - 5I_2 = 0$$

$$\Rightarrow 25 - 3I_2 + 3I_1 - 4I_2 - 5I_2 = 0$$

$$\Rightarrow 25 - 3I_1 - 6I_2 = 0$$

$$\Rightarrow -3I_1 - 6I_2 = -25$$

$$\Rightarrow 3I_1 + 6I_2 = 25$$

$$\Rightarrow I_1 + 2I_2 = \frac{25}{3}$$

$$\Rightarrow 25$$

$$\Rightarrow 25 + 3I_1 - 12I_2 = 0$$

$$\Rightarrow 3I_1 - 12I_2 = -25$$

$$\Rightarrow -3I_1 + 12I_2 = 25 \quad (2)$$

$$\Rightarrow -I_1 + 4I_2 = 8.33 \quad (2')$$

$$I_1 - 0.6I_2 = 2$$

$$-7I_1 + 4I_2 = 8.33$$

The loop expression (1) & (2) may be arranged in a matrix form.

$$[A] [I] = [V]$$

$$\begin{bmatrix} 5 & -3 \\ -3 & 12 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} 10 \\ 25 \end{bmatrix}$$

which can be solved by Cramer's Rule to get the unknown values of I_1 & I_2

$$\text{For finding } I_1 = \frac{\begin{vmatrix} 10 & -3 \\ 25 & 12 \end{vmatrix}}{\begin{vmatrix} 5 & -3 \\ -3 & 12 \end{vmatrix}}$$

$$I_1 = \frac{120 + 75}{60 + 9}$$

$$= \frac{195}{69}$$

$$= 3.82 \text{ A}$$

for finding I_2

$$= \frac{\begin{bmatrix} 5 & 10 \\ -3 & 25 \end{bmatrix}}{\begin{bmatrix} 5 & -3 \\ -3 & 12 \end{bmatrix}}$$

$$= \frac{125 + 30}{51}$$

$$= \frac{155}{51}$$

$$= 3.03 \text{ A (current flow } 4 \Omega)$$

current through 3Ω

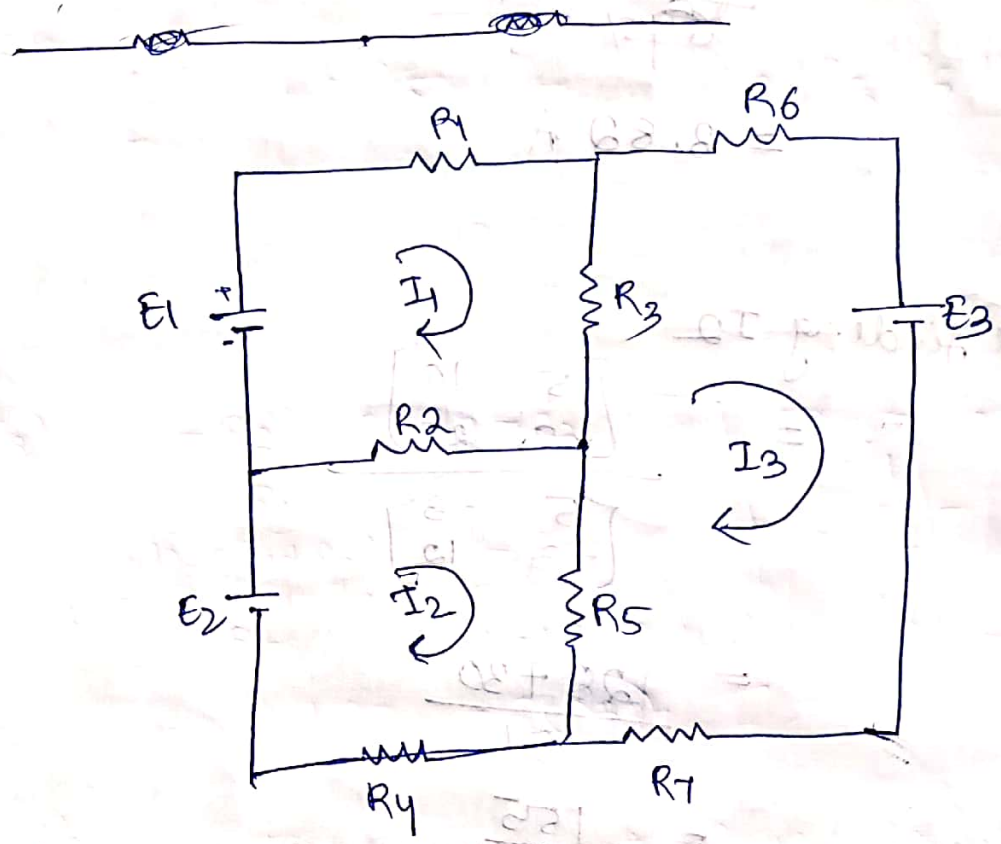
$$= I_1 - I_2$$

$$= 3.82 - 3.03$$

$$= 0.79 \text{ A}$$

Mesh Analysis using Matrix form :-

and $V_{E2} - R_2(I_2) - R_5(I_2 - I_3) - R_4 I_2$



Applying KVL in first mesh (1) :-

~~$+E_1 - I_1 R_1 - I_1 (R_3 - R_1) - I_1 R_2$~~

$E_1 - I_1 R_1 - R_3 (I_1 - I_3) - R_2 (I_1 - I_2) = 0$

$\Rightarrow E_1 - I_1 R_1 - I_1 R_3 + I_3 R_3 - I_1 R_2 + I_2 R_2 = 0$

$\Rightarrow E_1 - I_1 (R_1 + R_2 + R_3) + I_2 R_2 + I_3 R_3 = 0$

$\Rightarrow E_1 = I_1 (R_1 + R_2 + R_3) - I_2 R_2 - I_3 R_3$

$\Rightarrow (R_1 + R_2 + R_3) I_1 - R_2 I_2 - R_3 I_3 = E_1 \quad (1)$

mesh-2

$$E_2 - (I_2 - I_1) R_2 - R_5 (I_2 - I_3) - R_4 I_2 = 0$$

$$\Rightarrow \cancel{E_2 - (I_2 - I_1) R_2 - R_5 (I_2 - I_3)}$$

$$E_2 - (I_2 - I_1)$$

$$\Rightarrow E_2 - R_2 I_2 + R_2 I_1 - R_5 I_2 + R_5 I_3 - R_4 I_2 = 0$$

$$\Rightarrow E_2 - I_2 (R_2 + R_5 + R_4) - R_2 I_1 + R_5 I_3 = 0$$

$$\Rightarrow E_2 = I_2 (R_2 + R_5 + R_4) + R_2 I_1 - R_5 I_3$$

$$\Rightarrow R_2 I_1 - R_5 I_3 + I_2 (R_2 + R_5 + R_4) = E_2 \quad \dots (2)$$

mesh-3

$$E - I_3 R_6 - R_3 (I_3 - I_1) - R_5 (I_3 - I_2) - I_3 R_7 = 0$$

$$\Rightarrow E - I_3 R_6 - R_3 I_3 + R_3 I_1 - R_5 I_3 + R_5 I_2 - I_3 R_7 = 0$$

$$\Rightarrow E - I_3 (R_6 + R_3 + R_5 + R_7) + R_3 I_1 + R_5 I_2 = 0$$

$$\Rightarrow I_3 (R_6 + R_3 + R_5 + R_7) - R_3 I_1 - R_5 I_2 = E \quad \dots (3)$$

$$(R_1 + R_2 + R_3) \quad -R_2 \quad -R_3$$

$$-R_2 \quad (R_2 + R_4 + R_5) \quad -R_5$$

$$-R_3 \quad -R_5 \quad (R_3 + R_5 + R_6 + R_7)$$

$$\begin{bmatrix} \textcircled{R_{11}} & & \\ (R_1 + R_2 + R_3) & -R_2 & -R_3 \\ -R_2 & \textcircled{R_{22}} & -R_5 \\ -R_3 & -R_5 & (R_3 + R_5 + R_6 + R_7) \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ E_3 \end{bmatrix}$$

This is the matrix equivalent of the above three equations

R_{11} = Self resistance of mesh 1

R_{22} = Self resistance of mesh 2

that is sum of all the resistances present in

the mesh 2

R_{33} = Self resistance of mesh 3

that is the sum of all the resistances present in mesh 3

$$R_{12} = +R_{21} = \left(\text{Sum of all the resistances common to mesh (1) and mesh (2)} \right)$$

$$R_{23} = R_{32} = - \left(\text{Sum of all the resistances common to mesh (2) \& (3)} \right)$$

$$R_{13} = R_{31} = - \left(\text{Sum of all the resistances common to mesh (3) \& (1)} \right)$$

using the symbols the generalised form of the above matrix equivalent can be written as

$$\begin{bmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ E_3 \end{bmatrix}$$

Note

- * All the self resistances will be always positive.
- * All the mutual resistances will be always negative.

Q1 write the impedance matrix of the network shown in the figure and find the value of I_3

Superposition Theorem \Rightarrow

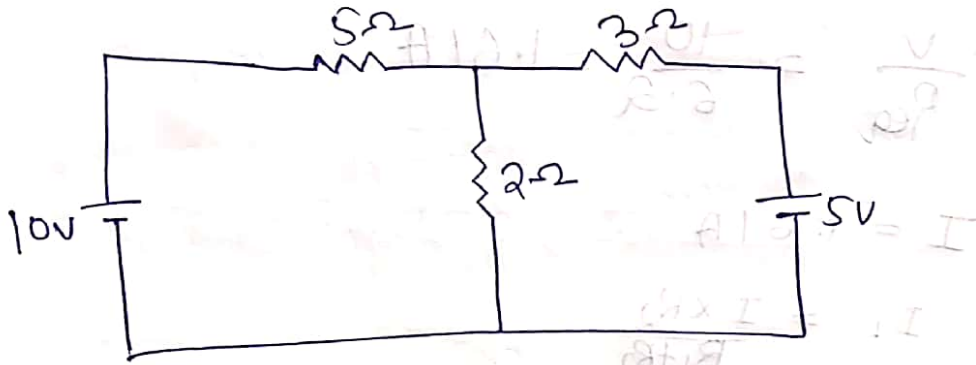
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In a linear bilateral circuit containing more than one source of energy the overall effect of all the sources considered simultaneously, each same as the algebraic sum of individual effects, of each source considered one at a time and being independent of all other sources.

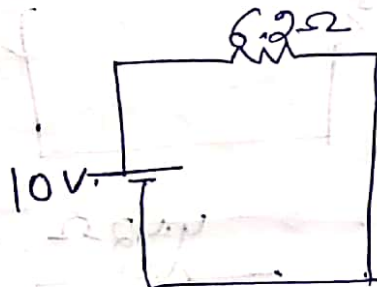
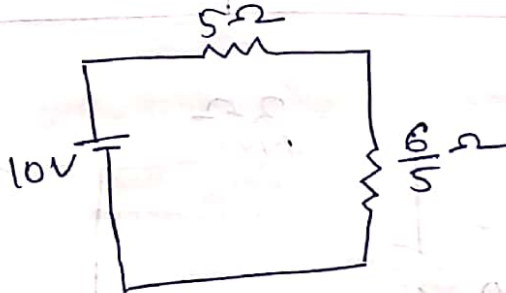
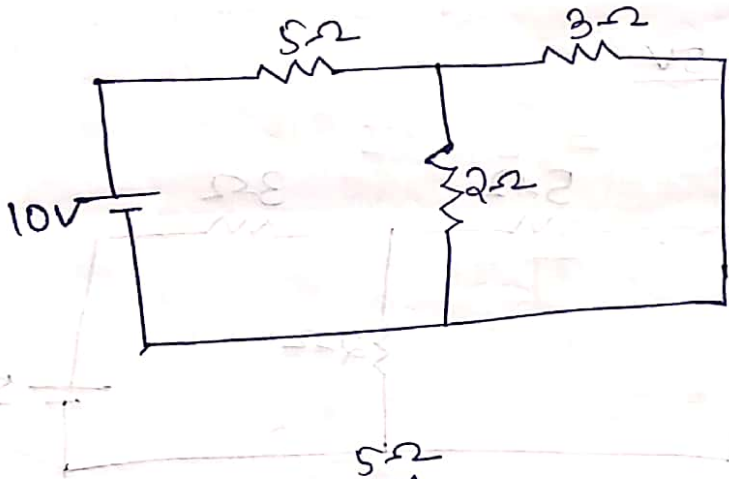
- * In superposition theorem if there are more than one source consider one source at a time, other source may be short circuit or open circuit.
- * If it is a voltage source then it is short circuit.
If it is a current source it is open circuit.
- * Then find the current across the particular branch.
- * Same process will continue when considering the other source.
- * In the end considering both the sources find the current across the particular branch.

Q:- Find current across 2Ω



Step-1

considering 10V



$$V = 10V$$

$$R_{eq} = 6.2\Omega$$

$$I = \frac{V}{R_{eq}} = \frac{10}{6.2} = 1.61A$$

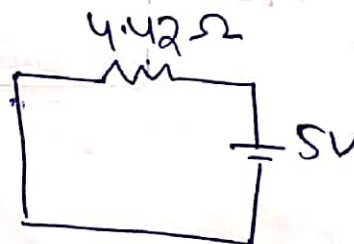
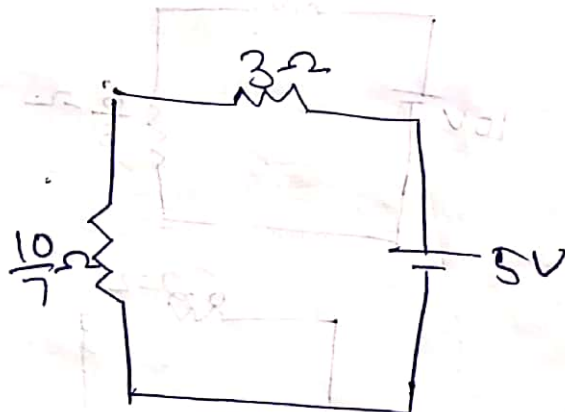
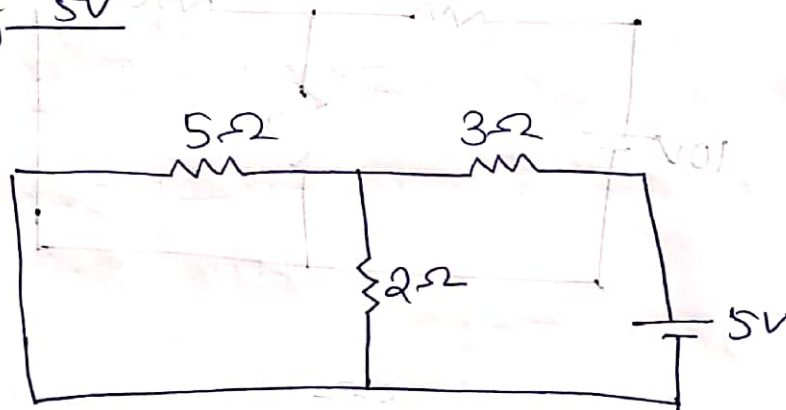
$$I = 1.61A$$

$$I_1 = \frac{I \times R_2}{R_1 + R_2}$$

$$= \frac{1.61 \times 3}{2 + 3} = \frac{4.83}{5} = 0.966A$$

Step-2

Considering 5V

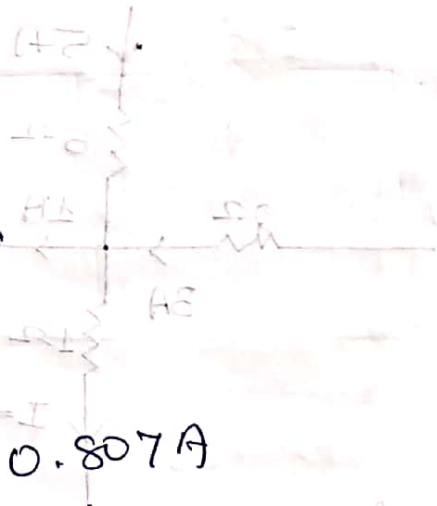


$V = 5V$

$R = 4.42 \Omega$

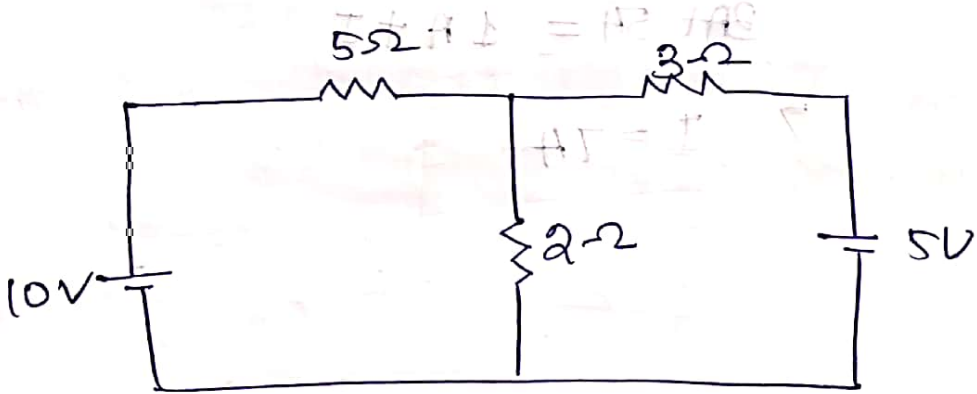
$I = \frac{V}{R} = \frac{5}{4.42} = 1.131 A$

$I_2 = \frac{1.131 \times 5}{2+5} = \frac{5.655}{7} = 0.807 A$



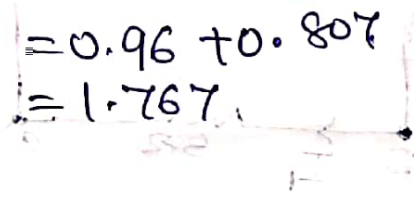
Step-3

considering Both voltage source 10V & 5V

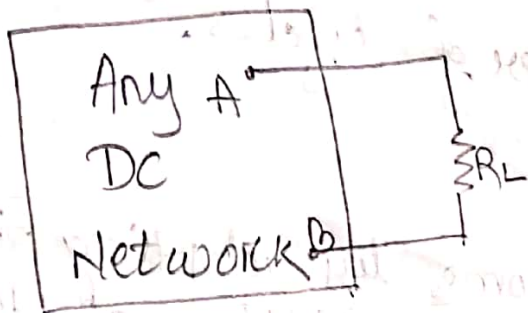


When I consider 10V the current across 2 Ohm resistance is downward, when I consider 5V voltage source the current across the 2 Ohm is also downward, so that the current across 2 Ohm will be.

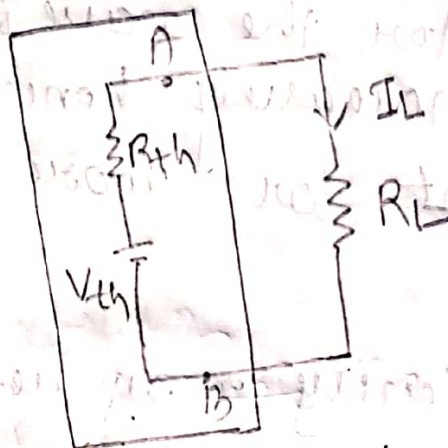
$I = 0.96 + 0.807 = 1.767$



THEVENIN'S THEOREM



A - Original network



B - Thevenin's equivalent circuit.

Defⁿ:- In order to find the response through any particular element connected across a pair of terminals A & B of a linear active network the rest of the network may be replaced by a Thevenin's equivalent circuit containing a voltage source called Thevenin's voltage V_{th} and a series resistance called Thevenin's resistance R_{th} .

For ~~the~~ it may be noted that V_{th} is the open circuit potential difference across A & B due to rest of the network in the absence of R_L (load resistance), and R_{th} is the equivalent resistance of rest of the network as viewed from terminals A & B in the absence of R_L with all the source made inactive.

$$I_L = \frac{V_{th}}{R_{th} + R_L} \quad \dots (1)$$

$$V_{AB} = I_L \times R_L \quad \dots (2)$$

Step-1

Replace the current sources if any equivalent voltage sources.

Step-2

Identify a pair of terminals A & B across the desired element and mark it as R_L .

Step-3

Find the voltage across A & B in the absence of R_L and mark as V_{th} .

Step-4

Replace all voltage sources with circuit resistance by calculate the equivalent network from ~~maintain~~ into the network from

the open terminals A & B and mark this as R_{th} .

Step-5

Draw the Thevenin's equivalent circuit as shown in the fig. B

Step-6

solve for current & voltage as per the eqn. no (1) & (2)



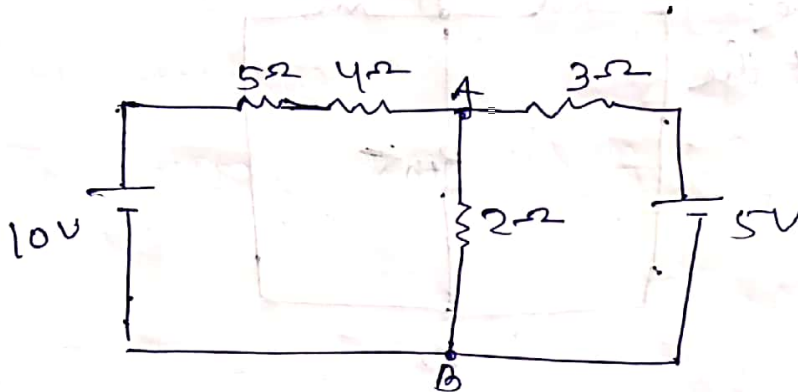
Q.1

Find the current flowing through the 2Ω resistor of the circuit shown in the fig. below by applying Thevenin's Theorem.



Step-1

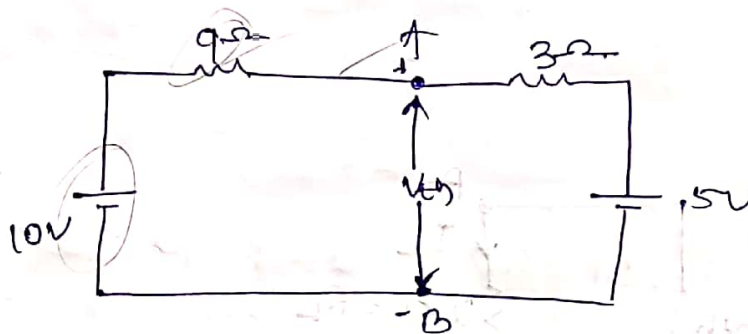
Replacing the current source as voltage source we got the circuit diagram as given below.



choice.

Step-2

for finding V_{th}



$$1-\phi = 230$$
$$3-\phi = R \text{ } \phi$$

Applying KVL on the circuit we get

$$10 - 9I - 3I - 5 = 0$$

$$\Rightarrow 10 - 12I - 5 = 0$$

$$\Rightarrow 5 = 12I$$

$$\Rightarrow I = \frac{5}{12} = 0.417 \text{ A}$$

$$10 - 9I - V_{th} = 0$$

$$V_{th} + 5 - 3I = 0$$

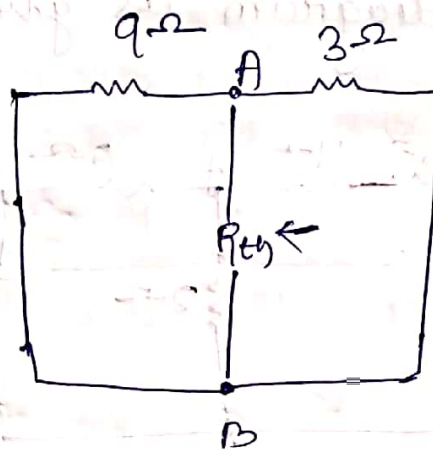
$$V_{th} = \frac{10 - 9 \times 0.417}{1}$$
$$= \frac{10 - 3.69}{1}$$
$$= 6.31 \text{ V}$$

$$5 + 3 \times 0.417$$
$$= 6.317$$

Step-3

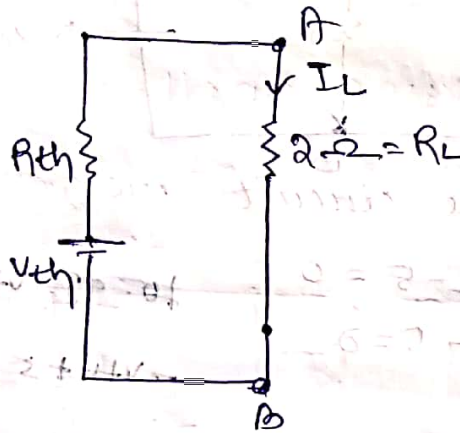
For finding R_{th}

For calculate R_{th} , circuit the voltages



$$R_{th} = \frac{9 \times 3}{9 + 3} = \frac{27}{12} = 2.25 \Omega$$

Step-4

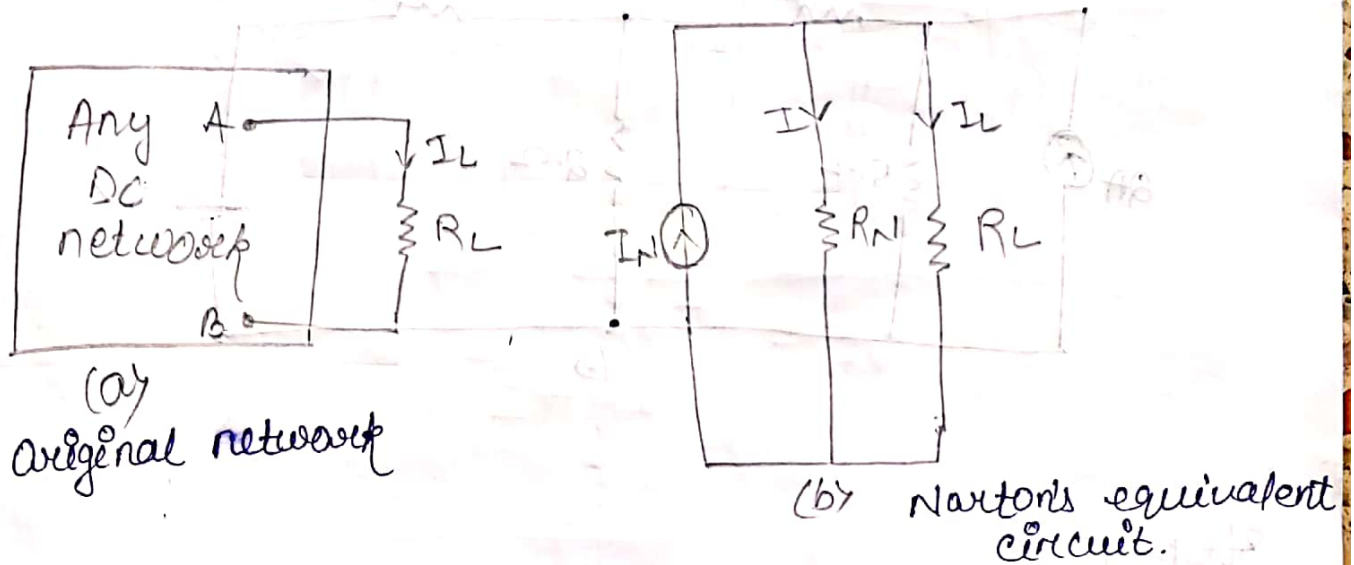


$$I_L = \frac{V_{th}}{R_{th} + R_L} = \frac{6.31}{2.25 + 2} = \frac{6.31}{4.25}$$

$$= 1.48 A$$

NORTON'S THEOREM

It is the opposite of Thevenin's Theorem. Application of this theorem becomes easier if the network contains current source only.

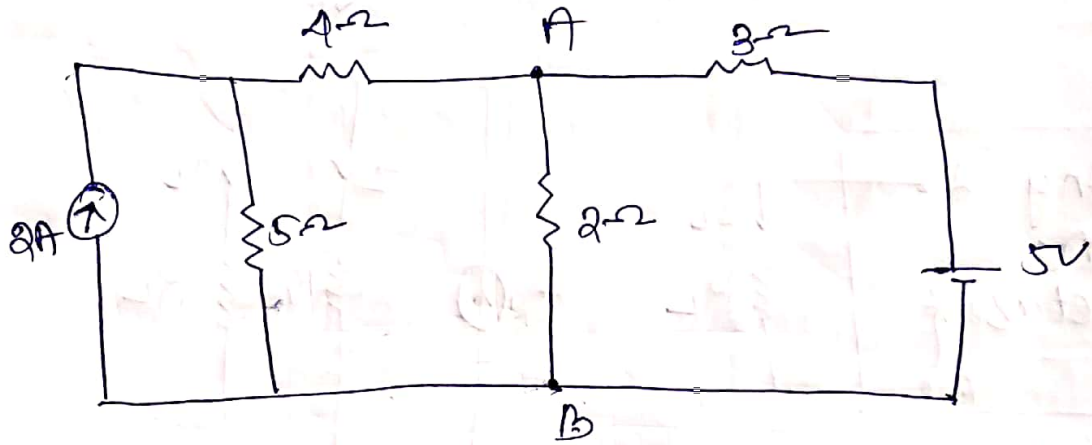


Defⁿ: In order to find the response through any particular element connected across a pair of terminals A & B of a linear active DC network, the rest of the network may be replaced by a Norton's equivalent circuit. Containing a current source called Norton current (I_N) and parallel resistance called Norton's Resistance (R_N).

$$I_L = \frac{I_N \times R_N}{R_N + R_L}$$

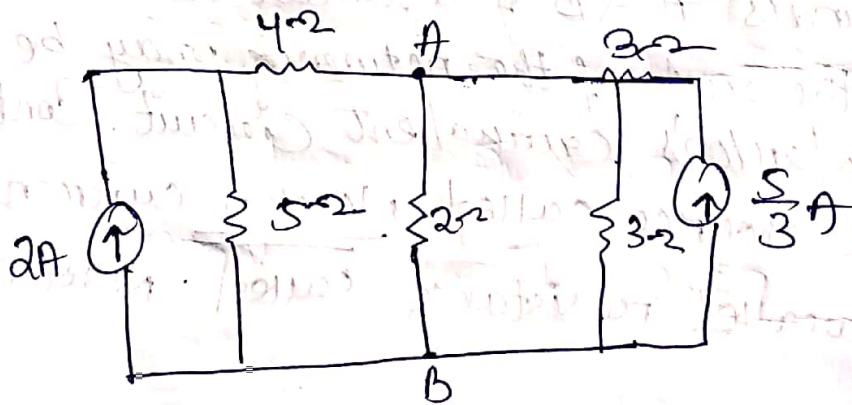
Q.1

Find the current flowing in the 2Ω Resistor of the circuit shown in the figure below by applying Norton's theorem.



Step-1

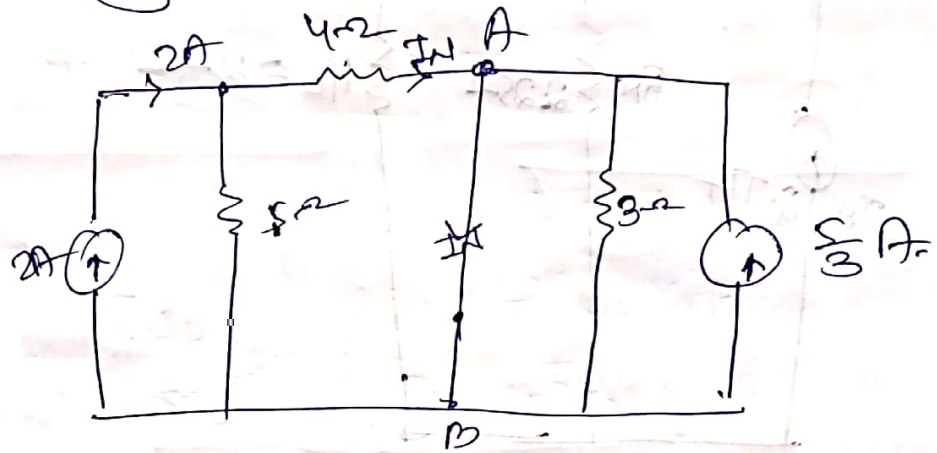
Converting voltage source to current source



Step-2

For finding I_N which is the circuit current that would flow through A & B. Due to the rest of the network

with R_L replaced by the short circuit. to find this we may redraw the network by replacing the 2Ω resistor by short circuit.

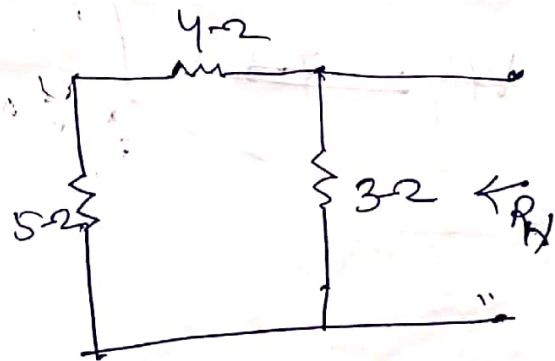


$$\begin{aligned}
 I_N &= \left(\frac{2 \times 5}{5+4} \right) + \frac{5}{3} \\
 &= \frac{10}{9} + \frac{5}{3} \\
 &= \frac{10+15}{9} = \frac{25}{9} = 2.77 \text{ A}
 \end{aligned}$$

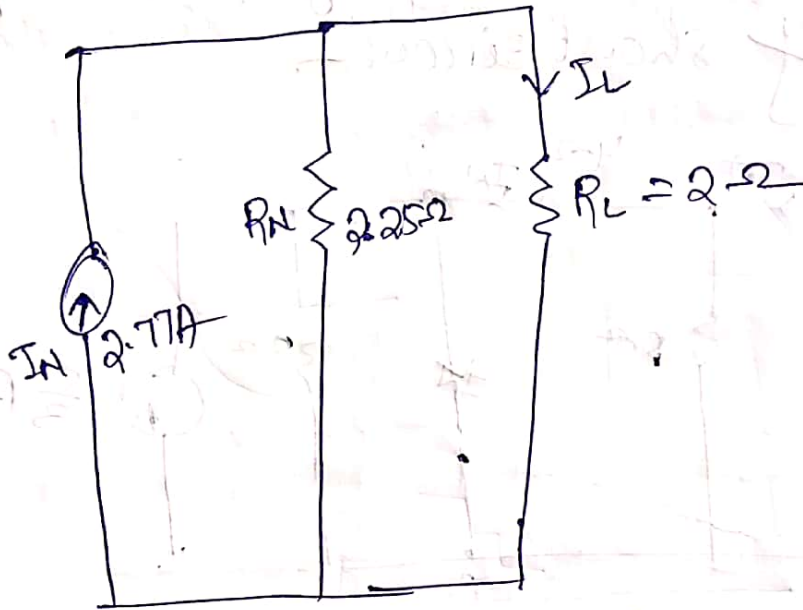
Step-3

For finding R_N which is the resistance of the network viewed from A & B with all the source inactive.

$$\begin{aligned}
 R_{eq} &= \frac{9 \times 3}{9+3} \\
 &= \frac{27}{12} \\
 &= 2.25 \Omega
 \end{aligned}$$



Step 4



$$I_L = \frac{I_N \times R_N}{R_N + R_L}$$
$$= \frac{2.77 \times 2.25}{2 + 2.25}$$

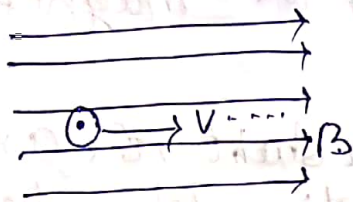
$$= 1.46\text{ A}$$

Single Phase (1- ϕ) AC Circuits

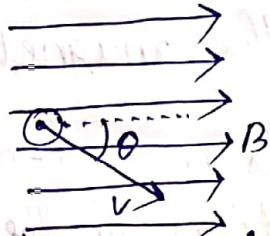
The basic object of this chapter is to familiarize with 1- ϕ AC generation and the basic nature of 1- ϕ emf.

1- ϕ emf generation:

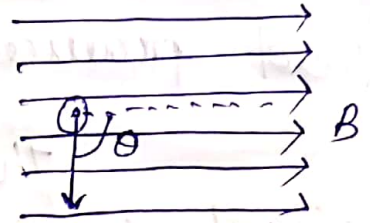
1- ϕ emf generation is based on the principle of dynamically induced or motional emf. According to this principle, a conductor of length l while moving at a velocity v making an angle θ to a steady magnetic field of flux density B , becomes the seat of a dynamically induced emf e as described in the figure below.



a) $\theta = 0^\circ, e = 0$



b) $0^\circ < \theta < 90^\circ$
 $e = Blv \sin \theta$



c) $\theta = 90^\circ$
 $e = Blv$

Dynamic induced emf in a conductor.

In the above figure the emf induced may have different values for different equations.

$$e = Blv \sin \theta \quad \text{----- (1)}$$

This principle may be extended to obtain 1- ϕ emf in a coil as per the arrangement shown in the figure below.

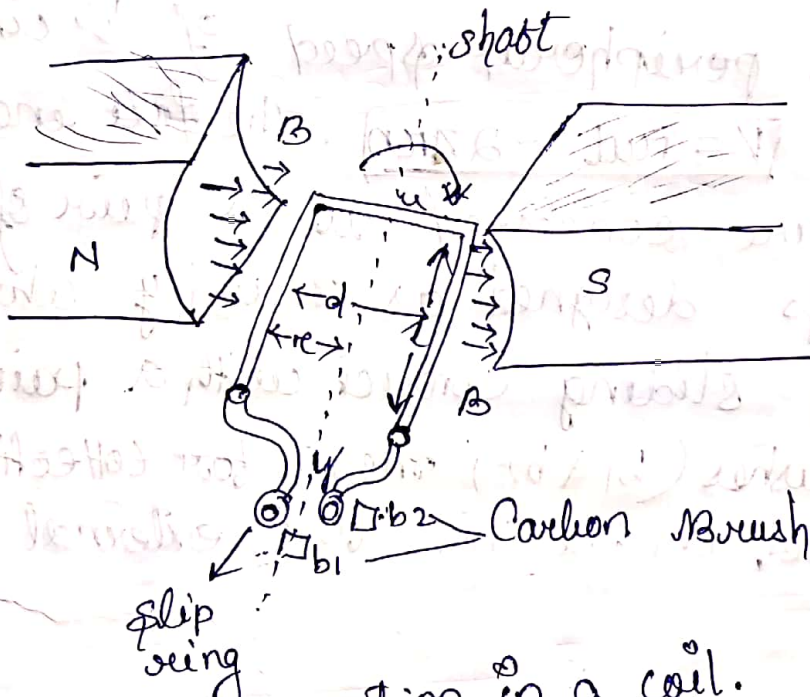


Figure 1- ϕ emf generation in a coil.
 The simplest practical case consist of a pair of magnetic poles designed as N (north pole) and S (south pole) in the form of a permanent magnet with a coil placed between, which is freely rotate about

an axis \perp to the direction of the magnetic field produced by the magnet

The coil is mounted on a shaft, the axis being \perp to the direction of the magnetic field. When the shaft is made to rotate at n revolutions per second (rps), it produces an angular speed

units (rad/sec) such as $\omega = 2\pi n$. The coil also assumes the same angular speed. The coil during its rotation describes a circle, the radius of which may be taken as r units (m) such as $r = d/2$. As the coil rotates in the space, the conductors assume a peripheral speed of v units (m/s) given by $v = r\omega = 2\pi rn$. The free ends of the coil are connected to a pair of isolated slip rings designed as x and y which form a kind of sliding contact with a pair of fixed carbon brushes (b_1 & b_2) meant for collection of the emf induced in the coil for external use.

Dt. 10.09.19

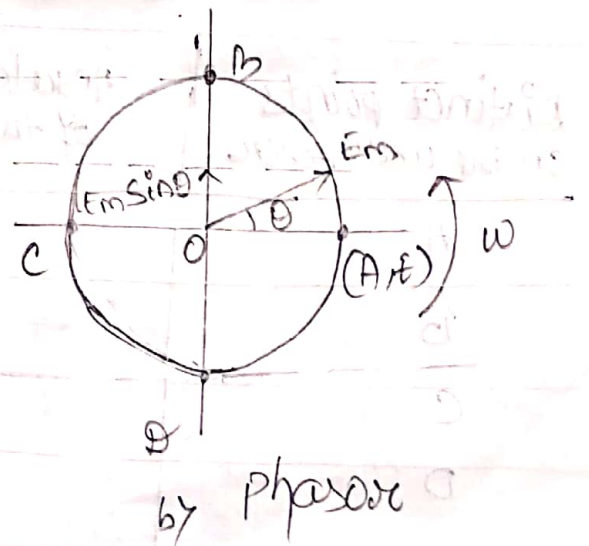
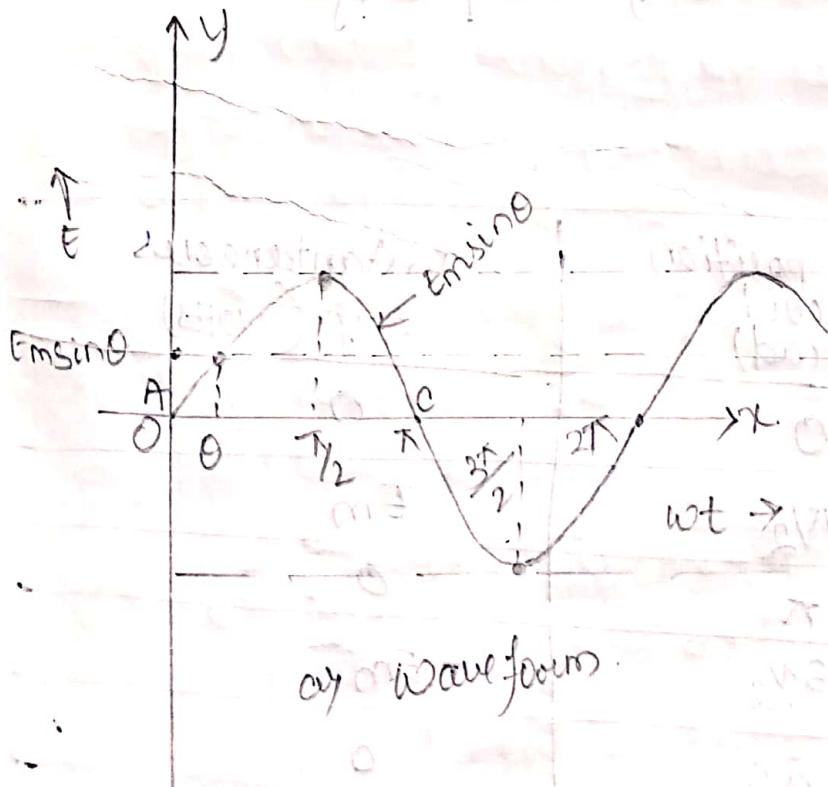
Sinusoidal wave form and phasor representation of EMF.

With the help of graphical means it is possible to have a better feel of vibrations. Variations of the single phase $(\sin \phi)$ emf represented in the equation no-4 with respect to time and angular positions of the coil.

Two familiar techniques used for this purposes are

1. Wave form representation
2. Phasor representation

1. Wave form Representation of EMF ::



In this technique the variation of ϵ as obtained from equation no-4 are plotted as a function of θ or ωt in a Cartesian coordinate system. This gives the plot of fig. A which is the result of the step by step plotting of instantaneous emf ϵ taken along y-axis corresponding to respective values of θ or ωt taken along x-axis.

A few distinct points of this waveform are highlighted in the table given below along with the information about the angular position and instantaneous emf there of

* Table \rightarrow
 Variation of instantaneous emf with angular position.

Distinct points on the waveform	Angular position of the coil (rad)	Instantaneous emf (volts)
A	0	0
B	$\pi/2$	E_m
C	π	0
D	$3\pi/2$	$-E_m$
E	2π	0

A complete revolution of the coil corresponds to one complete cycle or 2π radians or 360°

In view of this the plotting of the above figure is limited to one full cycle only.

2. Phasor Representation of Emf

As the number of cycles increases the length of the plot under the wave form representation technique goes on increasing hence the technique may not be convenient for flexible more number of cycles.

This difficulty may be overcome by adopting phasor techniques. ~~the~~ A phasor representation of the instantaneous emf is shown in the fig. b. in which the instantaneous variation of emf over a full cycle corresponds to one complete revolution of a phasor along a predefined circle.

Thus a rotating phasor is the key concept of this technique which is shown with the help of an arrow taking a particular radial position at a particular instant of time. the arrow has a fixed length equal to the magnitude of the peak emf E_m .

The direction of rotation of phasor is shown by the arrow mark, corresponding to ω which is in accordance with direction of rotation of coil.

for a particular instant of time t the phasor gets positioned at the corresponding angular position, indicated by $\theta = \omega t$.

The projection over to the y -axis drawn from the tip of the phasor at a particular position indicates the instantaneous value of the emf at that instant, thus satisfying equation (4) in every rep.

The salient points (A, B, C, D, E) in the above figure have also been corresponding between the two forms of representⁿ is that one complete cycle representation of the waveform in the fig (a) is equivalent to one complete revolution of the phasor in figure (b).

Note:

Phase and phase difference are two commonly used terms associated with waveforms & phasor.

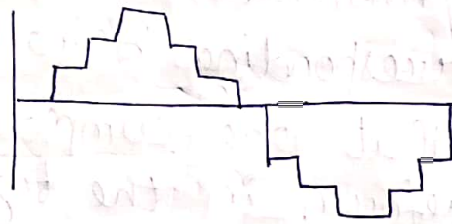
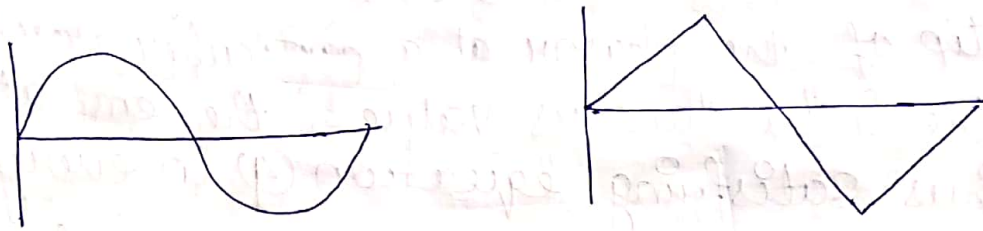
Phase of a phasor is defined as the instantaneous angular position of a waveform or phasor.

It is denoted by the symbol θ or ωt .

On the other hand phase difference is the angular difference between two waveforms or phasor as regards to their starting point. It is denoted by the symbol ϕ .

Cycle

one complete set of the \pm ve value of alternating quantity is called as cycle.



Time Period

The time taken by an alternating quantity to complete one cycle is called its time period T .

Exp: A 50 Hz alternating current has a time period of $1/50$ second.

Frequency :-

The number of cycles/second is called the frequency of the alternating quantity.

Amplitude

The maximum value, +ve or -ve of an alternating quantity is known as its amplitude.

Q. A coil rotating at 1000 RPM in a uniform magnetic field induces a sinusoidal emf of peak value of 100V. If the time is recorded as $t=0$ corresponding to 0 instantaneous emf, how long would it take for the instantaneous emf to attend a value of 30V for the first time.

$$E_m = \text{peak value}$$

$$E = 30V$$

Ans

$$n = 1000 \text{ RPM}$$

$$= \frac{1000}{60} = 16.66 \text{ RPS}$$

$$E_m = 100 \text{ V}$$

$$t = 0$$

$$E = E_m \sin \omega t$$

$$\omega = 2\pi n$$

$$= 2\pi \times 16.66$$

$$= 33.32\pi$$

$$= 33.32 \times 3.14$$

$$= 104.62$$

$$E = 30V$$

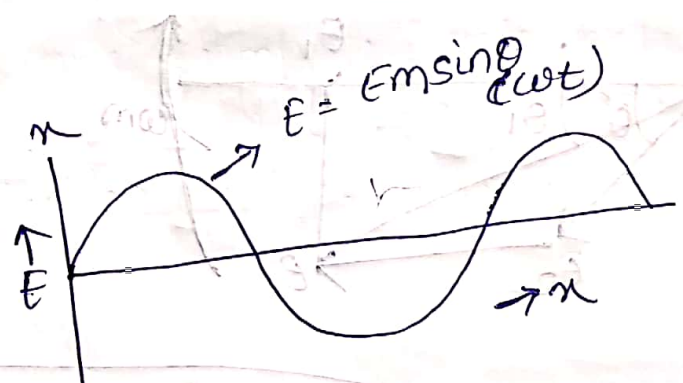
$$E = E_m \sin \omega t$$

$$\Rightarrow 30 = 100 \sin \omega t$$

$$\Rightarrow \sin \omega t = \frac{30}{100}$$

$$\Rightarrow \omega t = \sin^{-1} \left(\frac{30}{100} \right)$$

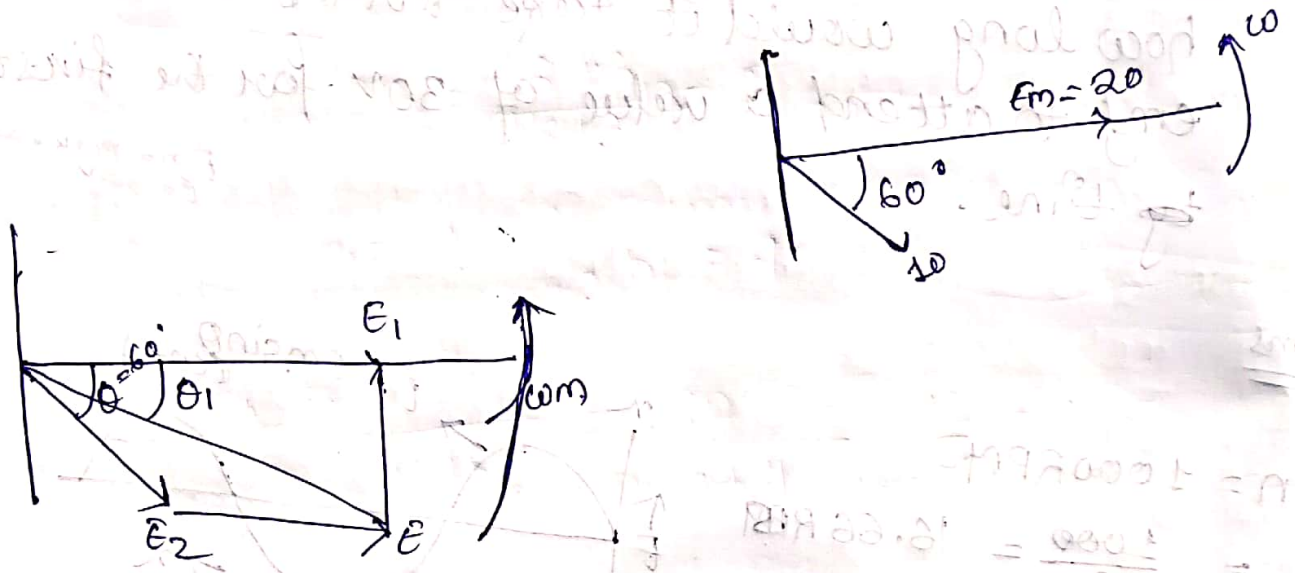
$$= 0.30 \text{ Rad}$$



$$\omega t = 0.30 \text{ Rad}$$

$$\Rightarrow t = \frac{0.30}{\omega} = \frac{0.30}{104.62} = 0.0028 \text{ sec.}$$

Q. Given the phasor representation for the sinusoidal emfs given by $E_1 = 20 \sin 314t$
 $E_2 = 10 \sin (314t - 60^\circ)$
 find the resultant of two phasors.



$$E_m = \sqrt{E_{m1}^2 + E_{m2}^2 + 2 E_{m1} E_{m2} \cos \theta}$$

$$= \sqrt{400 + 100 + 2 \cdot 20 \cdot 10 \times \cos 60^\circ}$$

0.34.

$$E_m = 26.45 \text{ V}$$

$$\phi_1 = \tan^{-1} \left[\frac{E_{m2} \sin \theta}{E_{m1} + E_{m2} \cos \theta} \right]$$

$$= \tan^{-1} \left[\frac{10 \times \sin 60}{20 + 10 \cos 60} \right]$$

$$= \tan^{-1} \left[\frac{10 \times \frac{\sqrt{3}}{2}}{20 + 10 \times \frac{1}{2}} \right]$$

$$= \tan^{-1} \frac{5\sqrt{3}}{25} = \tan^{-1} \frac{\sqrt{3}}{5}$$

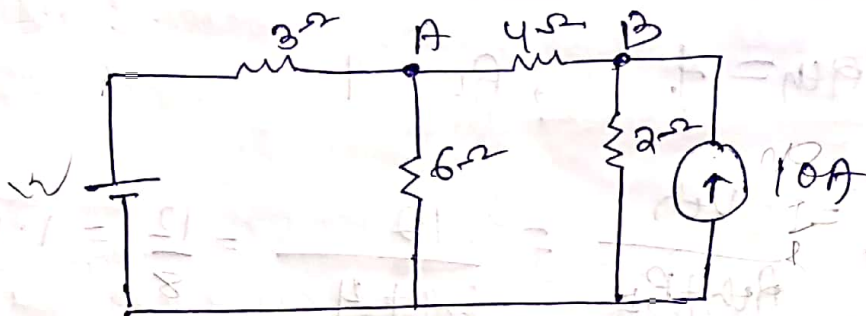
$$\phi_1 = 19.1^\circ$$

$$E = E_m \sin(\omega t - \theta)$$

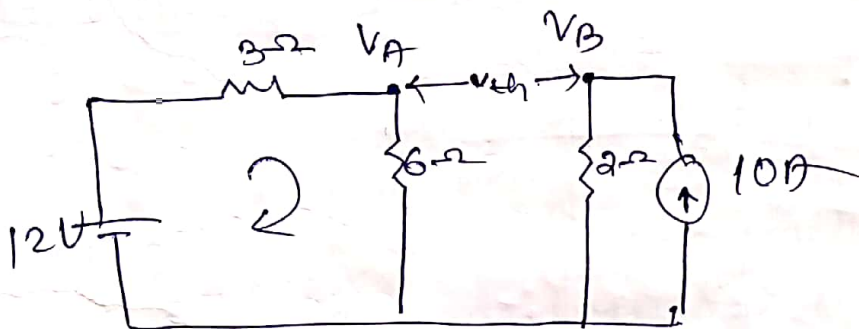
$$= 26.45 \cdot \sin(\omega t - 19.1^\circ)$$

$$= 26.45 \sin(314t - 19.1^\circ)$$

Q. using Thevenin's Theorem calculate the current flowing through the 4Ω resistor



step-1



$$12 - 3I_p - 6I_p = 0$$

$$\Rightarrow I = 12/6 = 1.33A$$

$$V_A = 1.33 \times 6 = 7.98V$$

$$V_B = 10 \times 2 = 20V$$

$$V_{th} = 20 - 8 = 12V (V_{BA})$$

1st step
Rth



$$R_{th} = \frac{6 \times 3}{6 + 3} + 2 = 4$$

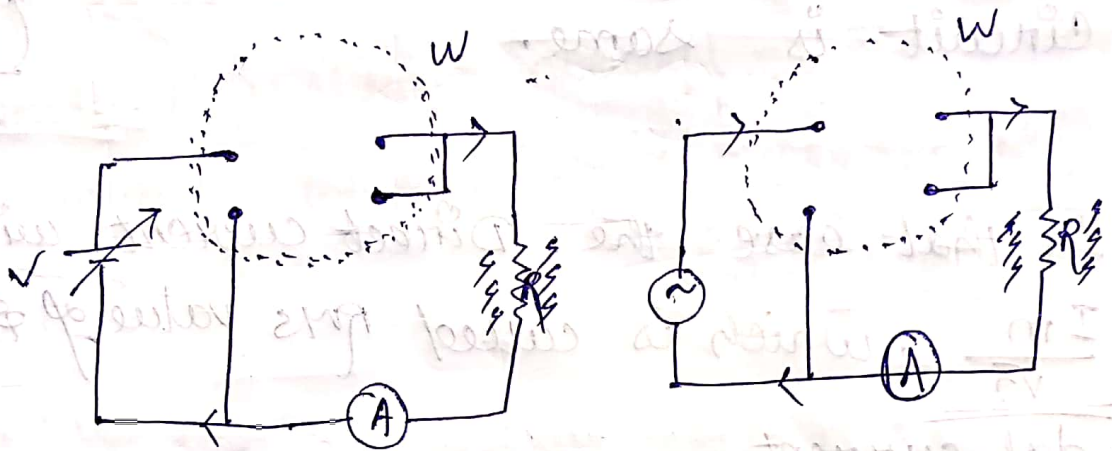
$$R_{th} = 4, \quad R_L = 4$$

$$I_L = \frac{V_{th}}{R_{th} + R_L} = \frac{12}{4 + 4} = \frac{12}{8} = 1.5$$

Dt. 13.09.19

Root Means Square Value: (RMS)

Defⁿ: The RMS value of an AC is given by that DC current which, when flowing through a given circuit for a given time produces the same heat as produced by the Alternating current (AC) when flowing through the same circuit for the same time.



It is also known as the effective or virtual value of AC. The former term being used more extensively for computing the RMS value of symmetrical sinusoidal AC. There are two methods for measuring RMS value: 1) Mid-ordinate Method, 2) Analytical method.

for symmetrical but non-sinusoidal waves. ~~The~~
(+ve, 1/2 cycle)
(-ve, 1/2 cycle)

* The mid-ordinate method would be found more convenient.

* A simple experimental arrangement for measuring the equivalent DC value of a sinusoidal current is shown in the figure above.

* The two circuits are similar Resistances but one is connected to a battery and other is connected to a sinusoidal generator.

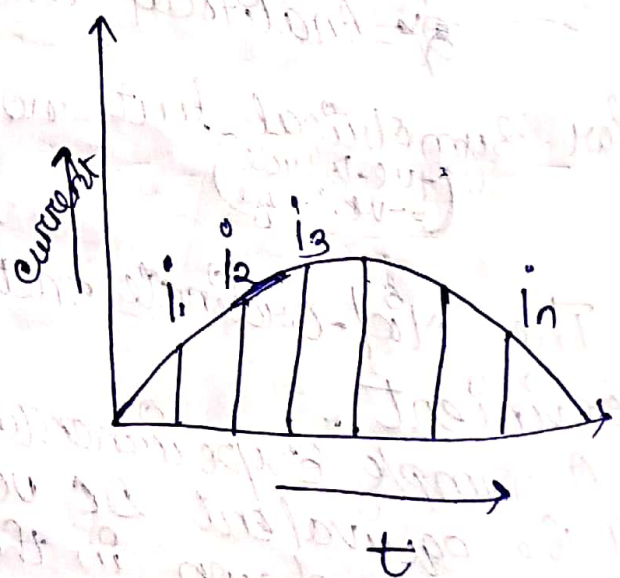
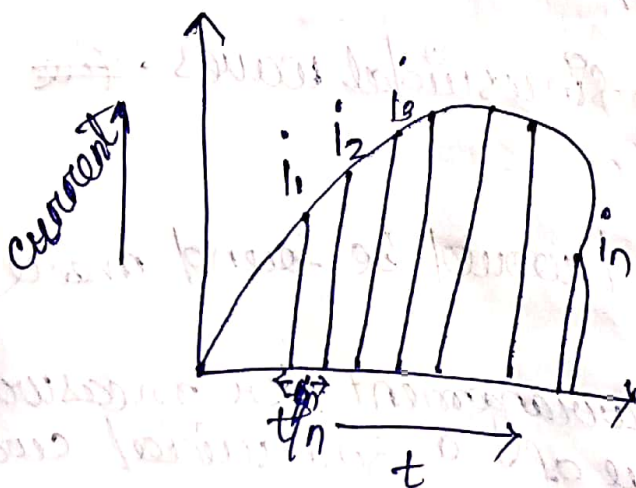
* Watt meters are used to measure the heat power in is circuit.

* The voltage applied to each circuit is so adjusted that heat power production of each circuit is same.

$$P = VI$$

* In that case the Direct current will be $\frac{I_m}{\sqrt{2}}$, which is called RMS value of sinusoidal current

1) Mid-ordinate Method :-



* The figure shows that the two half cycles for both symmetrical sinusoidal & non-sinusoidal alternating currents

* Dividing time base t into n equal intervals of time is duration of $\frac{t}{n}$ seconds

* Let the average values of instantaneous current during these intervals be respectively I_1, I_2, \dots, I_n .

Suppose that an alternating current is passed through the circuit of resistance $R \Omega$ then

$$\text{Heat produced in the first interval} = \underline{\underline{0.24 \times 10^{-3} I_1^2 \frac{RT}{n} \text{ kcal}}}$$

$$\text{Heat produced in the 2nd interval} = \underline{\underline{0.24 \times 10^{-3} I_2^2 \frac{RT}{n} \text{ kcal}}}$$

$$\text{Heat produced in the } n\text{th interval} = \underline{\underline{0.24 \times 10^{-3} I_n^2 \frac{RT}{n} \text{ kcal}}}$$

Total heat produced in t seconds

$$= \underline{\underline{0.24 \times 10^{-3} \times \frac{RT}{n} \left(\frac{I_1^2 + I_2^2 + \dots + I_n^2}{n} \right) \text{ kcal}}}$$

Now suppose that a DC of value I produces the same heat through the same resistance during the same time t , heat produced by it is equal to $\underline{\underline{0.24 \times 10^{-3} I^2 RT \text{ kcal}}}$:

By definition, the two amounts of heat produced should be equal

$$0.24 \times 10^{-3} I^2 RT \text{ kcal} = 0.24 \times 10^{-3} RT \left(\frac{I_1^2 + I_2^2 + \dots + I_n^2}{n} \right)$$

$$\Rightarrow I^2 = \left(\frac{I_1^2 + I_2^2 + \dots + I_n^2}{n} \right)$$

$$\Rightarrow I = \sqrt{\left(\frac{I_1^2 + I_2^2 + \dots + I_n^2}{n} \right)}$$

* Square Root of the, mean of the, squares of the instantaneous currents.

Similarly we have

$$V = \sqrt{\frac{V_1^2 + V_2^2 + \dots + V_n^2}{n}}$$

2) Analytical method

The standard form of a sinusoidal AC is equal to $I = I_m \sin \omega t$
 $= I_m \sin \theta$

The mean of the square of the instantaneous value of current over one complete cycle is -

$$\bar{I} = \frac{\int_0^{2\pi} I^2 d\theta}{2\pi - 0}$$

The square root is $\sqrt{\frac{\int_0^{2\pi} I^2 d\theta}{2\pi - 0}}$

$$\begin{aligned} \text{hence the RMS value is } I &= \left[\frac{\int_0^{2\pi} I_m^2 \sin^2 \theta}{2\pi} \right]^{1/2} \\ &= I_m \left[\frac{1}{2\pi} \int_0^{2\pi} \left(\frac{1 - \cos 2\theta}{2} \right) d\theta \right]^{1/2} \end{aligned}$$

$$= I_m \left[\frac{1}{4\pi} \left\{ (0)^{2\pi} - \left(\frac{\sin 2\theta}{2} \right) \right\} \right]^{1/2}$$

$$= I_m \left[\frac{1}{4\pi} \left\{ (2\pi - 0) - \frac{1}{2} (\sin 2\pi - \sin 0) \right\} \right]^{1/2}$$

$$= I_m \left[\frac{1}{4\pi} \times 2\pi \right]^{1/2}$$

$$= I_m \left[\frac{1}{2} \right]^{1/2} = \frac{I_m}{\sqrt{2}} = 0.707 I_m$$

* RMS value of current equals $= 0.707 \times$ max. value of current

Note:-

In Electrical Engineering circuit unless indicated otherwise, the values of the given current & voltage are always the RMS value.

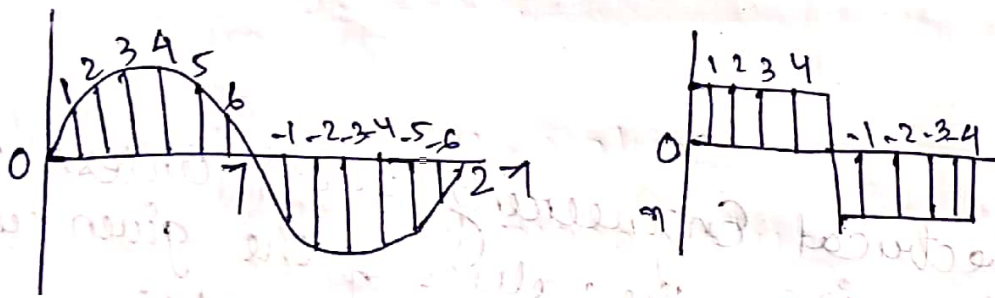
It should be noted that average heating effect produced during ~~half~~ one cycle is

$$I^2 R = \left(\frac{I_m}{\sqrt{2}} \right)^2 R = \frac{I_m^2}{2} \times R$$

Average value

The average value (I_A) of an AC is expressed by the steady state current which transports across any circuit the same charge in ~~the same time~~ as it transports by that AC during the same time.

In case of a symmetrical AC (that is one whose two half cycles are exactly similar, whether sinusoidal or non-sinusoidal), the average value over a complete cycle is zero.



Hence in this case the average value is obtained by adding ~~or~~ ~~of~~ integrating the instantaneous values of current over one half cycle only.

But in case of unsymmetrical AC the average value must ~~be~~ always be ^{taken} over the whole cycle.

Mid-ordinate Method :-

$$I_{avg} = \frac{(I_1 + I_2 + \dots + I_n)}{n}$$

Analytical method

The standard equation of an AC is

~~I_{avg}~~

$$I = I_m \sin \theta$$

$$I_{avg} = \int_0^{\pi} I_m \sin \theta \, d\theta$$

$$= \frac{I_m}{\pi} \int_0^{\pi} \sin \theta \, d\theta$$

$$= \frac{I_m}{\pi} [-\cos \theta]_0^{\pi}$$

$$= \frac{I_m}{\pi} [\cos \theta]_{\pi}^0$$

$$= \frac{I_m}{\pi} (\cos 0 - \cos \pi)$$

$$= \frac{I_m}{\pi} (1 + 1)$$

$$I_{avg} = \frac{2I_m}{\pi}$$

$$I_{avg} = 0.637 I_m$$

Note:

RMS value is always greater than the average value except in the case of rectangular wave when both are equal.

Oct. 17. 09. 19

FORM FACTOR

Form factor is defined as the ratio of RMS value & average value. for sinusoidal AC commonly.

$$\text{Form factor} = \frac{\text{RMS value}}{\text{Average value}}$$

$$= \frac{0.707 I_m}{0.637 I_m} = 1.11$$

$$\boxed{F.F = 1.11}$$

* Peak factor or crest factor or amplitude factor.

It is defined as the ratio between the maximum value & the RMS value.

$$\frac{I_m}{\frac{I_m}{\sqrt{2}}} = \sqrt{2} = 1.414$$

for AC sinusoidal wave only.

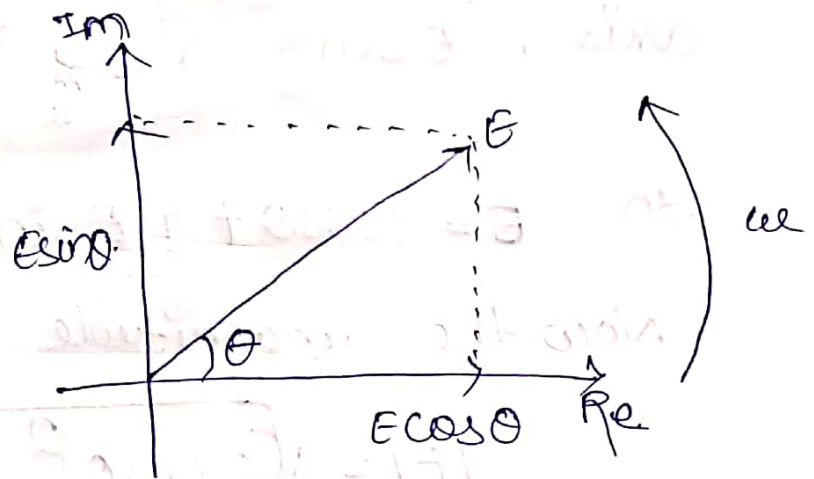
Complex Voltages & Currents

The concept of phasor notation and complex algebra is quite essential to understand complex voltages & currents in AC circuits.

The voltage and current phasors which exhibit variations in their magnitude & phase with respect to time are called complex voltage & current.

Complex voltages & currents can be represented graphically and mathematically for numerical application. Graphical representation involves two popular schemes known as complex representation & polar representation.

1) a + ib (Rectangular)
2) $b \angle \theta$ (Polar)



According to the complex algebra to orthogonal phasors can be represented simultaneously in one complex term which gives the resulting action of the two individual phasors one of them is called the Real part and other is called Imaginary

In a Cartesian coordinate system the x-axis is treated as real axis and y-axis is treated as Imaginary axis.

But in Electrical engineering Domain x-axis remaining the same as the real axis. y-axis is treated as the Imaginary axis which is shown in the above figure. Where the instantaneous phasor position of 'E' is characterized by two components " $E \cos \theta$ " along Real axis, $E \sin \theta$ along imaginary axis.

$$\text{So } E = E \cos \theta + j (E \sin \theta)$$

Now the magnitude of E will be

$$|E| = \sqrt{(E \cos \theta)^2 + (E \sin \theta)^2}$$

$$\theta = \tan^{-1} \left(\frac{E \sin \theta}{E \cos \theta} \right)$$

According to the complex algebra the value of 'j' operator is numerically equivalent to

$$\boxed{j = \sqrt{-1}}$$

This is quite useful to simplify the terms having higher powers of 'j' obtained from the multiplication of two or more complex quantities.

ADDITION OF TWO COMPLEX NO. BY 'J' OPERATOR.

$$(A + jB) + (C + jD)$$

$$= \boxed{(A + C) + j(B + D)}$$

SUBTRACTION OF TWO COMPLEX NO. BY 'J' OPERATOR.

$$(A + jB) - (C + jD)$$

$$= \boxed{(A - C) + j(B - D)}$$

MULTIPLICATION OF TWO COMPLEX NO. BY 'J' OPERATOR.

$$(A + jB)(C + jD)$$

$$= AC + jAD + jBC + j^2BD$$

$$= AC + jAD + jBC - BD$$

$$= \boxed{(AC - BD) + j(AD + BC)}$$

DIVISION OF TWO COMPLEX NO. BY 'J' OPERATOR.

$$\frac{A + jB}{C + jD}$$

$$= \frac{(A + jB)(C - jD)}{(C + jD)(C - jD)}$$

$$= \frac{AC - AjD + CjB - j^2BD}{c^2 - (jD)^2}$$

$$= \frac{AC - AjD + CjB + BD}{c^2 - (jD)^2}$$

$$= \frac{AC + BD + j(BC - AD)}{c^2 + D^2}$$

$$= \frac{(AC + BD) + j(BC - AD)}{c^2 + D^2}$$

$$= \frac{AC + BD}{c^2 + D^2} + j \frac{(BC - AD)}{c^2 + D^2}$$

Multiplication of two complex no. by polar operator.

$$(A \angle \alpha) \times (B \angle \beta) \\ = \boxed{(A \times B) \angle \alpha + \beta}$$

Division of two complex no. by polar operator.

$$\frac{A \angle \alpha}{B \angle \beta} \\ = \frac{A}{B} \angle \alpha - \beta$$

10/10/2024
5/10/2024

Q.1

Two complex quantities are represented as
 $A = 8 + j6$ and $B = 3 + j4$ calculate
their sum, difference, product & division.

Ans

$$A = 8 + j6 \\ B = 3 + j4$$

$$\text{Addition } A+B = (8+j6) + (3+j4) \\ = 11 + j10$$

$$\text{Difference } A-B = (8+j6) - (3+j4) \\ = 5 - j2$$

Product $AB = (8 + j56)(3 + j4)$

$$= (24 - 224) + j(32 + 18)$$

$$= 0 + j50$$

Division $A/B = \frac{8 + j56}{3 + j4}$

$$= \frac{24 + 24}{9 + 16} + j \frac{18 - 32}{9 + 16}$$

$$= \frac{48}{25} + j \frac{-14}{25}$$

$$= \frac{48}{25} - j 0.56$$

$$= 1.92 - j 0.56$$

St. 19.09.19

AC Through Resistance & Inductance.

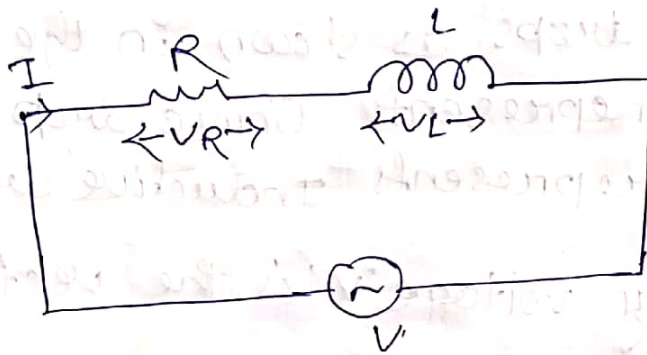
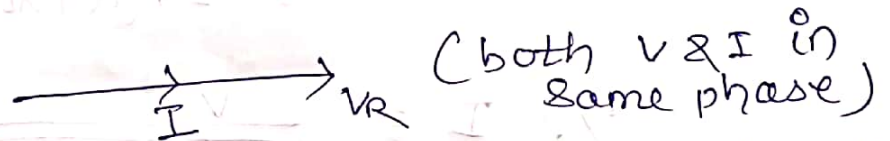


fig.(a)

let V is the RMS value of the applied voltage
 I is the RMS value of the Resultant current

$V_R = IR =$ voltage drop across 'R' (In phase with I)



$V_L = IX_L =$ voltage drop across the coil
(Ahead 90° to the current)

$X_L =$ Inductive Reactants
value = $2\pi fL$

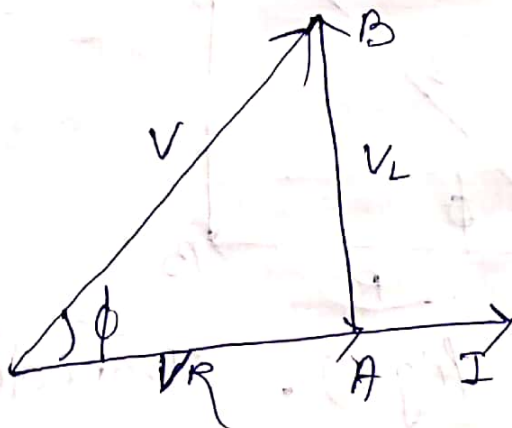


fig.(b)

These voltage drops as shown in the triangle OAB, \vec{OA} represents Ohmic drop (resistive drop) (VR) and \vec{AB} represents Inductive drop (VL) .

The apply voltage 'V' is the vector sum of these two.

$$V = \sqrt{VR^2 + VL^2}$$

$$= \sqrt{(IR)^2 + (IX_L)^2}$$

$$= I \sqrt{R^2 + X_L^2}$$

$$I = \frac{V}{\sqrt{R^2 + X_L^2}}$$

The quantity $\sqrt{R^2 + X_L^2}$ is known as Impedance. Unit is also " Ω ".

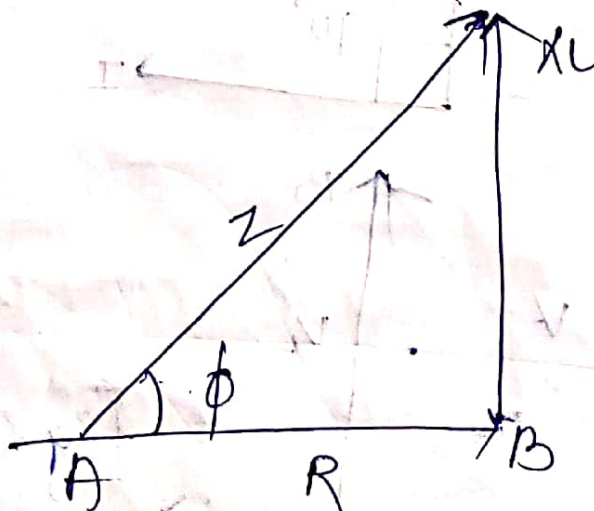


fig (c). Impedance triangle

as seen in the impedance triangle ABC

$$Z^2 = R^2 + X_L^2$$

$$\Rightarrow (\text{Impedance})^2 = (\text{Resistance})^2 + (\text{Reactance})^2$$

from the figure (b). It is clear that the applied voltage 'v' leads the current 'I' by an angle ϕ .

$$\phi \text{ such that } \tan \phi = \frac{V_L}{V_R}$$

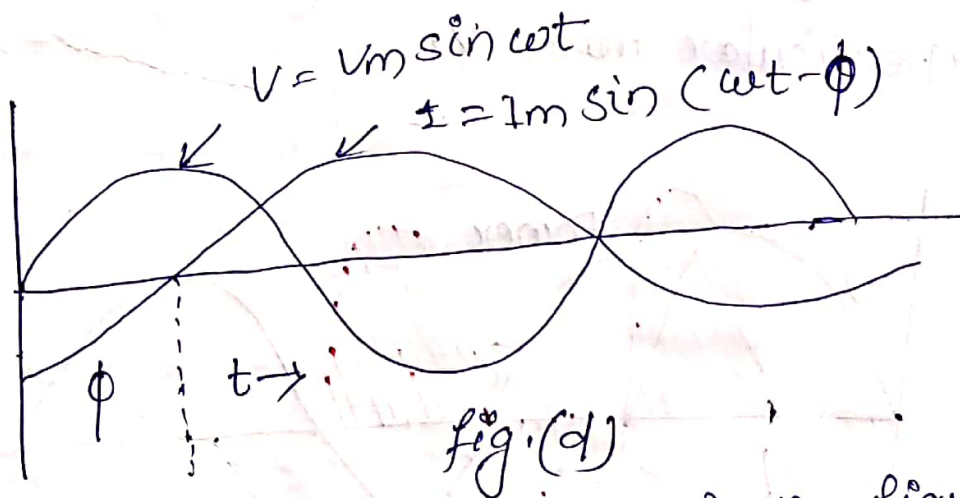
$$= \frac{I X_L}{I R}$$

$$\omega = 2\pi f$$

$$\tan \phi = \frac{X_L}{R}$$

$$= \frac{2\pi f L}{R}$$

$$\tan \phi = \frac{\omega L}{R}$$



Thus the same fact is also given in the figure (d)

In other words current I lags behind the applied voltage by an angle ϕ , hence if applied voltage is given by $V = V_m \sin \omega t$ then the current equation is $I = I_m \sin(\omega t - \phi)$.

where $I_m = \frac{V_m}{Z}$

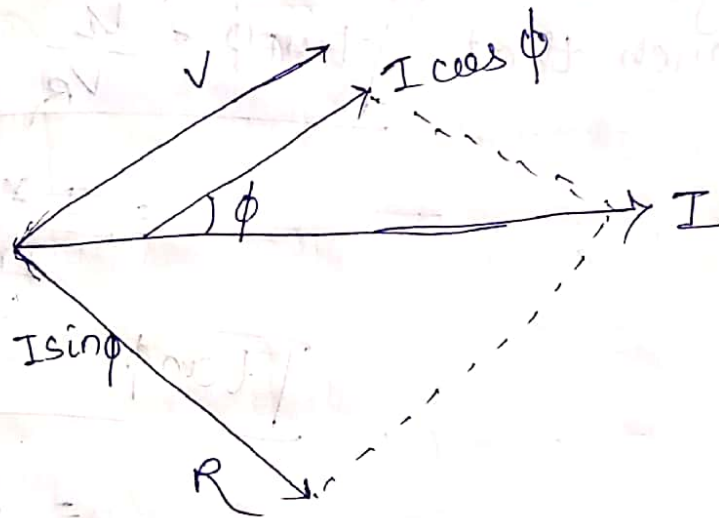
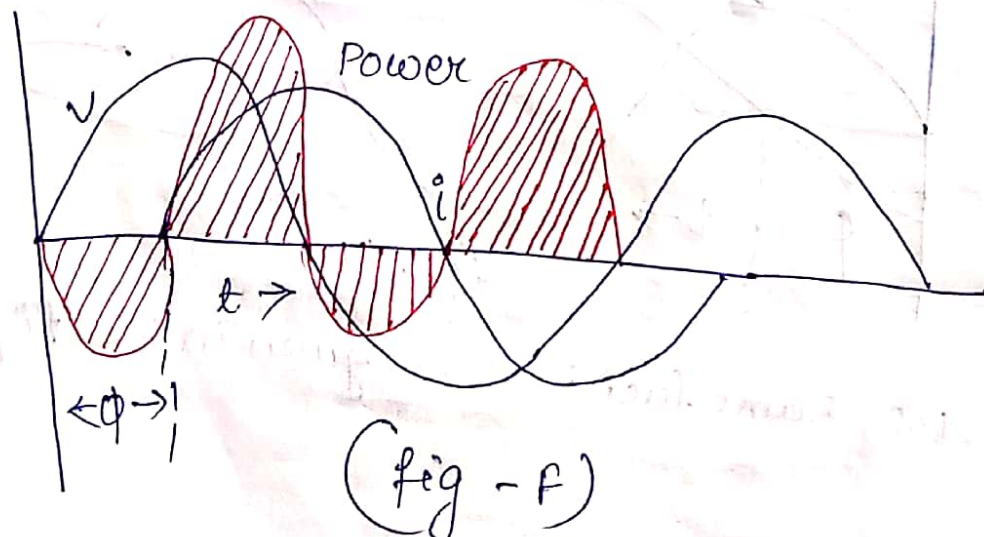


fig (e)

In the above figure I has been result into two mutually perpendicular components $I \cos \phi$ along the applied voltage V and $I \sin \phi$ is perpendicular with V .



(fig - f)

The mean power consumed by the circuit is given by the product of V and the component of the current I which is phase in with V . ϕ $[P = VI \cos \phi]$ = (RMS voltage) (RMS current) (power factor)

Note:

* In an AC circuit the product of RMS voltage and RMS current gives volt ampere (VA) and not true power in watt. So here

* So true power $[W = VA \times \cos \phi]$

* It should be noted that power consumed is due to Ohmic resistance only because pure inductance does not consume any power

Now $P = VI \cos \phi$

$= VI \times \frac{R}{Z}$

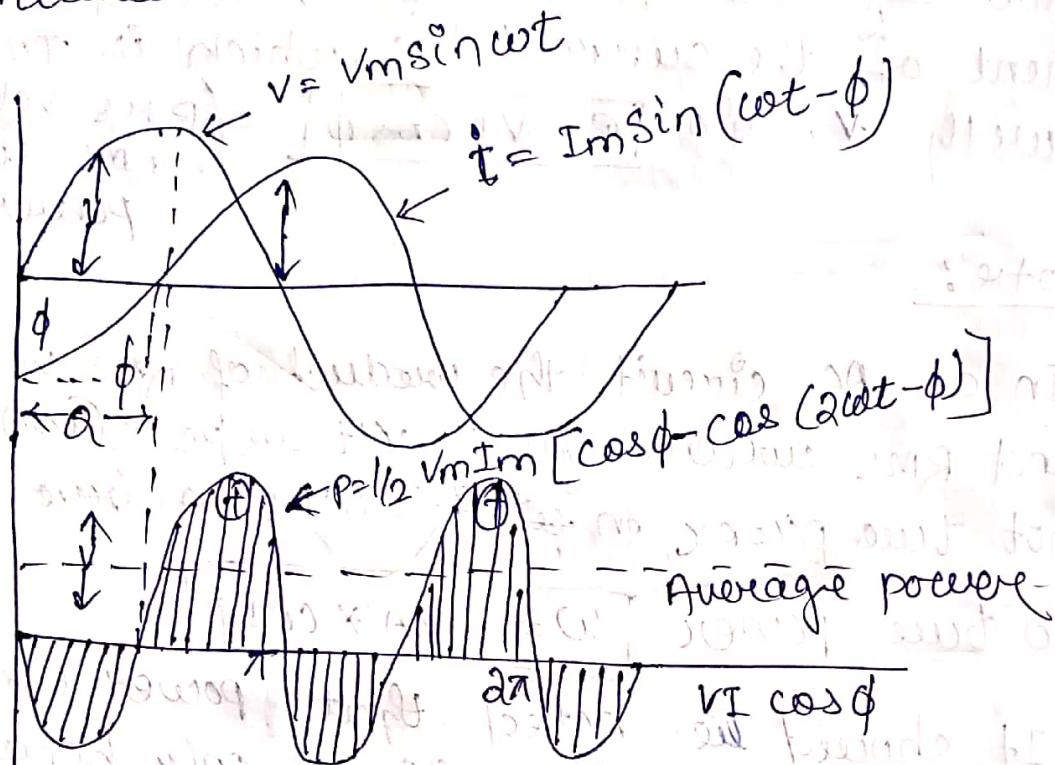
$V = IZ$

$= \frac{V}{Z} IR$

$= \frac{IZ}{Z} IR$

$[P = I^2 R \text{ watt}]$

Let us calculate power in terms of instantaneous value.



(fig - 9)

Instantaneous power is
$$\begin{aligned}
 v i &= V_m \sin \omega t \times I_m \sin(\omega t - \phi) \\
 &= V_m I_m \sin \omega t \cdot \sin(\omega t - \phi) \\
 &= \frac{1}{2} V_m I_m \cdot 2 \sin \omega t \cdot \sin(\omega t - \phi) \\
 &= \frac{1}{2} V_m I_m [\cos(\omega t + \omega t - \phi) - \cos(\omega t - \omega t + \phi)] \\
 &= \frac{1}{2} V_m I_m [\cos(2\omega t - \phi) - \cos \phi]
 \end{aligned}$$

[∵ $\cos(A+B) - \cos(A-B)$

$$\begin{aligned}
 &= \cos A \cdot \cos B - \sin A \cdot \sin B - \{ \cos A \cdot \cos B + \sin A \cdot \sin B \} \\
 &= \cos A \cdot \cos B - \sin A \cdot \sin B - \cos A \cdot \cos B - \sin A \cdot \sin B \\
 &= -2 \sin A \cdot \sin B] \\
 &= \frac{1}{2} V_m I_m [\cos \phi - \cos(2\omega t - \phi)]
 \end{aligned}$$

Obviously this power consists of two parts.
i) a constant part $\frac{1}{2} V_m I_m \cos \phi$ which contributes to real power.

ii) a pulsating component $\frac{1}{2} V_m I_m \cos(2\omega t - \phi)$

which has a frequency twice that of the voltage & current. It does not contribute to actual power since its average value over a complete cycle is zero.

Hence, average power consumed,

$$= \frac{1}{2} V_m I_m \cos \phi$$

$$= \frac{V_m}{\sqrt{2}} \times \frac{I_m}{\sqrt{2}} \cos \phi$$

$$= VI \cos \phi$$

where V & I represents the R.M.S. value.

Symbolic Notation

$$Z = R + jX_L$$

Impedance vector has numerical value of

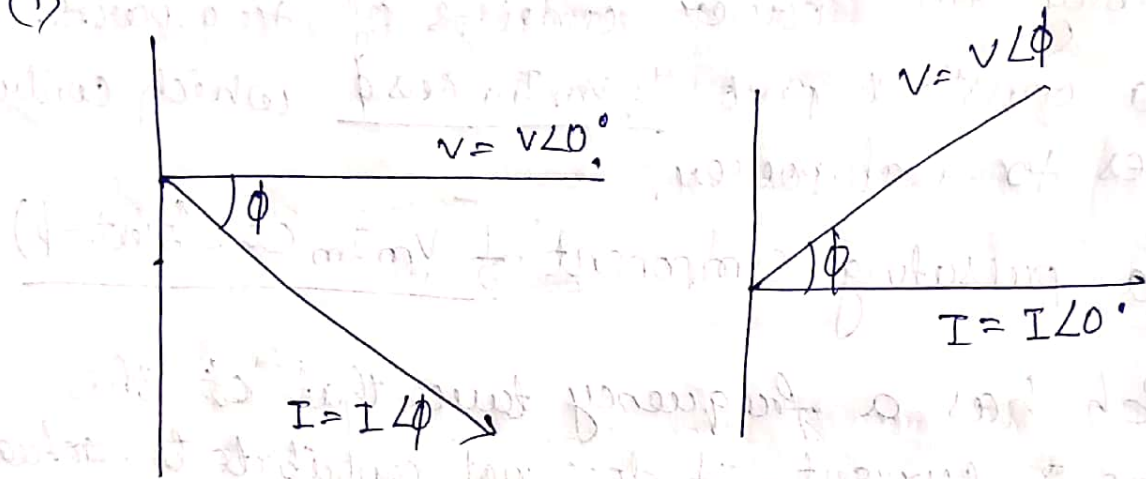
$$Z = \sqrt{R^2 + X_L^2}$$

$$\phi = \tan^{-1}\left(\frac{X_L}{R}\right)$$

It may also be expressed in the polar form

as $Z = Z \angle \phi^\circ$

(i)



Assuming $v = V\angle 0^\circ$

$$I = \frac{V}{Z} = \frac{V\angle 0^\circ}{Z\angle \phi^\circ} = \frac{V}{Z} \angle -\phi^\circ$$

It shows that current vector is lagging behind the voltage vector by ϕ° . The numerical value of current is $\frac{V}{Z}$

(ii) However we assumed that

$$I = I\angle 0^\circ \text{ then}$$

$$V = IZ = I\angle 0^\circ \times Z\angle \phi^\circ$$

$$V = IZ\angle \phi^\circ$$

It shows that voltage vector is ahead of current vector

Power factor

It may be defined as

(i) cosine of angle of lead or lag.

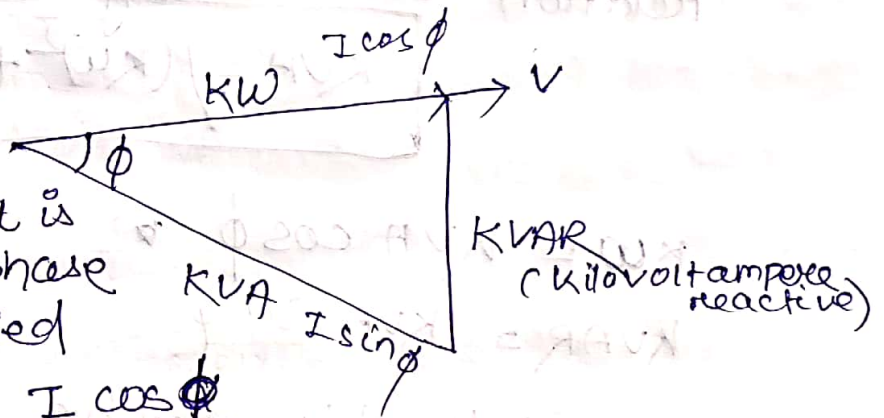
(ii) The Ratio = $\frac{R}{Z} = \frac{\text{Resistance}}{\text{Impedance}}$ (from fig-c)

(ii) The ratio $\frac{\text{True power}}{\text{apparent power}}$

$$= \frac{\text{Watts}}{\text{volt amperes}}$$
$$= \frac{W}{VA}$$

Dt. 20.9.19

Active & Reactive components of circuit current I.



Active component is that which is in phase with the applied voltage V is, $I \cos \phi$

It is also known as wattful component

Reactive component is that which is quadrature with V , that is, $I \sin \phi$, It is also known as wattless component.

It should be noted that product of volt & ampere in an AC circuit gives VA. Out of

this the actual power is $VA \cos \phi$ is equal to W and reactive power is $VA \sin \phi$

Expressing the values in KVA we find that it has two rectangular component.

a) Active component which is obtained by multiplying KVA by $\cos \phi$ and this gives the power in KW.

b) The reactive component known as reactive KVA and is obtained by multiplying KVA by $\sin \phi$, is written as KVAR. The following relation can be easily deduced ~~KVA = KW + KVAR~~

$$KVA = \sqrt{(KW)^2 + (KVAR)^2}$$

$$KW = KVA \cos \phi$$

$$KVAR = KVA \sin \phi$$

The relationship can be easily understood by the resolving the KVA triangle in the figure above.

where it should be noted that lagging KVAR has been taken as negative.

Exp

Suppose a circuit draws a current I ampere which is equal to $1000A$ and a voltage of $20,000V$ & has a power factor of 0.8 . then, your input will be

$$P = VI$$

$$= 1000 \times \frac{20,000 \times 10^3}{1000}$$

$$= 20,000 \text{ KVA}$$

$$P.f. = 0.8$$

$$\cos \phi = 0.8$$

$$\cos^2 \phi + \sin^2 \phi = 1$$

$$\Rightarrow \sin^2 \phi = 1 - \cos^2 \phi$$

$$\Rightarrow \sin \phi = \sqrt{1 - \cos^2 \phi}$$

$$= \sqrt{1 - 0.8^2}$$

$$= 0.6$$

$$KW = 20,000 \times 0.8$$
$$= 16,000$$

$$KVAR = 20,000 \times 0.6$$
$$= 12,000$$

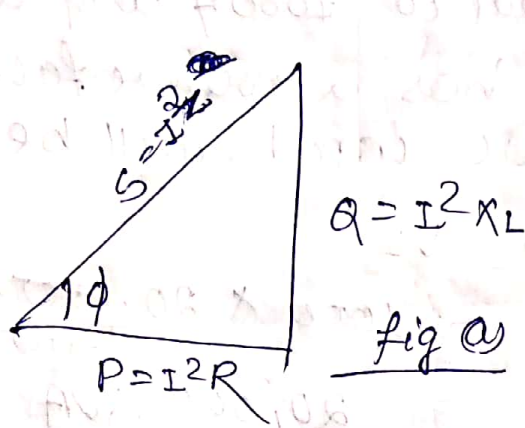
now

$$KVA = \sqrt{(KW)^2 + (KVAR)^2}$$

$$= \sqrt{(16,000)^2 + (12,000)^2}$$

$$= 20,000$$

Active / Reactive & Apparent power



$$R^2 + X_L^2 = Z^2$$

Let ^{an} a series arrange circuit draw a current 'I' when an alternating voltage value 'V' is applied to it. Suppose that current lags behind the applied voltage by ϕ then ^{three} powers drawn by the circuit as under

A. Apparant Power (S) :

It is given by the product of RMS value of the applied voltage and circuit current

So $S = VI$

$$= (IZ)I$$

$$= I^2Z \text{ (VA' unit)}$$

in DC $V = IR$
AC $V = IZ$

B. Active Power : (P or W) :

It is the power which is actually dissipated in the circuit resistance

$$\text{so, } P = I^2 R$$

$$= VI \cos \phi \text{ watt}$$

c- Reactive Power (Q).

It is the power developed in the inductive reactants of this circuit

$$Q = I^2 X_L$$

$$= I^2 Z \sin \phi$$

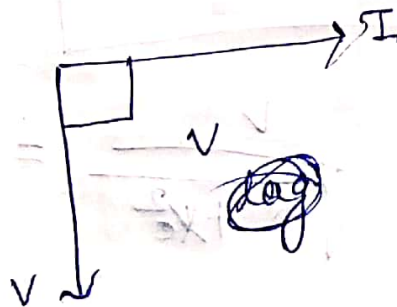
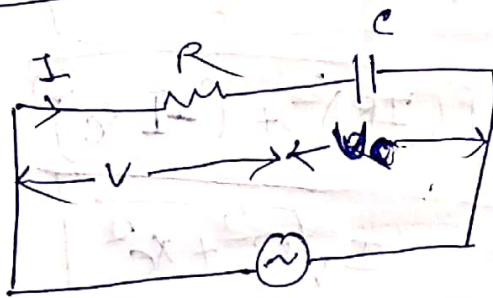
$$= I^2 Z \sin \phi$$

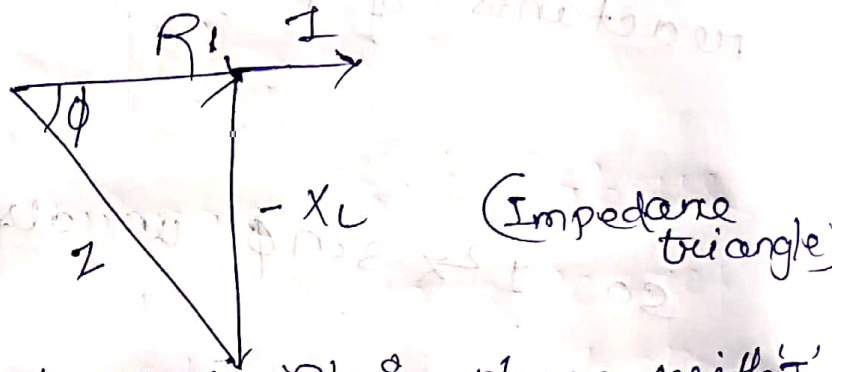
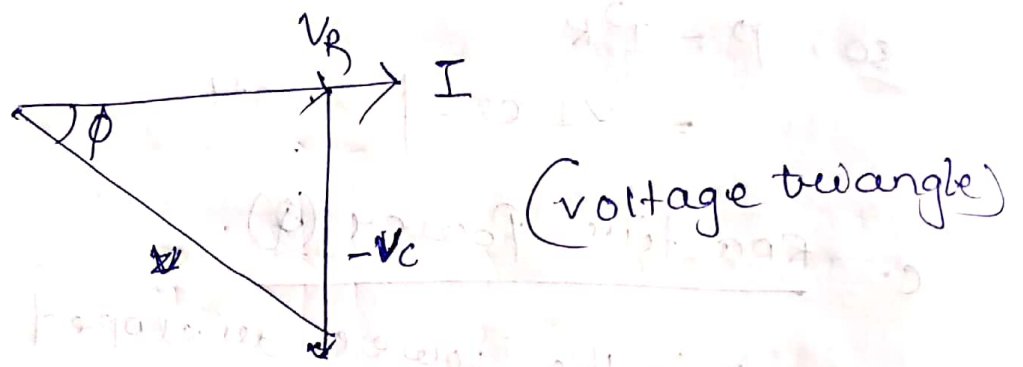
so $I^2 Z \sin \phi$ we also called $VI \sin \phi$ KVAR

These three powers as shown in the power triangle fig (a), where $S^2 = P^2 + Q^2$

$$\Rightarrow S = \sqrt{P^2 + Q^2}$$

AC through Resistance & capacitance





Here $V_R = IR$, drop across R in phase with I .

$V_C = IX_C$, drop across the capacitor, lagging I by 90° as C .

As capacitive reactance X_C is taken negative V_C is shown along negative direction of y -axis.

$$V = \sqrt{V_R^2 + (-V_C)^2}$$

$$V = \sqrt{(IR)^2 + (-IX_C)^2}$$

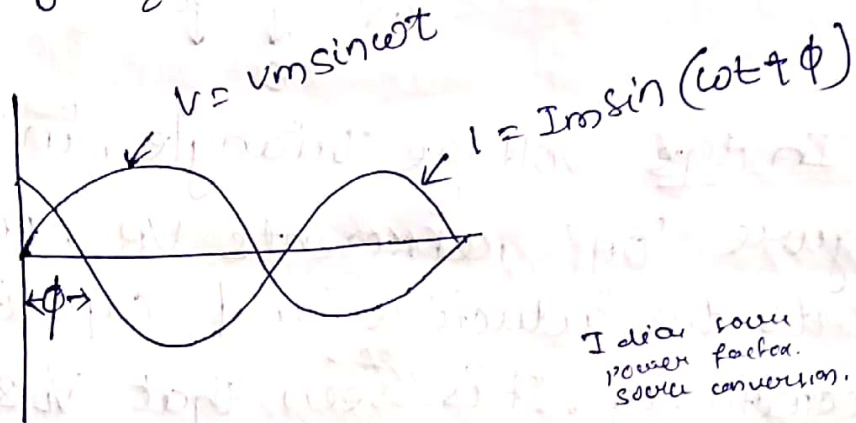
$$V = I\sqrt{R^2 + X_C^2}$$

$$I = \frac{V}{\sqrt{R^2 + X_C^2}} = \frac{V}{Z}$$

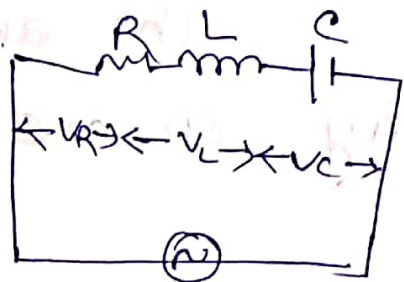
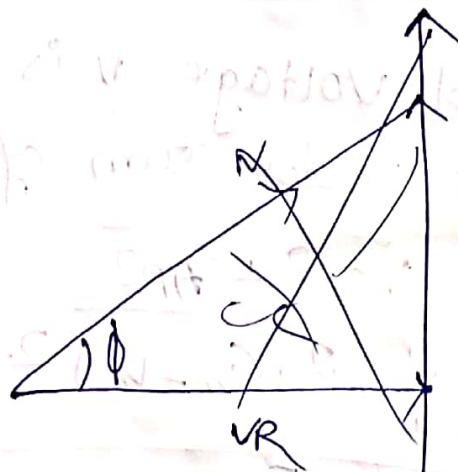
$X_L = 2\pi fL$	Inductive Reactance
$X_C = \frac{1}{2\pi fC}$	

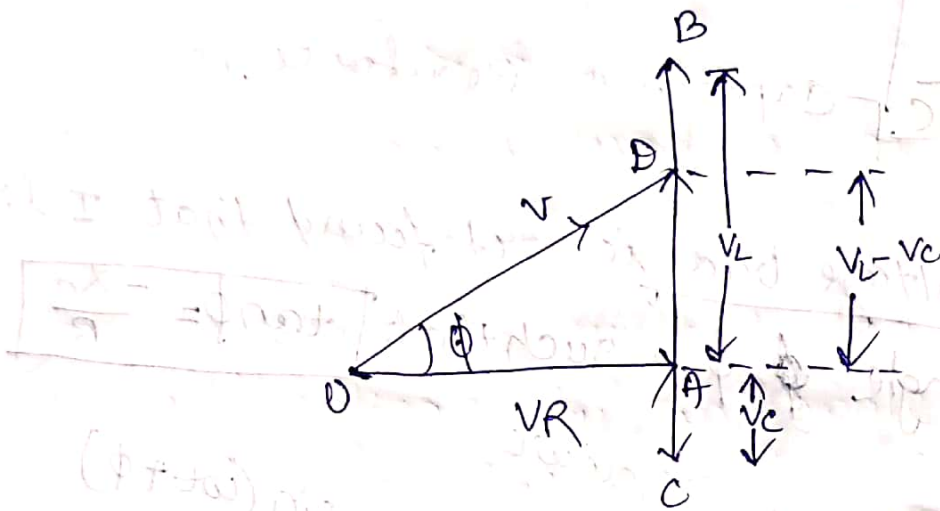
Capacitive Reactance

From fig. voltage triangle it found that I leads v by an angle ϕ , such that $\tan \phi = \frac{-X_C}{R}$



Resistance, Inductance & Capacitance in series (RLC series circuit)





In the voltage triangle, in the above figure 'OA' represents V_R , AB & AC represents the inductive and capacitive drops respectively. It is seen that V_L & V_C are 180° out of phase with each other i.e. they are in direct opposition to each other.

Subtracting $BD = AC$ from AB , we get net reactive drop $AD = I(X_L - X_C)$.

The applied voltage V is represented by OB and the vector sum of OA & AD

$$\begin{aligned}
 OP &= \sqrt{OA^2 + AD^2} \\
 \Rightarrow V &= \sqrt{V_R^2 + (V_L - V_C)^2} \\
 &= \sqrt{(IR)^2 + (IX_L - IX_C)^2} \\
 &= I \sqrt{R^2 + (X_L - X_C)^2}
 \end{aligned}$$

$$\Rightarrow I = \frac{V}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$\Rightarrow I = \frac{V}{\sqrt{R^2 + X^2}} = \frac{V}{Z}$$

The term $\sqrt{R^2 + (X_L - X_C)^2}$ is known as the impedance of the circuit.

$$(\text{Impedance})^2 = (\text{Resistance})^2 + (\text{net Reactance})^2$$

$$\Rightarrow Z^2 = R^2 + (X_L - X_C)^2$$

$$\Rightarrow Z^2 = R^2 + X^2$$

where X is the net reactance

$$\tan \phi = \frac{(X_L - X_C)}{R} = \frac{X}{R}$$

$$\text{Power factor} = \cos \phi = \frac{R}{Z}$$

$$= \frac{R}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$= \frac{R}{\sqrt{R^2 + X^2}}$$

$$= \frac{R}{\sqrt{R^2 + X^2}}$$

Hence in the RLC circuit:

$$V = V_m \sin \omega t$$

$$I = I_m \sin(\omega t \pm \phi)$$

The (+ve) sign is used when current leads
i.e. $X_c > X_L$.

The -ve sign is used when current lags
i.e. $X_L > X_c$

In general the current lag or lead, the
supplied voltage by an angle ϕ
such that $\tan \phi = \frac{X}{R}$.

24.09.2019

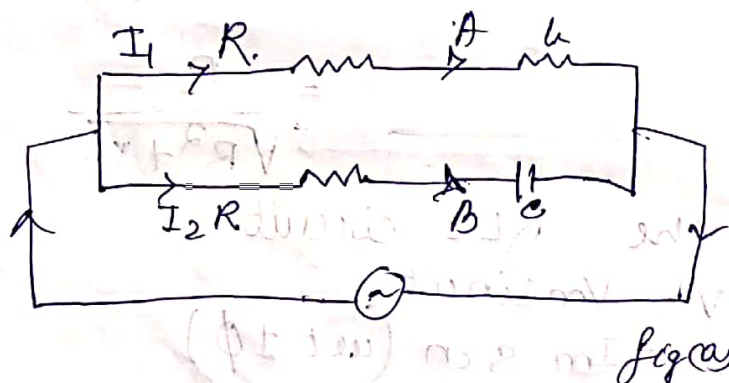
Parallel RMS circuit:-

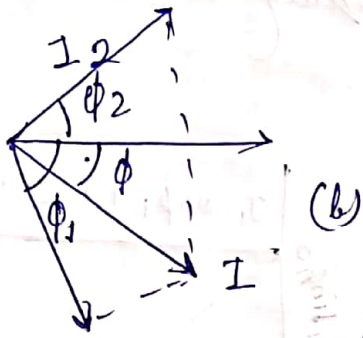
solving parallel circuit:-

when impedance are joined in parallel there are
three methods are available.

- a) Vector or phasor method
- b) Admittance method.
- c) Vector algebra.

a) Vector or phasor method:





for branch A $Z_1 = \sqrt{R_1^2 + X_1^2}$
 $I_1 = \frac{V_1}{Z_1}$

$$\cos \phi = \frac{R_1}{Z_1}$$

$$\phi = \cos^{-1} \left(\frac{R_1}{Z_1} \right)$$

Here current I_1 lags behind the applied voltage by an angle ϕ_1 which is shown in the fig (b)

→ for branch B $Z_2 = \sqrt{R_2^2 + X_2^2}$

$$I_2 = \frac{V_1}{Z_2}$$

$$\cos \phi_2 = \frac{R_2}{Z_2}$$

$$\Rightarrow \phi_2 = \cos^{-1} \frac{R_2}{Z_2}$$

Here current I_2 leads the voltage V by an angle ϕ_2 which is shown in the fig (b)

b) Resultant current:

The resultant current 'I' is the vector sum of the branch I_1 and I_2 and can be found by using parallelo gram law of vectors.

part 2' is preferred as it is quick and convenient.

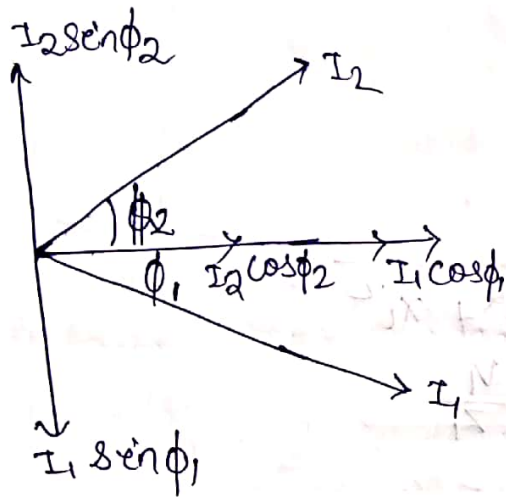


fig (a)

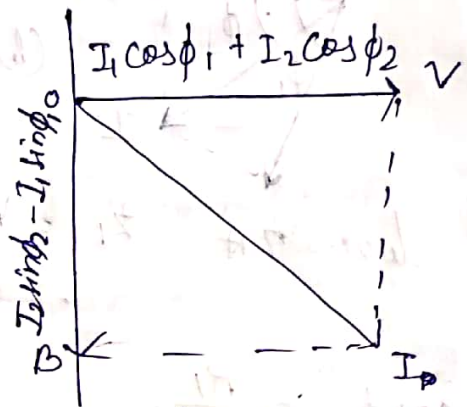


fig (b)

From fig (a) some of the active component of I_1 and I_2 is equal to $I_1 \cos \phi_1 + I_2 \cos \phi_2$.

Some of the reactive component of I_1 and I_2 is equal to $I_2 \sin \phi_2 - I_1 \sin \phi_1$.

If 'I' is the resultant current and ϕ its phase then its active and reactive component must be equal to these x and y component respectively as shown in the fig (b).

$$I \cos \phi = I_1 \cos \phi_1 + I_2 \cos \phi_2 \quad \text{active component}$$

$$I \sin \phi = I_2 \sin \phi_2 - I_1 \sin \phi_1 \quad \text{reactive component}$$

$$\text{Now resultant current } I = \sqrt{(I_1 \cos \phi_1 + I_2 \cos \phi_2)^2 + (I_2 \sin \phi_2 - I_1 \sin \phi_1)^2}$$

$$\text{Then } \sin \phi = \frac{I_2 \sin \phi_2 - I_1 \sin \phi_1}{I_1 \cos \phi_1 + I_2 \cos \phi_2}$$

If $\tan \phi$ is positive then current leads it
 -ve then current lags to the applied voltage (V)

power factor for the whole circuit given by

$$\cos \phi = \frac{I_1 \cos \phi_1 + I_2 \cos \phi_2}{I}$$

Admittance Method (Y)

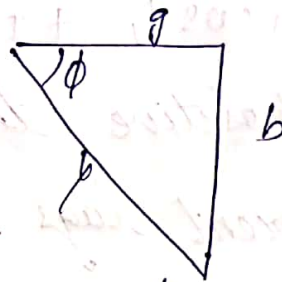
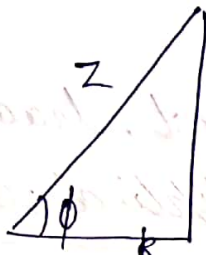
Admittance of a circuit is defined as the reciprocal of its impedance $\boxed{Y = \frac{1}{Z}}$

it is also called $\boxed{Y = \frac{I}{V}}$

$$\text{or } Y = \frac{\text{RMS current}}{\text{RMS Voltage}}$$

* Its unit is Siemens (ohm)

As impedance (Z) of a circuit has two components X & R which is shown in the figure A below
 Similarly admittance (Y) has also two components which is the figure shown in the below,



g is your conductance, b is your susceptance

$$\text{conductance } \boxed{g = y \cos \phi}$$

$$\boxed{\cos \phi = \frac{g}{y}}$$

In place $y = \frac{1}{Z} \times \frac{R}{Z}$

$$\boxed{\Rightarrow y = \frac{R}{Z^2}}$$

$$\boxed{g = \frac{R}{R^2 + X^2}}$$

$$Z = \sqrt{R^2 + X^2}$$

$$\Rightarrow Z^2 = R^2 + X^2$$

Similarly $b = y \sin \phi$

$$\sin \phi = \frac{b}{y}$$

$$\Rightarrow b = \frac{1}{Z} \times \frac{X}{Z}$$

$$\boxed{\Rightarrow b = \frac{X}{Z^2}}$$

$$b = \frac{x}{R^2 + x^2}$$

the admittance $Y = \sqrt{g^2 + b^2}$

* The unit of g, b, Y are ohms^{-1}

We will regard the capacitive reactance as positive and inductive reactance as -ve.

- The End -

Module-2

Dt. 17.10.19

3- ϕ AC circuits:

3- ϕ system:

The measure component of a three 3- ϕ AC system are 3- ϕ AC sources and 3- ϕ load device. A 3- ϕ AC source may be thought of as a combination of three 1- ϕ AC sources of same magnitude and frequency having mutual phase difference of

120° electrical degrees from each other. When in electrical Engineering we often encounter the term electrical degree when rotating machines are consult.

The Relation between mechanical degree & electrical degree is that.

$$\textcircled{*} \left[\text{one mechanical degree} = \frac{P}{2} \text{ electrical degree} \right]$$

where p is the number of magnetic poles present in the rotating machine.

Difference Between 1- ϕ AC system & 3- ϕ AC system

1- ϕ AC system

• It is not so balanced, and efficient in comparison to 3- ϕ AC system.

• 1- ϕ systems operate at one voltage level that is called phase voltage.

• The output and efficiency of a 1- ϕ machine is less than that of a single phase 3- ϕ machine for a given size of frame.

• 1- ϕ AC motors produce pulsating ~~torque~~ torque.

3- ϕ AC system

• Three phase systems are more balanced, efficient and robust in comparison to 1- ϕ system.

• 3- ϕ system having star connection possesses two operating voltage levels called line voltage & phase voltage.

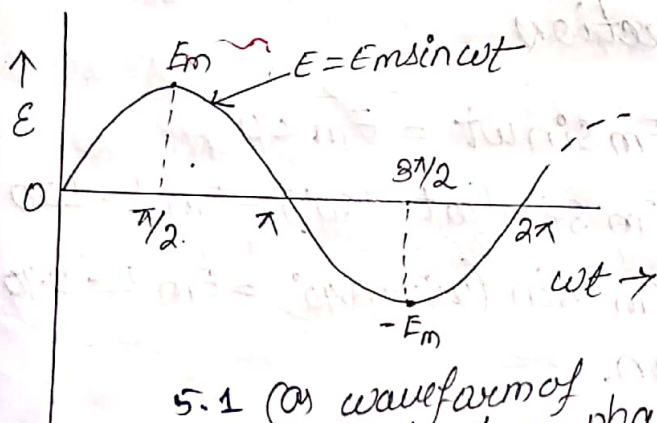
• The output and efficiency of a 3- ϕ machine is greater than that of single phase machine for a given size of frame.

• 3- ϕ AC motors can produce uniform ~~torque~~ torque.

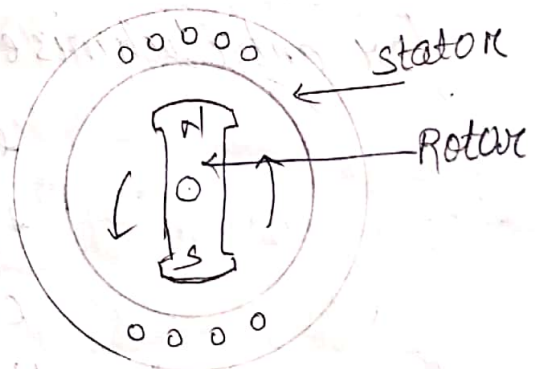
3- ϕ Emf Generation:

* A device used for generation of 3- ϕ emf is called a 3- ϕ AC Generator or simply it is called alternator.

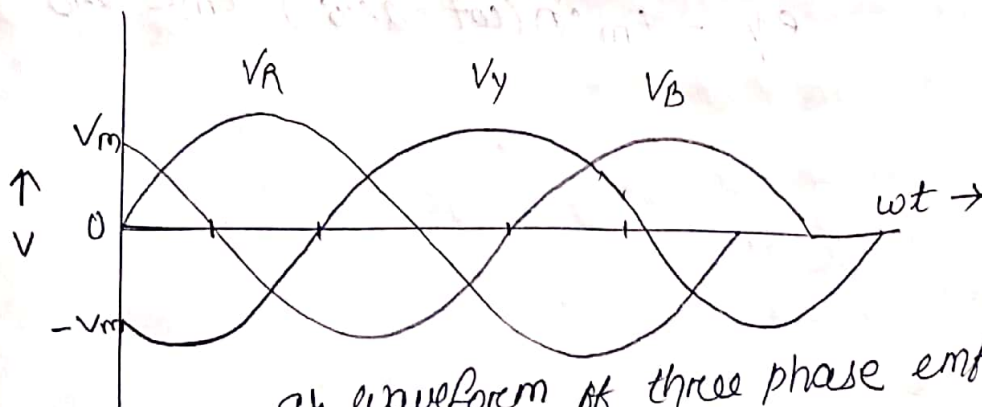
The principle of 3- ϕ emf generation is similar to 1- ϕ emf generation which we have already discussed. However there exist some constructional differences before proceeding, let us first focus our attention to the requirement of each case which is indicated in the figure below.



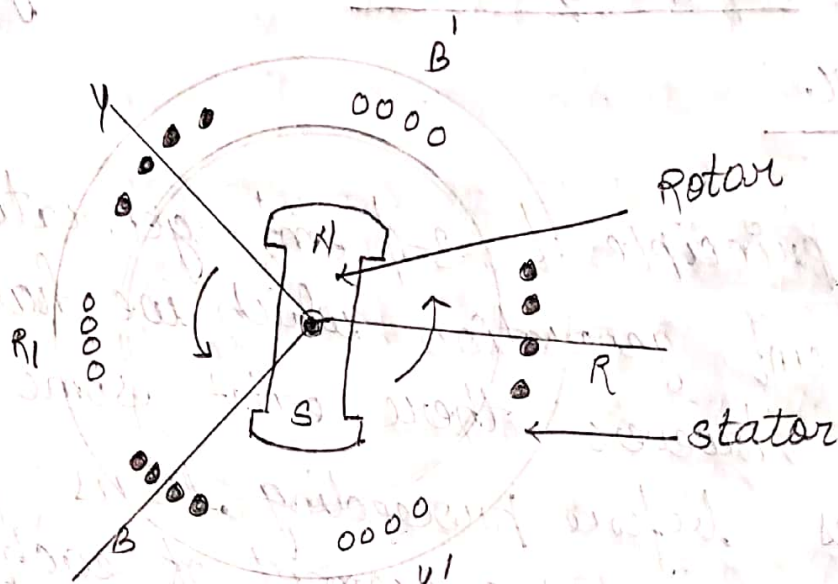
5.1 (a) waveform of single phase emf



(b) physical arrangement



5.2 (a) waveform of three phase emf



(b) Physical arrangement.

or waveform

for anticlockwise direction

$$e_R = E_m \sin \omega t = E_m \angle 0^\circ$$

$$e_Y = E_m \sin(\omega t - 120^\circ) = E_m \angle -120^\circ$$

$$e_B = E_m \sin(\omega t - 240^\circ) = E_m \angle -240^\circ$$

for clockwise direction.

$$e_R = E_m \sin \omega t = E_m \angle 0^\circ$$

$$e_B = E_m \sin(\omega t - 120^\circ) = E_m \angle -120^\circ$$

$$e_Y = E_m \sin(\omega t - 240^\circ) = E_m \angle -240^\circ$$

A device used for generation of 3- ϕ emf generation is called a 3- ϕ ac generator or simply an alternator. The principle of 3- ϕ emf generation is similar to that of single phase emf generation, which is already explained. However, there exist some constructional difference. Before proceeding any further, let us first focus our attention on the requirement for each case and indicated in the figure.

fig 5.1(a) illustrates a sinusoid that represents the instantaneous emf induced in one coil due to rotary motion of a magnetic field as per arrangements shown in figure 5.1(b) on the other hand fig 5.2(a) illustrates three sinusoids having a mutual phase shift of 120 degrees between one another, thus representing the 3- ϕ instantaneous emf that may be induced in three separate coils (R, Y, and B) having cyclic arrangement along the periphery of a circle subject to the rotary motion of a magnetic field as shown in figure 5.2(b).

In a practical 3- ϕ alternator, the external frame supports the three phase balanced winding that forms the armature, since the armature remains stationary, it is referred as stator. The three phase stator winding are designated by symbols R-R', Y-Y', B-B', which have a mutual spacing of 120 degrees between each other as shown in fig 5.2(b).

On the other hand, the field system is mounted over a shaft with a provision of rotation, hence called the rotor. The field constitutes a pair of magnetic poles designated by symbols N & S , which provide the necessary magnetic flux. When the shaft is driven by a prime mover, a relative motion between the armature and the field is developed that produces the time rate of change of magnetic flux linkage in the armature conductors and hence emf gets induced in them. The nature of emf induced in the three phases of stator assumes sinusoidal waveform having same magnitude and frequency but displaced from each other by 120 electrical degrees. There are three individual phases of the stator can not attain peak emf value simultaneously. The sequence in which the three individual phase emf attains their peak is referred as phase sequence.

In the rotor of fig 5.2 (b) assumes rotation in the anticlockwise direction, then the order in which the emfs of respective phases attain their peak values represented by R-Y-B sequence or +ve sequence. If E_m happens to be the peak value of the emf induced per phase, then the instantaneous emf of respective phases for R-Y-B sequence may be represented by Eqn (5.1)

$$e_R = E_m \sin \omega t = E_m \angle 0^\circ$$

$$e_Y = E_m \sin (\omega t - 120^\circ) = E_m \angle -120^\circ$$

$$e_B = E_m \sin (\omega t - 240^\circ) = E_m \angle -240^\circ$$

for clockwise

$$e_R = E_m \sin \omega t = E_m \angle 0^\circ$$

$$e_B = E_m \sin (\omega t - 120^\circ) = E_m \angle -120^\circ$$

$$e_Y = E_m \sin (\omega t - 240^\circ) = E_m \angle -240^\circ$$

There exists a simple relationship between the speed of revolution of the rotor in revolutions per minute marked as N , existing number of poles in the field marked as P , and the generation frequency of the induced emf marked as f . It may be clearly noted that the frequency of the emf remains same for all the three phases. Assuming that if a rotor having P number of poles revolves at N revolution per minute, the frequency f of the induced emf per phase may be calculated in a simple manner

f (usually expressed in cycle per sec)

$$= \frac{P}{2} \times \frac{N}{60}$$

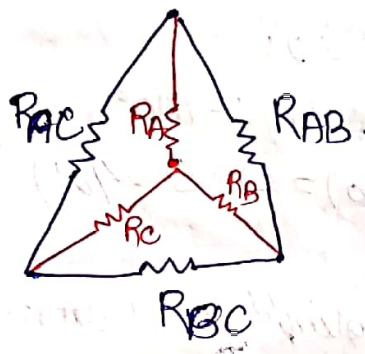
$$= \frac{PN}{120}$$

$$\text{So } f = \frac{PN}{120} \text{ Hz}$$

where P - poles
 N = synchronous speed
 f = frequency

Delta to star conversion

27

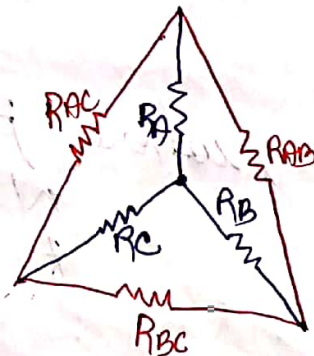


$$R_A = \frac{R_{AB} \times R_{AC}}{R_{AB} + R_{BC} + R_{CA}}$$

$$R_B = \frac{R_{AB} \times R_{BC}}{R_{AB} + R_{BC} + R_{AC}}$$

$$R_C = \frac{R_{AC} \times R_{BC}}{R_{AB} + R_{BC} + R_{AC}}$$

Star to delta conversion

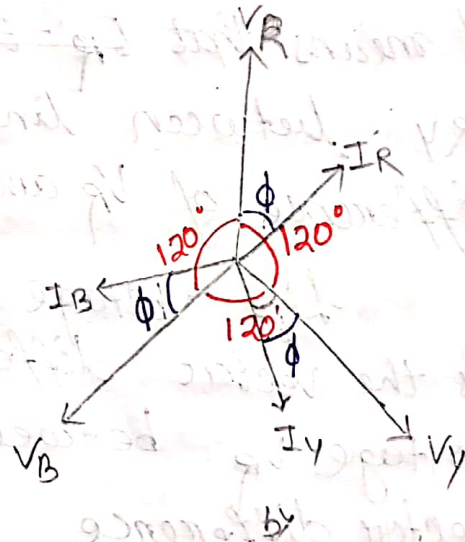
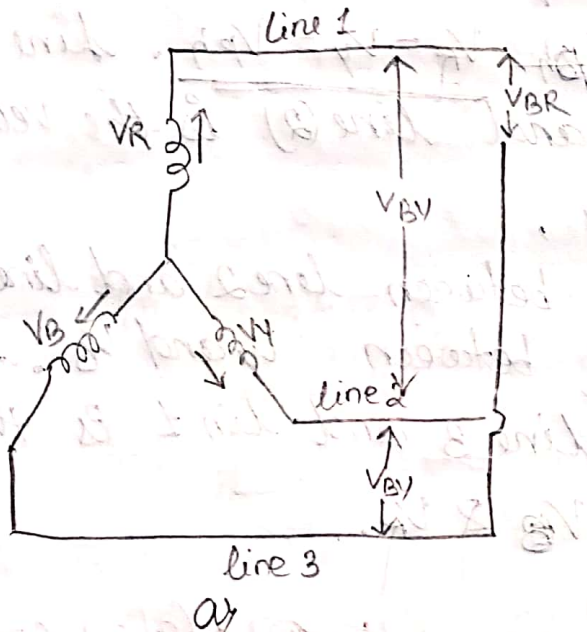


$$R_{AB} = R_A + R_B + \frac{R_A R_B}{R_C} = \frac{R_A R_B + R_B R_C + R_C R_A}{R_C}$$

$$R_{BC} = R_B + R_C + \frac{R_B R_C}{R_A} = \frac{R_A R_B + R_B R_C + R_C R_A}{R_A}$$

$$R_{CA} = R_C + R_A + \frac{R_C R_A}{R_B} = \frac{R_A R_B + R_B R_C + R_C R_A}{R_B}$$

Voltage & current Relation in star connection :-



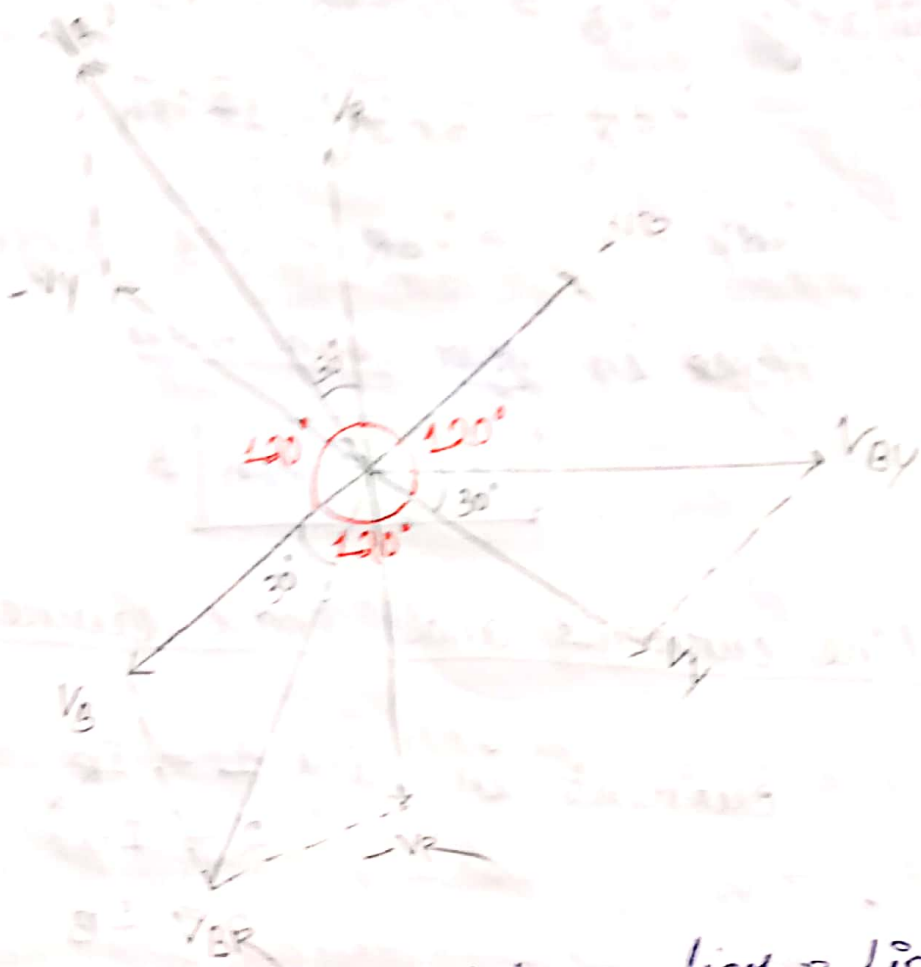
The voltage induce in each winding is called phase voltage. and current in each winding is like wise known as phase current. However the voltage available between the pair of terminals is called line voltage (V_L), and current flowing in each line is called line current (I_L). In fig(a) there is a inter connection, there are two phase windings between each pair of terminals but

since their similar ends have joined together they are in opposition. Obviously the instantaneous value of potential difference between any two terminals is the arithmetic difference of the two phase emfs concerned. However the rms value of this potential difference is given by the vector difference of the two phase emfs. The vector diagram for n voltages and current in a star connection each shown in the above figure (b), where a balanced system has been assumed.

It means that $E_R = E_Y = E_B$, $V_R = V_Y = V_B$. Line voltage V_{RY} between line (1) and line (2) is the vector difference of V_R and V_Y ,

Line voltage V_{YB} between line 2 and line 3 is the vector difference between V_Y and V_B . Line voltage V_{BR} between line 3 and line 1 is the vector difference of V_B & V_R .

Line Voltages & phase voltages: (Star connection)



The potential difference between line 1 & line 2 is $V_{RY} = V_R - V_Y$, hence V_{RY} is found by subtracting V_Y from V_R and its value is given by the diagonal of the parallelogram which is shown in the above figure. Obviously the angle between V_R and V_Y reversed each 60° hence if $V_R = V_Y = V_B = V_{ph}$ the phase emf.

$$\begin{aligned}
 \text{then } V_{RY} &= V_R - V_Y \\
 &= 2 V_{ph} \times \cos\left(\frac{60^\circ}{2}\right) \\
 &= 2 V_{ph} \cos 30^\circ \\
 &= 2 \times V_{ph} \times \frac{\sqrt{3}}{2}
 \end{aligned}$$

$$\boxed{V_{RY} = \sqrt{3} V_{ph}}$$

Similarly $V_{YB} = V_Y - V_B = \sqrt{3} V_{ph}$

$$V_{BR} = V_B - V_R = \sqrt{3} V_{ph}$$

$$V_{RY} = V_Y - V_R = \sqrt{3} V_{ph} = \text{line voltage say } V_L$$

Hence in star connection -

$$\boxed{V_L = \sqrt{3} V_{ph}} \quad \&$$

by line currents and phase currents: &

$$\text{current in line 1} = I_R$$

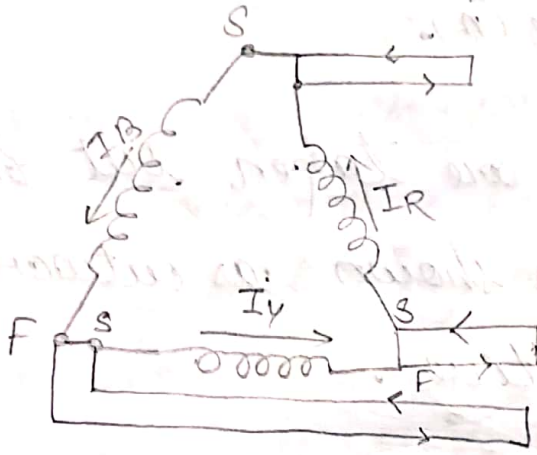
$$2 = I_Y$$

$$3 = I_B$$

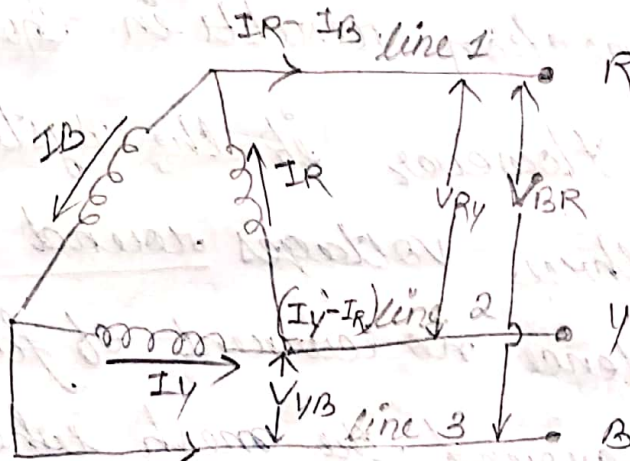
$$I_R = I_Y = I_B = \text{say } I_{ph} \text{ - phase current}$$

$$\boxed{\text{line current} = I_L = I_{ph}} \quad (\text{star connection})$$

Delta connection of Mesh connection:



(a)



(b)

In this form of inter connection the dissimilar ends of three phase winding are join together that is the "stranding" end of one phase is joined to the "finshing", end of the other phase and show on, which is shown in the fig (a).

In other words the three windings are joined in series to form a closed mesh which is shown in the figure (B).

Three leads are taken out from the three junctions as shown as outward directions are taken as positive.

It might look as if the ϕ this short interconnection results in short circuit the three windings. However if the system is balanced then sum of three voltages round the ^{closed} mesh is zero. Hence no current of fundamental frequency can flow around the mesh when the terminals are open. It should be clearly understood that at any instant the EMF. in $1-\phi$ is equal and opposite to the resultant of those in the other two phases.

This type of connection is also referred as ϕ 3- ϕ , three wire system.

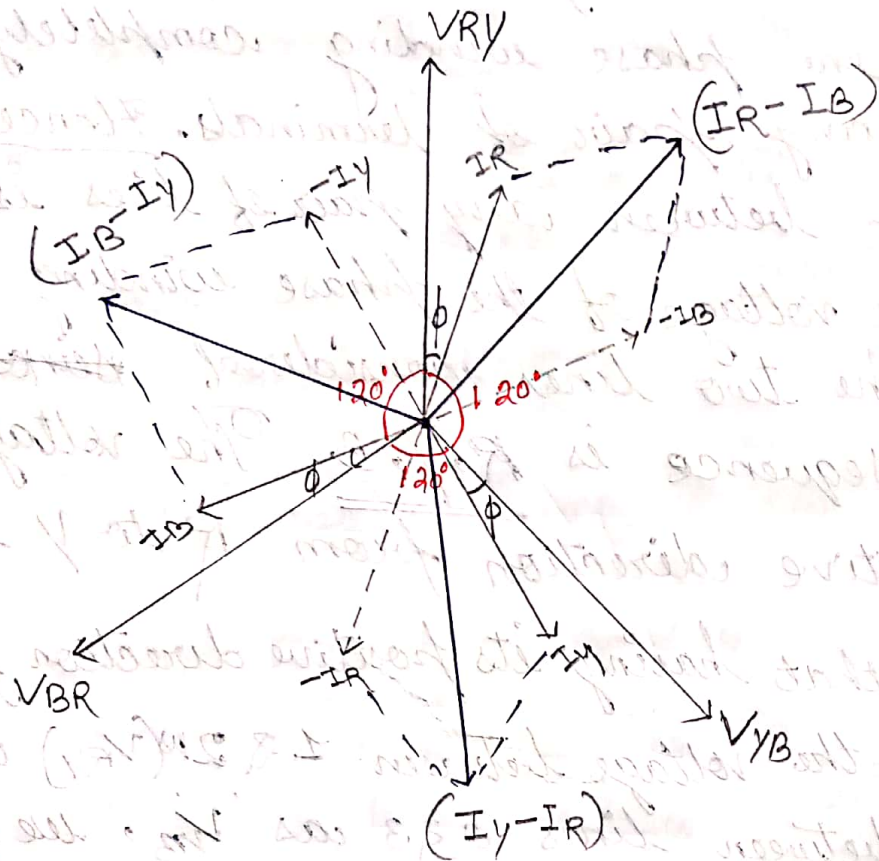
Line Voltages & Phase Voltages:

It is seen from the figure (b) that there is only one phase winding completely included between any pair of terminals. Hence Δ -connect the voltage between any pair of lines is equal to the phase voltage of the phase winding connected between the two lines considered ~~since~~ since phase sequence is R, Y, B. The voltage having its positive direction from R to Y leads by 120° on that having its positive direction from Y-B. calling the voltage between 1 & 2nd (V_{RY}) and that having between lines 2 & 3 as V_{YB} , we find that V_{RY} lead V_{YB} by 120° . Similarly V_{YB} leads V_{BR} by 120° as shown in the figure. Let, $V_{RY} = V_{YB} = V_{BR} =$ the line voltage V_L . Then it is

seen that $V_L = V_{ph}$

Now we will

Line currents & phase currents:



Current in line 1 that is $I_1 = I_R - I_B$

Current in line 2 $I_2 = I_Y - I_R$

Current in line 3 $I_3 = I_B - I_Y$

Current in line no 1 is found by compounding IR and I_B reversed and its value is given by the diagonal of parallelogram which is shown in the phasor diagram. The angle between IR and I_B reversed ($-I_B$) is 60° . If $I_R = I_Y$ is the phase current I_{ph} (say) then current in the line no-1

$$I_1 = 2I_{ph} \times \cos\left(\frac{60}{2}\right) = 2 \times I_{ph} \times \frac{\sqrt{3}}{2}$$

$$= \sqrt{3} I_{ph}$$

$$I_1 = \sqrt{3} I_{ph}$$

current in line no 2 is

$$I_2 = I_Y - I_R$$
$$I_2 = \sqrt{3} I_{ph}$$

In line no 3. $I_3 = I_B - I_Y$

$$I_3 = \sqrt{3} I_{ph}$$

Since all the line currents equal in magnitude that is $I_1 = I_2 = I_3 = I_L$. i.e. $I_L = \sqrt{3} I_{ph}$

Power:

$$\text{power per phase} = V_{ph} \times I_{ph} \cos \phi$$

$$\text{Total power} = 3 \times V_{ph} I_{ph} \cos \phi$$

However $V_{ph} = V_L$ and $I_{ph} = \frac{I_L}{\sqrt{3}}$

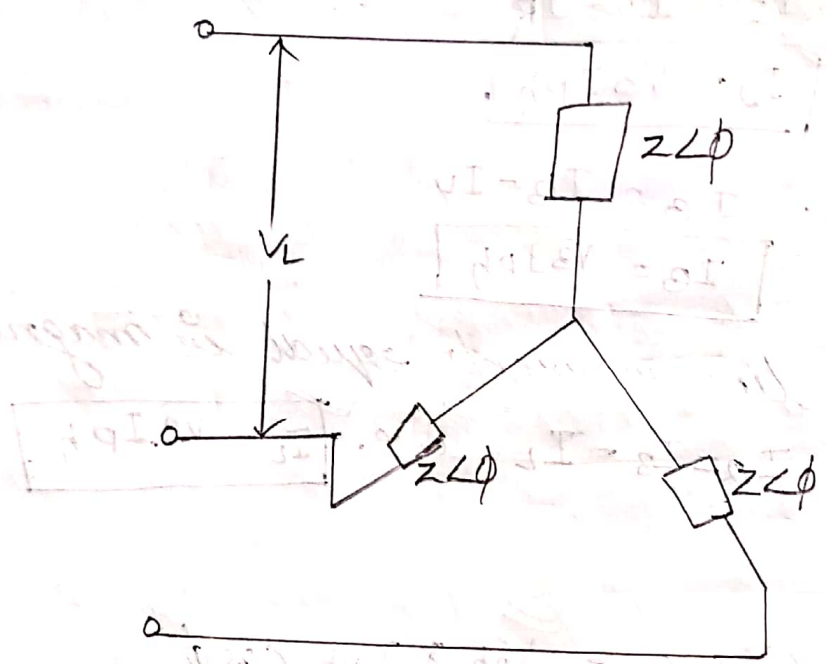
$$\Rightarrow I_{ph} = \frac{I_L}{\sqrt{3}}$$

Hence in terms of line values the above expression for power becomes $P = 3 \times V_L \times \frac{I_L}{\sqrt{3}} \cos \phi$

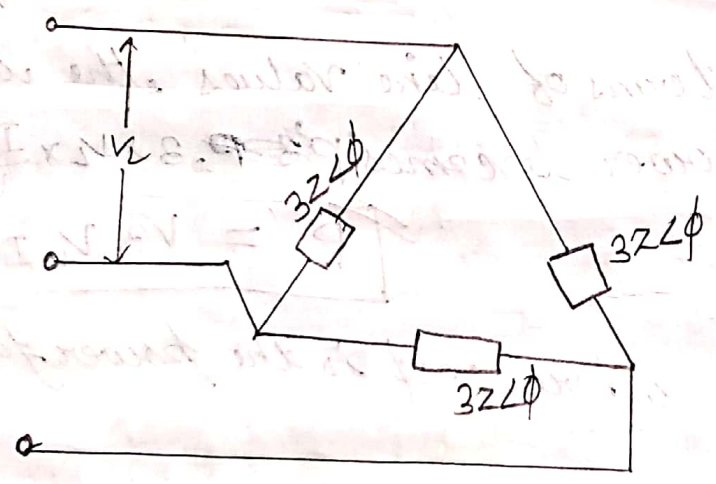
$$P = \sqrt{3} V_L I_L \cos \phi$$

where $\cos \phi$ is the power factor.

Balance Y/Δ and Δ/Y conversion:



(a)



(b)

In few view of the above relationship between the line and phase current and voltages, Any balanced star connection system may be completely replaced by an equivalent Δ connected system. For an Exmp. A three phase Δ connected system having voltage of V_L and line current I_L may be replaced by a Δ connected system in which phase voltage is V_L and phase current is $\frac{I_L}{\sqrt{3}}$.

Similarly a balanced Y connected load having equal branch impedance each of Z_{Δ} may be replaced by an equivalent Δ connected load whose each phase impedance each $3Z_{\Delta}$ which is shown in the above figure.

For a balanced Y connected load let $V_L =$ line voltage, $I_L =$ line current and $Z_{\Delta} =$ impedance per phase

$$V_{ph} = \frac{V_L}{\sqrt{3}}$$

$$I_{ph} = \frac{I_L}{\sqrt{3}} \quad I_{ph} = I_L$$

$$\phi \theta \left[Z_{\Delta} = \frac{V_L}{\sqrt{3} I_L} \right]$$

Now in the equivalent Δ -system the line voltages and currents must have the same values as in the \star Y-connected system. Hence we must have

$$V_{ph} = V_L$$

$$I_{ph} = \frac{I_L}{\sqrt{3}}$$

$$\therefore Z_{\Delta} = \frac{V_{ph}}{I_{ph}} = \frac{V_L \sqrt{3}}{I_L}$$

$$Z_{\Delta} = \frac{V_L \sqrt{3}}{I_L}$$

$$Z_{\Delta} = 3Z_Y$$

~~$$Z_{\Delta} = 3Z_Y$$~~

$$Z_{\Delta} = 3Z_Y \text{ or}$$

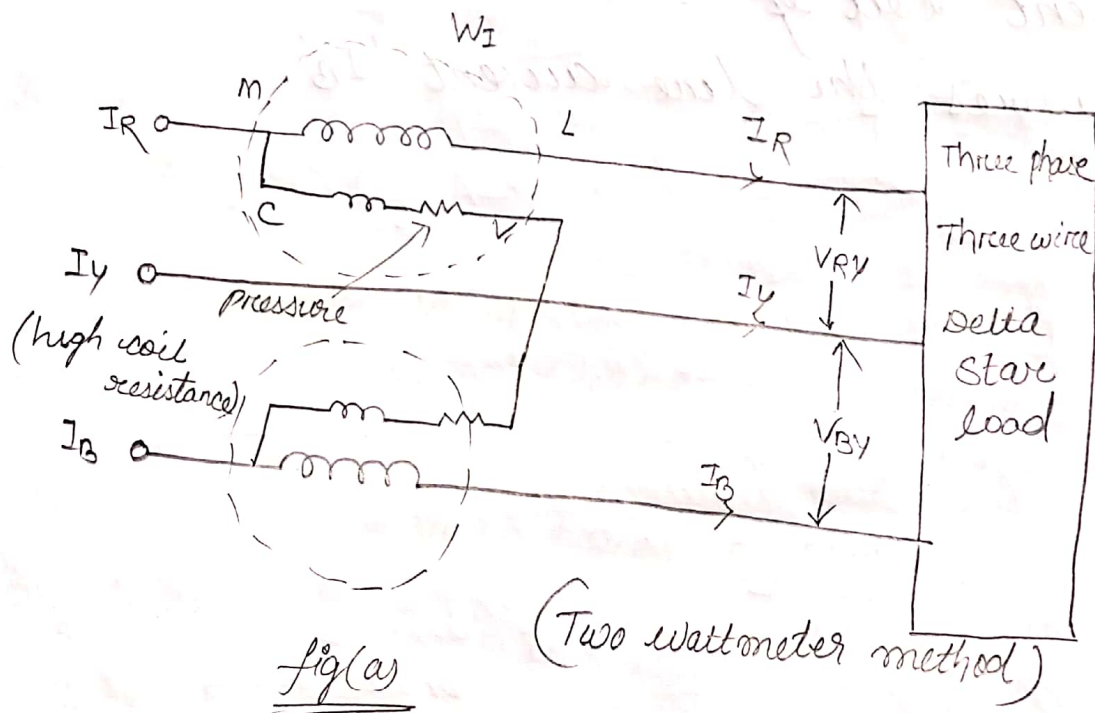
$$Z_Y = \frac{Z_{\Delta}}{3}$$

power measurement in three phase circuit:

Following methods are available for measuring power in a 3- ϕ load

- a) Three wattmeter method.
- b) Two wattmeter method.
- c) One wattmeter method.

by Two wattmeter method:



⇒ This method is the most effective method of all methods.

⇒ The circuit diagram for this scheme for clearly shown in the above figure. In which one phase is common to both pressure coil and current coil are connected in series with the remaining two phases.

⇒ As shown in the above figure, pressure coil of the first wattmeter (W_1) measures the line voltage ' V_{RY} ' and the pressure coil of the 2nd wattmeter (W_2) measures the line voltage ' V_{YB} '.

⇒ Similarly current coil of the first wattmeter w_1 measures the line current ' I_R ' and the current coil of the second wattmeter ' w_2 ' measures the line current ' I_B '.

In the figure (a) and (b) power measured by the 1st wattmeter (w_1) may be given in the form.

$$W_1 = V_{RY} \times I_R \cos \alpha$$

$$[W_1 = V_L I_L \cos(30^\circ + \phi)] \quad \dots (i)$$

$$W_2 = V_{By} + I_B \times \cos \beta$$

$$\boxed{W_2 = V_L \times I_L \times \cos(30 - \phi)} \quad \dots (ii)$$

Now sum of the two readings can be found by adding the eqⁿ (i) and (ii)

$$\begin{aligned} W_1 + W_2 &= V_L I_L [\cos(30 + \phi) + \cos(30 - \phi)] \\ &= V_L I_L [\cos 30 \cdot \cos \phi - \sin 30 \cdot \sin \phi + \cos 30 \cdot \cos \phi + \sin 30 \cdot \sin \phi] \\ &= V_L I_L [2 \cos 30 \cdot \cos \phi] \\ &= V_L I_L 2 \times \frac{\sqrt{3}}{2} \cos \phi \end{aligned}$$

$$\boxed{W_1 + W_2 = \sqrt{3} V_L I_L \cos \phi}$$

$$\boxed{W_{\text{total}} = \sqrt{3} V_L I_L \cos \phi} \quad \dots (iii)$$

To calculate the power factor of the circuit with the help of the readings,

$$|W_1 - W_2|$$

$$\begin{aligned} W_1 - W_2 &= V_L I_L [\cos(30 - \phi) - \cos(30 + \phi)] \\ &= V_L I_L [\cos 30 \cdot \cos \phi + \sin 30 \cdot \sin \phi - \cos 30 \cdot \cos \phi + \sin 30 \cdot \sin \phi] \\ &= V_L I_L [2 \sin 30 \cdot \sin \phi] \\ &= V_L I_L \times 2 \times \frac{1}{2} \times \sin \phi \end{aligned}$$

$$\boxed{W_1 - W_2 = V_L I_L \sin \phi} \quad \dots (iv)$$

ratio of equation (4) & (3)

$$\frac{|W_1 - W_2|}{|W_1 + W_2|} = \frac{V_L I_L \sin \phi}{\sqrt{3} V_L I_L \cos \phi} = \frac{1}{\sqrt{3}} \tan \phi$$

$$\Rightarrow \phi = \tan^{-1} \sqrt{3} \frac{|W_1 - W_2|}{|W_1 + W_2|} \quad \text{--- (vi)}$$

for power factor = $\cos \phi$
 $= \cos \cdot \tan^{-1} \sqrt{3} \left(\frac{W_1 - W_2}{W_1 + W_2} \right)$

sometimes two readings are equal i.e.

$$W_1 = W_2$$

$$\Rightarrow \cos \phi = \cos \cdot \tan^{-1} \sqrt{3} \left(\frac{W_1 - W_2}{W_1 + W_2} \right)$$

$$\Rightarrow \cos \phi = \cos \cdot \tan^{-1} \sqrt{3} \left(\frac{W_2 - W_2}{W_1 + W_2} \right)$$

$$\Rightarrow \cos \phi = \cos \cdot \tan^{-1} \sqrt{3} \times 0$$

$$\Rightarrow \cos \phi = \cos 0$$

$$\Rightarrow \boxed{\cos \phi = 1} \quad (\because 1 \text{ unity factor})$$

unity power factor.

Power management in 3- ϕ circuits:

following methods are available for

measuring power in a 3- ϕ load

a) Three wattmeter method

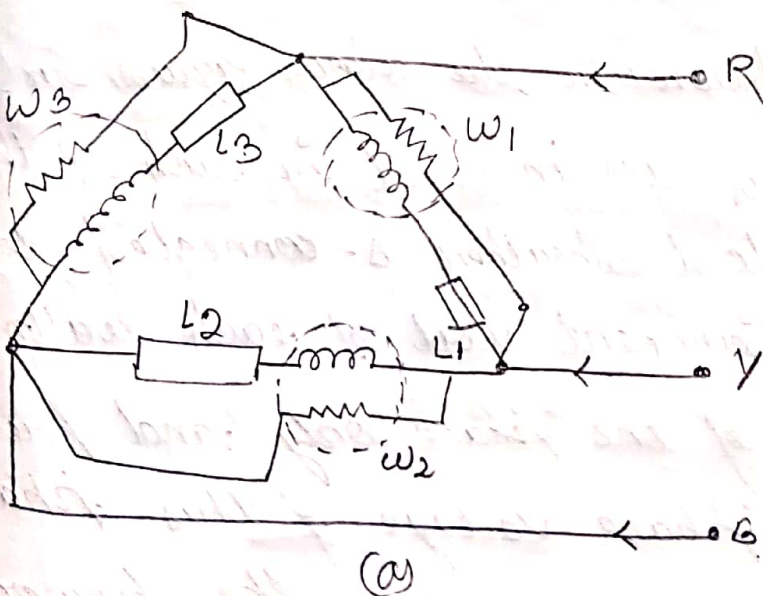
b) Two wattmeter method

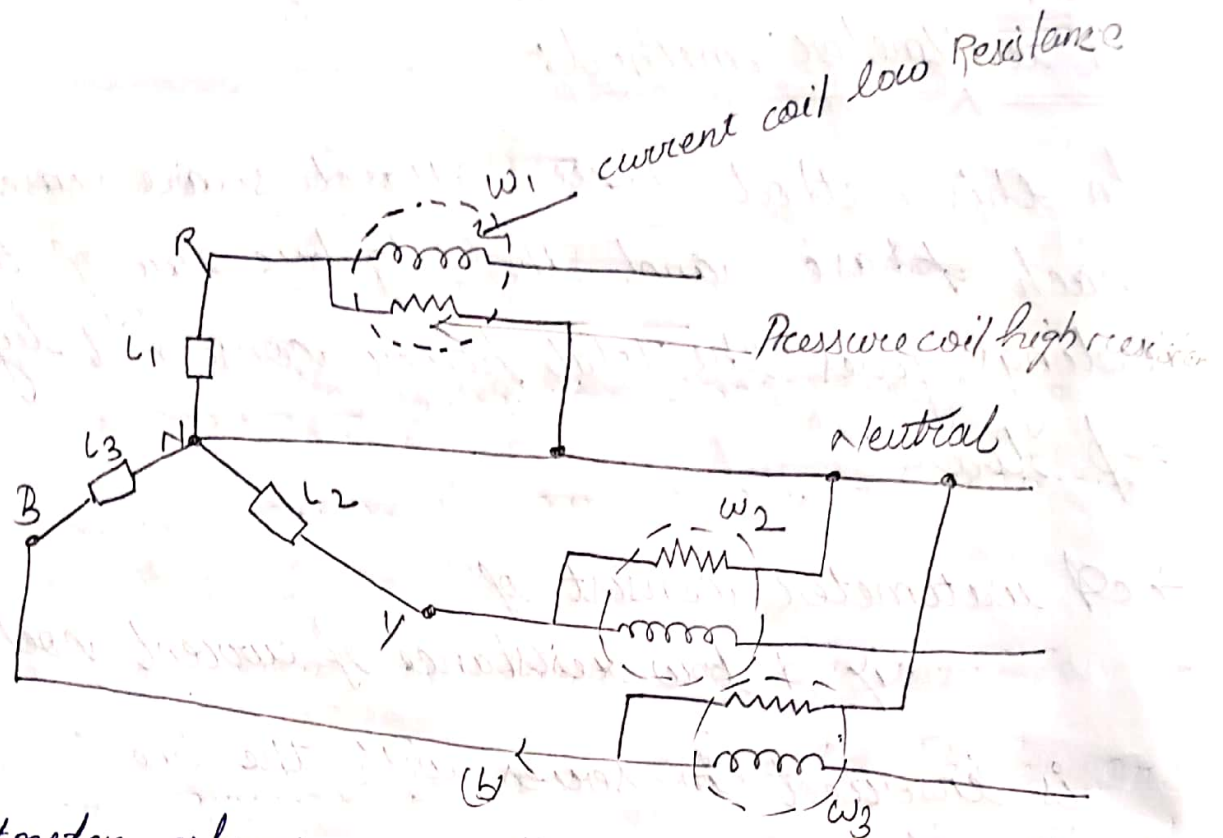
c) One wattmeter method

Three wattmeter method:

In this method, three wattmeters are inserted one in each phase and the algebraic sum of their readings gives the total power consumed by the 3- ϕ load.

- A wattmeter consist of
- i) A low resistance of current coil which is inserted in series with the line the current.
 - ii) High resistance pressure coil which is connected across the two points whose potential difference is to be measured.





A wattmeter shows a reading proportional to the product of the current through its current coil the potential difference across its potential or pressure coil and cosine of the angle between this voltage and current.

As shown in the above figure in this method 3 wattmeters are inserted in each of the three phase of the load whether Δ -connected or λ -connected. The current coil of each wattmeter carries the current of one phase only and pressure coil measures the phase voltage of this phase. Hence each wattmeter measures the power in a single phase. The algebraic sum of the readings of three wattmeter must give the total power in the load.

lance

high resistance

The difficulty of this method is that under ordinary conditions it is not generally feasible to break into the phases of a Δ -connected load not is it always possible, in the case of a Y -connected load, to get at the neutral point which is required for connections as shown in the figure.

Magnetic Circuit

M:3

Module: 3

Magneto Motive force (MMF):

It drives or tends to drive flux (ϕ) through a magnetic circuit corresponds to electromotive force (EMF) in an electrical circuit.

MMF is equal to the workdone in joules in carrying a unit magnetic pole once through the entire magnetic circuit. It is measured in ampere turns (AT) in fact as potential difference between any two points is measured by the workdone in carrying a unit charge from one point to another, similarly MMF between two points is measured by the workdone in joules in carrying a unit magnetic pole from one point to another.

Ampere Turns (AT) :

It is the unit of magnetomotive force (MMF) and is given by the product of number of turns of magnetic circuits and the current in amperes.

in those turns.

$$\boxed{\text{MMF} = NI}$$

Reluctance :

It is the name given to that property of the material which opposes the creation of magnetic flux through it. In fact it measures the opposition offered to the passage of magnetic flux through a material and is analogous to Resistance in an electrical circuit. Its unit is

$$\frac{\text{AT}}{\text{web}}$$

$$\text{Reluctance} = \frac{l}{\mu A} = \frac{l}{\mu_0 \mu_r A}$$

$$\boxed{\text{Resistance} = R = \frac{\rho l}{A}}$$

$$R = \frac{l}{\sigma A}$$

In other words the Reluctance of a magnetic circuit is the number of Ampere Turns required per web. of magnetic flux in the circuit, since

$$1 \text{ AT/web.} = \frac{1}{\text{henry}}$$

the unit of Reluctance is Reciprocal of henry.

Magnetic flux (ϕ) is \propto MMF,

$$\Rightarrow \phi = k \text{MMF}$$

where k is a constant of proportionality and is defined as the reciprocal of Reluctance. Thus we may write as -

$$\phi = \frac{1}{R} \text{MMF}$$

$$\Rightarrow R (\text{Reluctance}) = \frac{\text{MMF}}{\phi}$$

$$R = \frac{NI}{\phi A} \quad \left(\begin{array}{l} \because \text{MMF} = NI \\ \phi = \phi A \end{array} \right)$$

$$\Rightarrow R = \frac{NI}{\mu H A}$$

$$\Rightarrow R = \frac{NI}{\mu \left(\frac{NI}{l} \right) A} \quad \left(\because H = \frac{NI}{l} \right)$$

$$\Rightarrow R = \frac{l}{\mu A}$$

Note:

The quantity used in electromagnetism have some similarities with the quantities with the electricity. The analogy between two shades is represented below

Electric quantity

magnetic quantity

1) EMF (volt)

1) MMF (AT)

2) current (A)

2) flux (web)

3) Resistance (Ω)

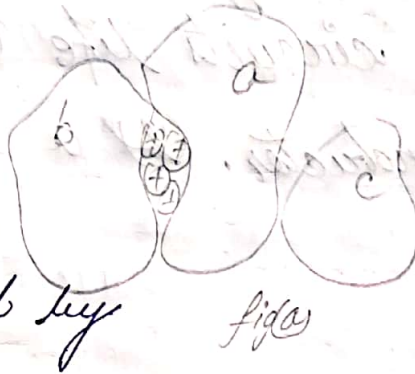
4) reluctance (AT/web)

4) current density (A/m²)

5) flux density (wb/m²)

Ampere's Work Law or Ampere's circuit law:

The law states that the MMF around a closed path is equal to the current enclosed by the path



mathematically $\oint \vec{H} \cdot d\vec{s} = I$ amperes

where \vec{H} is the vector represented

magnetic field in dot product with vector $d\vec{s}$ of the enclosing path 's' around current I ampere and that is why line integral (\oint) of dot product $\vec{H} \cdot d\vec{s}$ is taken.

Work law is very comprehensive

and is applicable to all magnetic field whatever the shape of enclosing path

Ex: 'a' and 'b' in the above figure. Since path

'c' does not enclose the conductor, the mmf around it is zero.

The above work law is used for obtaining the value of the magnetomotive force around simple idealized circuits like (a) a long straight current carrying conductor, (b) a long solenoid.

Magnetic Motive force Around a long straight conductor:

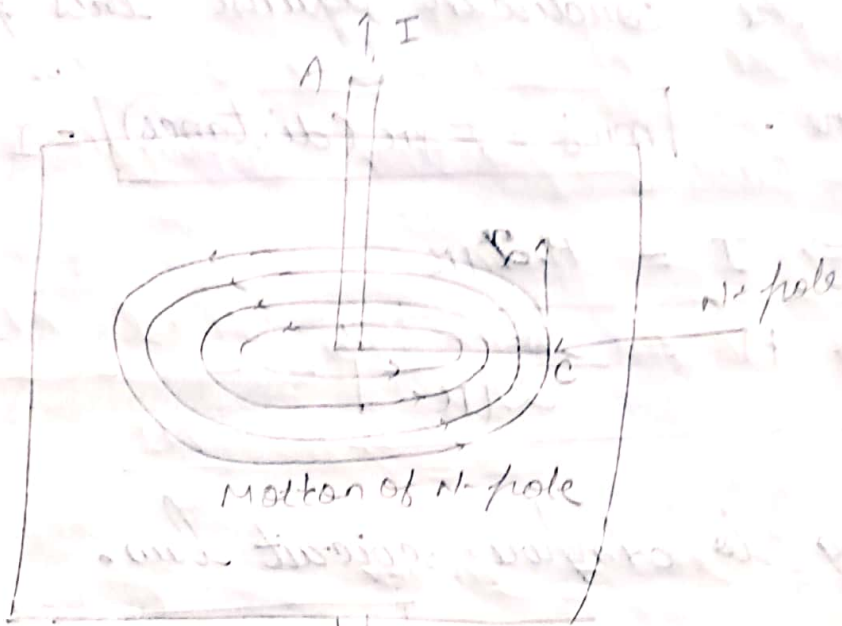


Fig. (a)



Fig. (b)

In the fig (a) a straight conductor which is assumed to extend to infinite in either direction let it carry a current ' I ' ampere upwards the magnetic field consist of circular lines of force having there plane perpendicular to the conductor. and there centers at the center of the conductor.

Suppose that field strength at point 'c' distance r meter from the center of the conductor is ' H ' then it means that if a unit N-pole is placed at direction of this force would be tangential to the circular line of force passing

through c, If this n-hole is moved once ~~around~~ round the conductor against this force then the work done. $\boxed{mmb = F \times r \times (\text{distance})} = I$

$$\Rightarrow I = H \cdot 2\pi r$$

$$\boxed{\Rightarrow H = \frac{I}{2\pi r}} \quad \text{--- --- --- (1)}$$

According to Ampere circuit law,

$$\boxed{\oint \vec{H} \cdot d\vec{s} = I} \quad (\text{unit} = \text{joule/A})$$

According to the fig (b).

If there are n number of conductors then

$$\boxed{H = \frac{nI}{2\pi r}} \quad (\text{unit of } nI = \text{A/m})$$

$$\boxed{B = \mu_0 \cdot \frac{nI}{2\pi r} = \mu_0 \mu_r \frac{nI}{2\pi r}}$$

$$\boxed{\mu = \mu_0 \mu_r}$$

~~B = H~~

$\frac{\text{weber}}{\text{m}^2} = \frac{\text{Vs/A}}{\text{m}^2}$
which is the unit of B.

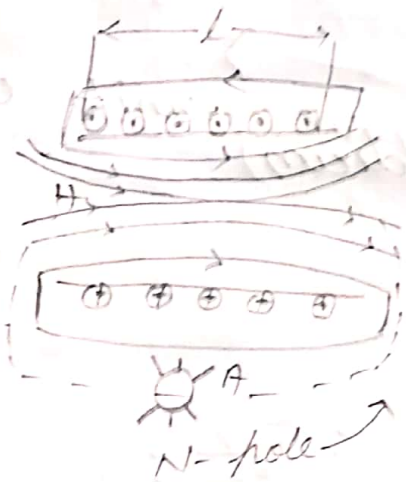
In Air $B = \mu_0 \cdot \frac{nI}{2\pi r}$

In medium $B = \mu_0 \mu_r \frac{nI}{2\pi r}$

Magnetic field strength in a long solenoid:



Magnetic field around
a coil carrying electric current



Let the magnetic field strength along the axis of solenoid be H . Let us assume that

1. The value of H remains constant throughout the length l of the solenoid.

2. The volume of H outside the solenoid is negligible.

H is the force acts on the N-pole only over the length l then the work done in one round is =

$$\boxed{H \times l = I \text{ Amp.}}$$

Joule

The ampere turns lived with this path are NI , where N = Number of turns ; I = is the current passing through it

According to the work law $[H \times l = NI]$

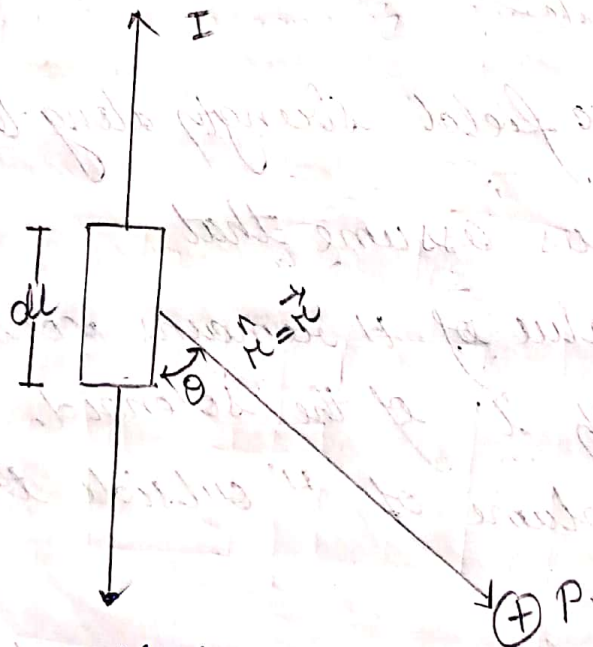
$$\Rightarrow H = \frac{NI}{l}$$

also 'B' = $\frac{\mu NI}{l}$ in Air

$B = \frac{\mu_0 \mu_r NI}{l}$ in medium

} unit web/m²

Biot-Savart Law:



$$dH = \frac{I dl \sin \theta}{4\pi r^2} \text{ A/m}$$

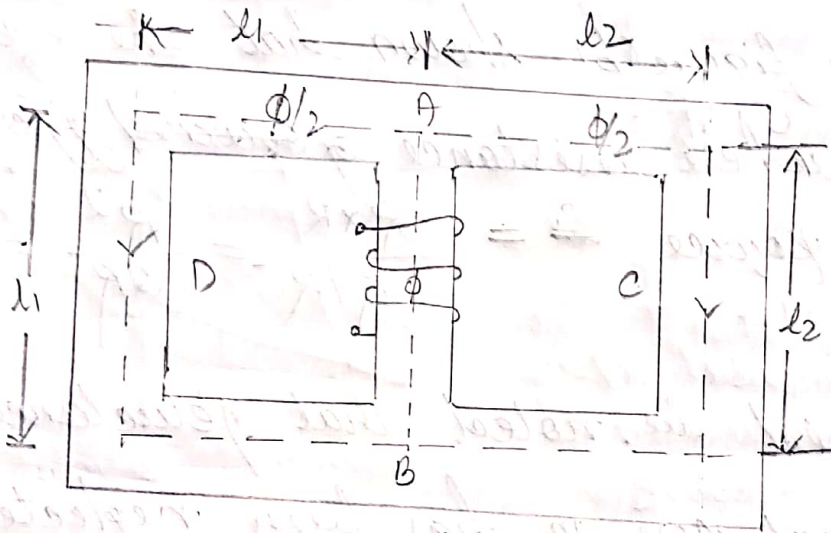
or, $d\vec{H} = (I d\vec{l} \times \vec{r}) / 4\pi r^2$ in vector form

The direction of $d\vec{H}$ is perpendicular to the plane containing both $d\vec{l}$ and \vec{r} i.e.

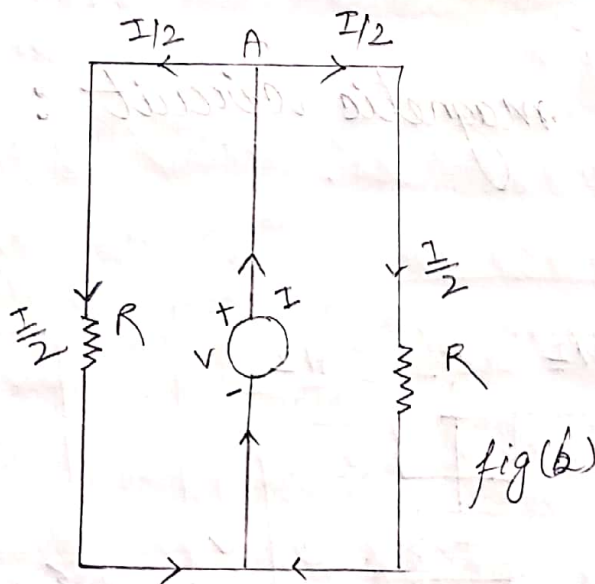
entering, or $d\vec{B}_0 = \frac{\mu I dl \sin\theta}{4\pi r^2} \omega b/m^2$

* and $d\vec{B}_0 = \frac{\mu \vec{I} \times d\vec{r}}{4\pi r^2}$ in vector form

parallel magnetic circuit:



fig(a)



fig(b)

In fig(a) a parallel magnetic circuit is shown which consists of two parallel magnetic paths ACB, ADB acted upon the same mmf each magnetic path has an average length of $2 \times (l_1 + l_2)$. The flux produced by the coil wound on the central core is divided equally at the point

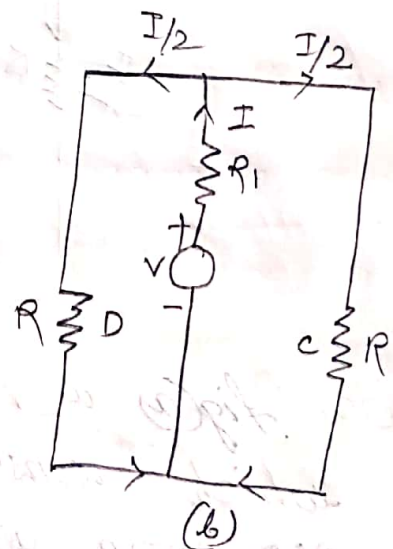
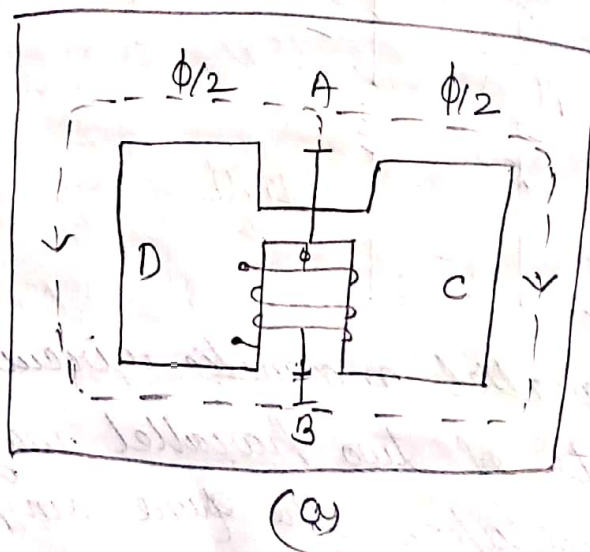
A. between the two outer parallel paths.

The reluctance offered by the two parallel paths is equal to the half of reluctance of each path.

In the figure (b) shown that the equivalent circuit where resistance offered to the voltage source $i = \frac{R \times R}{R + R} = \frac{R^2}{2R} = \frac{R}{2}$

It should be noted that reluctance offered by the central core AB has been neglected in the above treatment

Series parallel magnetic circuit :



In the fig(a) it shows that two parallel magnetic circuit ACB and ACD connected across the common magnetic path AB, which contains an air gap of length $2l_g$ as usual the flux ϕ in the common core is divided equally at the point A between the two parallel paths which has equal reluctance. The reluctance of the path AB consists of

- i) air gap reluctance
- ii) The reluctance of the central core which comparatively negligible hence the reluctance of the central core AB equals only the air gap reluctance across which are connected to equal parallel reluctances.

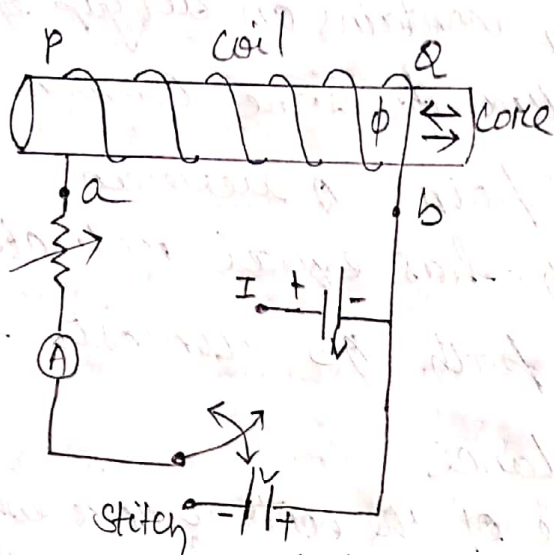
Hence the MMF required for this circuit would be the sum of

- i) that required for the air gap
- ii) that required for either of the two paths (not for both)

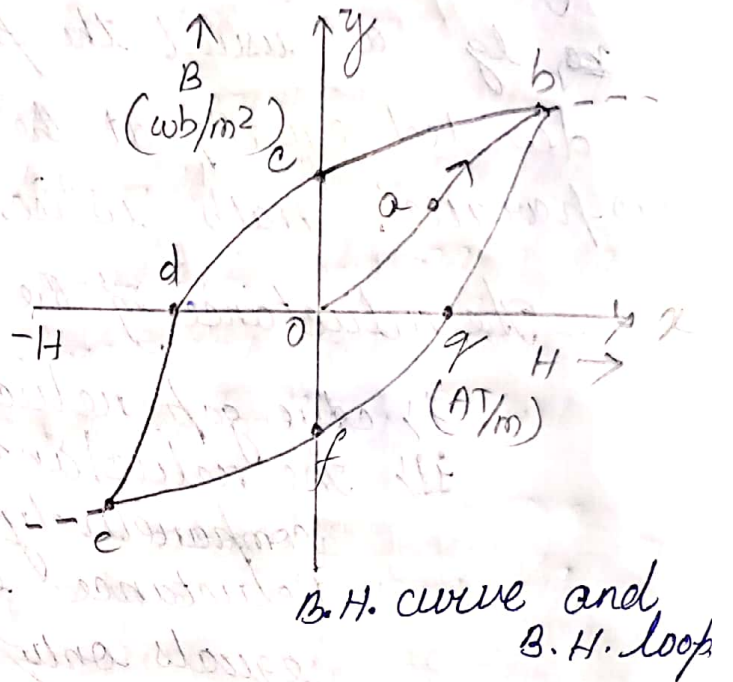
The equivalent electrical circuit which is shown in the figure (b) where the total resistance offered to the voltage source.

$$R_1 + \frac{R \times R}{R + R} = R_1 + \frac{R^2}{2R} = R_1 + \frac{R}{2}$$

B-H curve for magnetic materials:



Experimental set-up for determination of B-H curve



B.H. curve and B.H. loop

A graphical representation of the variation in 'b' as a result of variation in H in a sample of magnetic material is called B.H. curve or simply a magnetisation curve. The arrangement of experimental determination of B.H. curve for a given specimen of a magnetic material is shown in the fig. (a). It consists of a specimen of magnetic material marked as P & Q. A piece of conducting wire with enamel covering is wound over the specimen

which forms the coil two batteries a rheostat and one ammeter are connected to the closed loop wire as shown in the figure there may be two cases to examine the forward variation and reversal of magnetisation H as discussed below.

case - 1

when the key is moved the position 'one' a current I flows in the conductors from a to b. which in terms sets of magnetic flux ϕ in the specimen.

The cores of magnetic flux is straight but outside the specimen it is curved let the magnetic flux in this case be directed from left to right which corresponds to the forward direction and magnetisation in the core of the specimen.

case - 2

when the key is moved to the position (2), a current I flow in the conductors from end b to end a, which in terms sets of magnetic flux ϕ in the specimen. Inside the specimen the cores of magnetic flux is straight but outside the specimen it is curved let the magnetic flux in this case be directed from right to left which corresponds to reversal of magnetisation in the core of the specimen.

The objective of this experiment is to vary the $\text{ampere turns per unit length (H)}$ from zero to a sufficiently large value for each of the two cases described above and observe the corresponding variation in flux density (B). This is achieved by varying the current in the circuit with the help of the rheostat present in the circuit. For each variation of the current in both directions (i.e. forward flow and backward flow) corresponding values of H and B are recorded and plotted in the graph to obtain the $B-H$ curve as shown in curve fig.

Initially B remains directly proportional to H for which the graph gives a linear characteristic as illustrated by the portion oa . With increasing H , the cores get saturated and cannot permit a proportionate increase in B . Thus the graph becomes flat for increasing H . This has been shown by the region ab of the graph. In the next step, the current is reduced from the existing value to zero value and the curve is traced along bc . Then the current is reversed by changing over the switch from position 1 position to 2 and reversal of ampere turns takes place. As the current increases in the reverse direction, the B increases in the reverse direction too and the graph is retraced along cd .

In the next step the mmf is increased in the negative direction until saturation is observed at point e. Then the current is reduced from the existing value to zero value and the curve is traced along eb. Then the current is again reversed by changing over the switch from position 2 to 1 and by repeating the process, we may close the graph at point b by tracing through point g.

The closed loop characteristic of B versus H so obtained by the process of repeating the forward application and reversal of H in the specimen is called B-H loop or hysteresis loop. Some salient points on the B-H loop are explained below. (b, c, d, e, and g)

Saturation:

Point b and e represents two extreme condition of magnetization, called saturation condition of the magnetic material, during forward and reversal condition of magnetization respectively, for each of these points B has a limiting value which speaks of the maximum flux density that can be produced in a magnetic material for any increasing

order of H.

Retentive capacity:

At locations c and f on the B-H curve, B indicates a non zero value (denoted by B_c or B_f) even though H indicates a zero value. It means that B and H do not go step in step rather B exhibit a lagging effect with respect to H.

that is why the core retains some flux density of magnetism, although current has been completely withdrawn. The amount of magnetism held by the core at these points is also referred as residual magnetism, which is solely due to retentive capacity of the material.

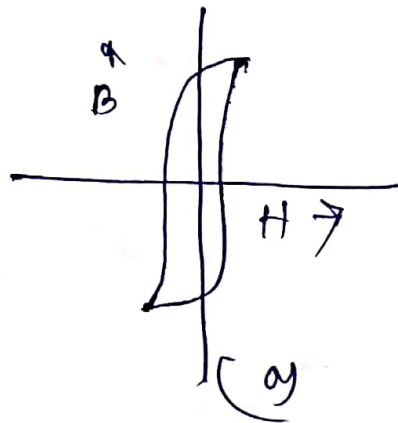
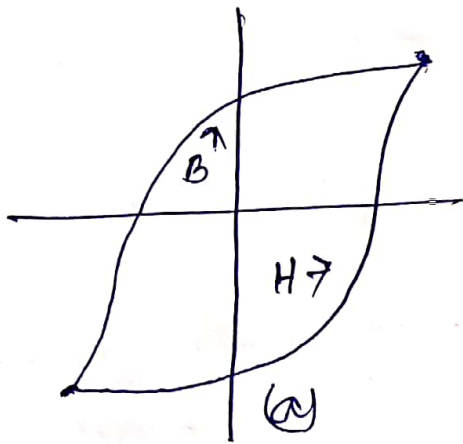
Coercivity: At the location d and g on B-H curve B indicates a zero value even though H indicates a non zero value. It means that B and H do not go step in step; rather B exhibits a lagging effect with respect to H. The amount of H required to reduce the residual magnetism to zero is called ~~core~~ coercive force.

Hysteresis Loss:

The effect due to which the magnetism established in a magnetic material lags behind the magnetization during cyclic application of forward and ^{reverse} magnetic fields to the sample of the magnetic material is called hysteresis. Hysteresis is mainly due to inertial effect that is the inability of the magnetic dipoles present in the specimen to follow up, the desired orientation as demanded by the quick reversal of the impressed cyclic magnetic field. In this process some energy gets dissipated to overcome and opposition raised by the ~~material~~

Hysteresis. This loss of energy is termed as hysteresis loss. Let the energy loss due to hysteresis is dissipated as heat energy. It is numerically equal to the area bounded within the hysteresis loop.

one major drawback of hysteresis loss is the temperature rise in the ~~the~~ core due to heat engine energy, which is highly undesirable as it affects the performance and operation of equipment. Thus it is always preferable to select magnetic materials with narrow hysteresis loop so as to reduce the hysteresis loss. These materials are designed separately and are manufactured with care. Some typical names of magnetic materials having narrow hysteresis loop are: a) silicon steel b) cold-rolled grain-oriented steel c) hot rolled grain oriented steel. A comparison of the hysteresis loop for the two cases of ordinary steel and silicon steel is shown.



There are various factors that affect the hysteresis loss in a magnetic material. Steinmetz developed a generalized expression for hysteresis loss as given in ^{below} Eq.

$$W_h = K_h f (B_m)^k$$

where W_h = Hysteresis loss per unit volume in W/m^2

K_h = Hysteresis coefficient,

f = cyclic frequency of magnetization. (Hz)

B_m = maximum flux density (Wb/m^2)

K = Steinmetz coefficient (varies between 1.5 to 2.5)

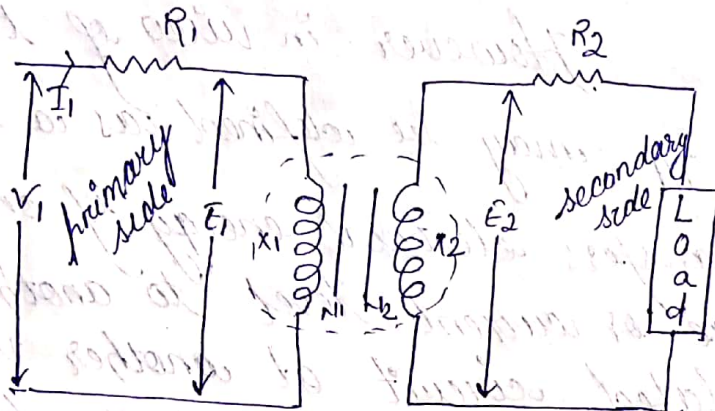
Transformer

Module: 4

Module: 4

Single phase transformer (1- ϕ):

It is a static device used to transform ac electrical energy at constant frequency.



circuit diagram of 1- ϕ transformer

The main aim of this chapter is to familiarize to the reader with the utility of the transformers in practical ac circuit a transformer plays an important role in the present day power systems in transmitting and distributing electrical power at various levels of voltage. For this reason transformer may be classified as

1. 1- ϕ and 3- ϕ transformer (T/F)
2. step up and step down T/F
3. core type and shell type
4. power T/F, distribution T/F, instrument T/F, auto T/F.

Definition: In the construction view of a transformer. It may be defined as a static device of two windings (primary and secondary) which are electrically isolated from each other but magnetically coupled by a common magnetic flux.

However in view of this operation a 1- ϕ T/F may be defined as a static device, transfers electrical energy of one circuit of one voltage or current level to another electrically isolated circuit at another voltage or current level without changing the power and frequency.

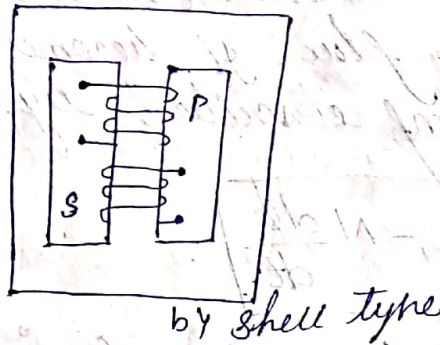
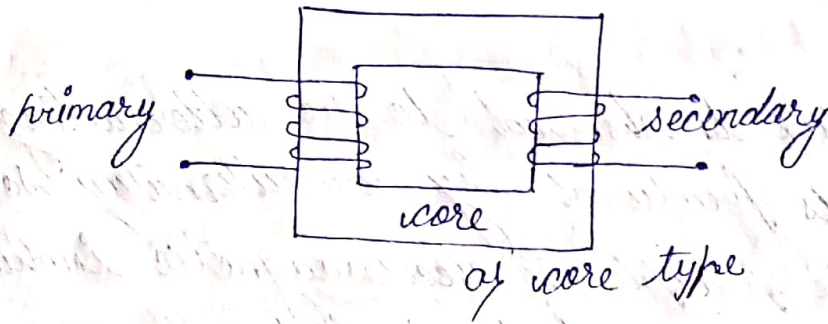
construction:

The main parts of a 1- ϕ T/F

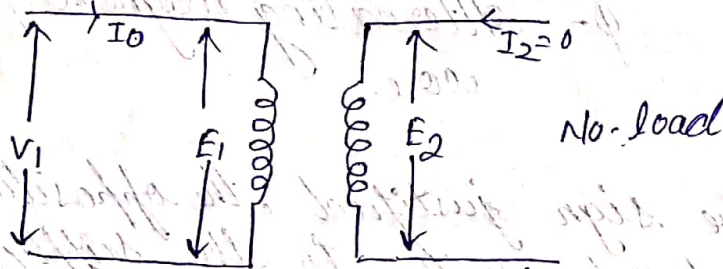
1. A setup two isolated winding.
2. A common magnetic core.

Depending on the winding arrangement over the core 1- ϕ transfer may be classified as core type and shell type. In the core type transformer, the windings surround the core in a shell type T/F, the core surrounds the winding.

The left diagram is shown in the below figure.



Operation :



operation of a transformer is based on the principle of Faraday's law of electromagnetic induction, which includes self induction and mutual induction. Let us first imagine that an alternating voltage of rms value V_1 and frequency f is fed to the primary winding of a $1-\phi$ T/F while the secondary winding is open. Due to the action of AC voltage primary winding draws a current which refers to no load primary current I_0 .

This current sets up a magnetic flux ϕ in the magnetic core which is in turn links both the windings.

This flux is observed to be alternating in nature as it is produced by an alternating source according to the principle of electromagnetic induction when a coil or a conductor is linked with an alternating magnetic flux. It becomes the seat of an induced emf described by

$$E = -N \frac{d\phi}{dt} \quad \dots \dots \dots (1)$$

where E = induced emf in the coil.

N = Number of turns in the coil.

ϕ = Alternating magnetic flux in the core.

The -ve sign justified the opposition offered by the induced emf to the supply voltage that is satisfying Lenz's law, which states that the effect opposes the cause that produced it.

Since both windings are linked by a common alternative flux separate emf get induced in each winding. The emf is induced in the primary winding may be designated by E_1 which as the result of self induction i.e. flux of a coil links the coil itself and induced

in the secondary winding may be designated by E_2 which is the result of mutual induction (i.e. flux of a coil links another coil and induces a emf in the other coil) with the help of eq. we may now write the expression for E_1 and E_2 separately.

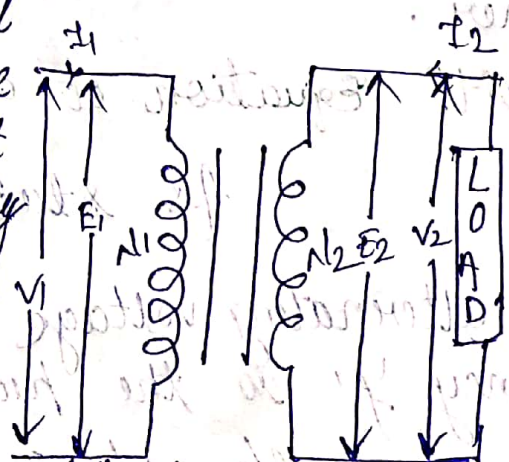
$$E_1 = -N_1 \frac{d\phi}{dt} \quad \dots (A)$$

$$E_2 = -N_2 \frac{d\phi}{dt} \quad \dots (B)$$

where N_1 and N_2 representing no. of turns in the primary and secondary winding respectively. As long as secondary winding remains open, the terminal voltage remains equals to the emf induced in the secondary (i.e. during the no load condition - $V_2 = E_2$). The operation described is called no load operation of a single phase transformer.

operation of a 1- ϕ transformer with load:

In order to explain the load operation of a single phase transformer, let us connect to a load to the secondary terminal of the transformer as shown in the above fig.



Due to this load a secondary current I_2 starts flowing in the closed loop of the secondary winding. This current

produces another alternative flux (ϕ') whose direction of flow in the core is found to be opposite to the earlier flux (ϕ) present in the same core. Hence the net flux in the core reduces from ϕ_2 to ϕ_1 is equal to $(\phi - \phi')$. As the flux reduces in strength the emf induced in two windings reduces in magnitude too.

A reduction in the magnitude of E_1 may be viewed as ~~weaking~~ weakening of the opposition offered to the supply voltage v_1 , and as a result the new current in the primary increases from I_0 to I_1 . So finally it may be concluded that although these two windings are electrically isolated, a change in load current I_2 in the secondary winding reflected the corresponding change on the primary current I_1 . This part of the operation is known as on load operation of a 1- ϕ transformer.

EMF Equation of a 1- ϕ transformer:

As stated in the previous section the alternating voltage of rms value v_1 and frequency f is applied to the primary winding makes a current flow of I_0 in the same winding.

which in term, develops a magnetic flux ϕ in the core assuming that the supply is sinusoidal, the flux should also be sinusoidal in nature which be mathematically expressed as $\phi = \phi_m \sin \omega t$ --- (4)

It is also mentioned earlier that due to the rate of change of flux linkage with the winding to separate emf get induced in respective winding as indicated in the eqⁿ.

(2) & eqⁿ (3) respectively. These eqⁿ become the starting point for obtaining the required EMF eqⁿ of a 1- ϕ transformer so eqⁿ (2) & eqⁿ (3) are explained in the following manner to get the final emf eqⁿ.

$$E_1 = -N_1 \frac{d\phi}{dt}$$

$$= -N_1 \frac{d}{dt} (\phi_m \sin \omega t)$$

$$= -N_1 \phi_m \omega \cos \omega t$$

$$= -N_1 2\pi f \phi_m \left[-\sin(\omega t - \pi/2) \right]$$

$$\Rightarrow E_1 = N_1 2\pi f \phi_m \sin(\omega t - \pi/2)$$

$$\Rightarrow E_1 = E_{m1} \sin(\omega t - \pi/2) \quad \text{--- (5)}$$

$$\text{So } E_{m1} = 2N_1 \pi f \phi_m \quad \text{--- (6)}$$

$$E_2 = -N_2 \frac{d\phi}{dt} = -N_2 \frac{d}{dt} (\phi_m \sin \omega t)$$

$$= -N_2 \phi_m \omega \cos \omega t$$

$$= -N_2 \phi_m 2\pi f (\cos \omega t)$$

$$= -N_2 2\pi f \phi_m \left[\sin(\omega t - \pi/2) \right]$$

$$= -N_2 2\pi f \phi_m \sin(\omega t - \pi/2)$$

$$E_2 = E_{m2} \sin(\omega t - \pi/2) \dots (7)$$

$$\text{So } \boxed{E_{m2} = 2N_2 \pi f \phi_m} \dots (8)$$

eqⁿ. (6) & eqⁿ. (8) represents the peak value corresponding to the instantaneous emf given by eqⁿ. (5) & (7) respectively. Therefore from their respective peak values.

$$E_{m1} = 2\pi N_1 f \phi_m$$

$$E_{1\text{rms}} = \frac{E_{m1}}{\sqrt{2}} = \frac{2\pi N_1 f \phi_m}{\sqrt{2}} = \sqrt{2} \pi N_1 f \phi_m$$

$$\boxed{E_{1\text{rms}} = 4.42 N_1 f \phi_m} \dots (9)$$

$$E_{m2} = 2\pi N_2 f \phi_m$$

$$E_{2\text{rms}} = \frac{E_{m2}}{\sqrt{2}} = \frac{2\pi N_2 f \phi_m}{\sqrt{2}}$$

$$= \sqrt{2} \pi N_2 f \phi_m \dots$$

$$\boxed{E_{2\text{rms}} = 4.42 N_2 f \phi_m} \dots (10)$$

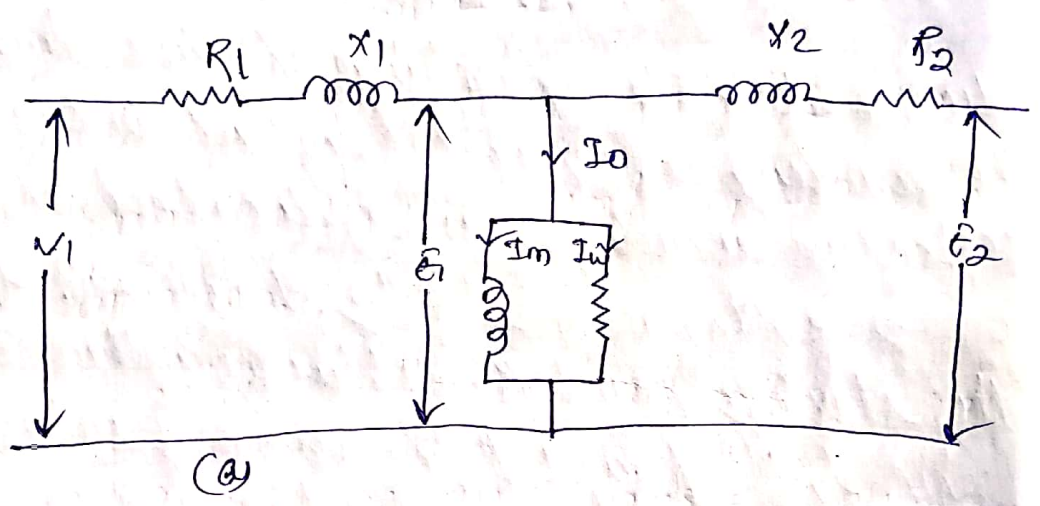
Eqⁿ. (9) represents the primary side emf eqⁿ for a single phase transformer. Eqⁿ. (10) represents the secondary side emf eqⁿ for a 1- ϕ transformer.

In this two eqⁿ it is important to note that emf induced in a particular winding of a transformer as a function of supply frequency.

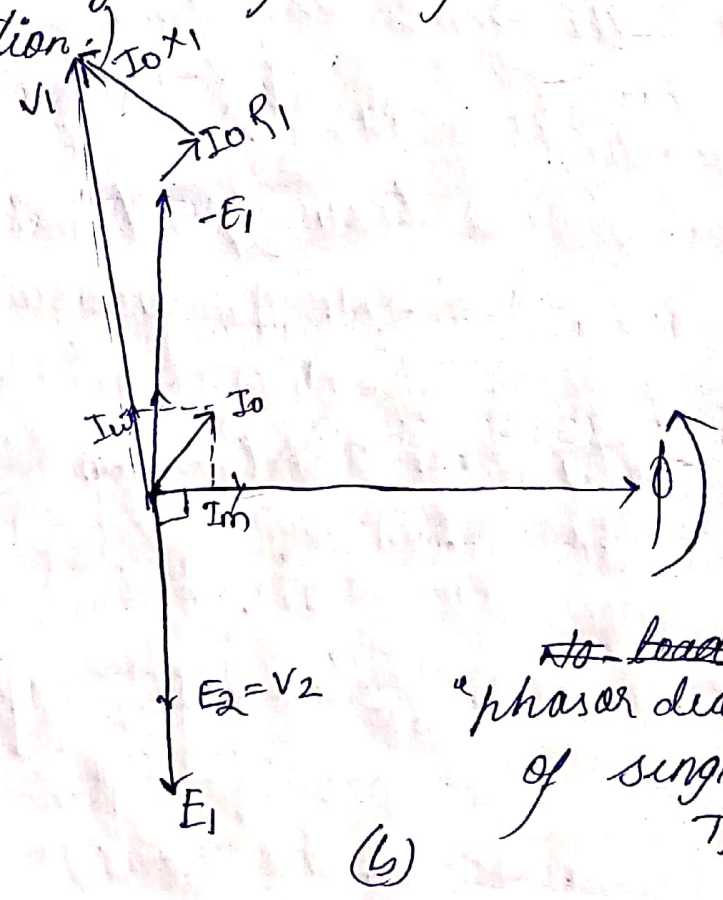
Transformer phasor diagram :

1. No load phasor diagram
2. Unload phasor diagram

No load phasor diagram :



(circuit diagram of transformer under no-load condition)



No load no-load phasor diagram of single phase T.F.

In order to draw the no-load phasor diagram we start with flux phasor as the reference phasor, and plot it along the +ve x-axis of the coordinate system, which is shown in the figure

as already indicated in the equation,

$$E_1 = E_m \left[\sin \left(\omega t - \frac{\pi}{2} \right) \right] \quad \text{--- (9)}$$

$$\phi = \phi_m \sin \omega t \quad \text{--- (10)}$$

A sinusoidal flux induces EMFs in the primary and secondary windings, which are also sinusoidal in nature and maintain a phase lag of $\frac{\pi}{2}$ radians. Hence the two emf phasors may be plotted in the same phasor diagram along the negative y-axis, thus satisfying the phase lag of $\frac{\pi}{2}$ radians between the flux (ϕ) and emfs (E_1 and E_2), since in no-load condition there is no current flow in the secondary side so, $I_2 = 0$. The secondary 'emf' and secondary terminal voltage become equal which is shown in figure 'b'

$$\text{that is } \boxed{V_2 = E_2}$$

The primary current I_0 may be divided into two orthogonal components that is I_m & I_w . I_m represents magnetising component of I_0 which is the source

for the common flux (ϕ)

Hence ϕ and I_m remains in the same phase in other hand I_w represents the iron loss component or I_o ,

Such that $I_w \perp I_L$ and I_m order to locate primary (side) supply voltage V_1 , let us draw the induced emf E_1 in the opposite direction.

Then by adding the no-load voltage draw phasor along with the EMF phasor E_1 , we may find V_1 the mathematical expression for V_1 ,

$$V_1 = E_1 + I_o (R_1 + jX_1) \quad (11)$$

$$= E_1 + I_o R_1 + j I_o X_1$$

The angle between V_1 and I_o is no-load power factor angle ϕ_o whose power factor is $\cos \phi_o$. mathematically we may find some more relations from the no-load phasor diagram as given below.

Iron loss at no load

$$P_i = V_1 \times I_o \cos \phi_o \quad (12)$$

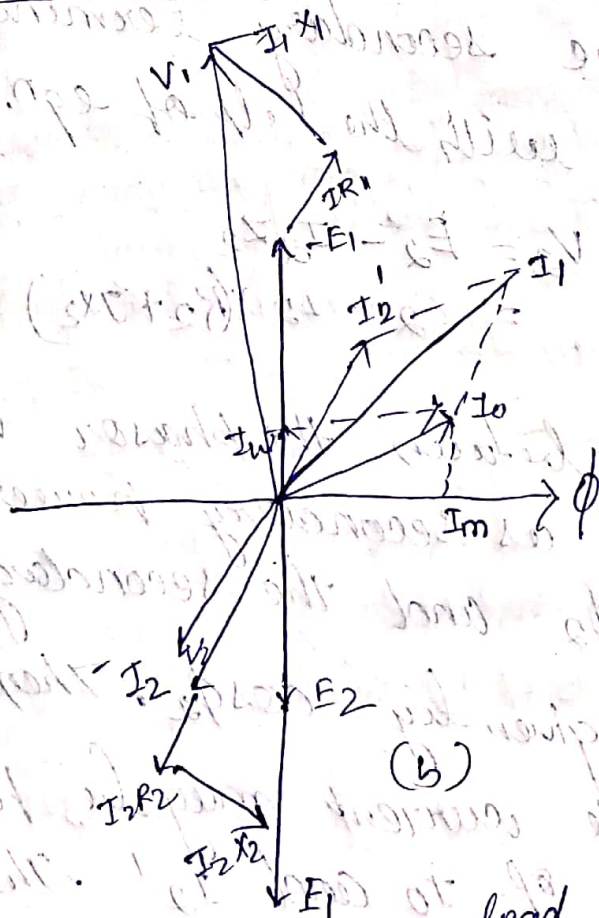
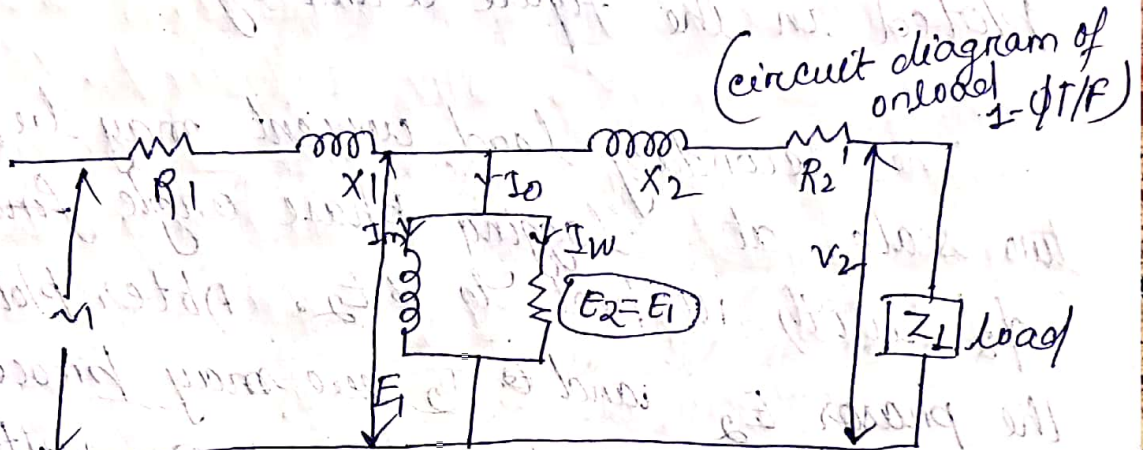
Loss component of no-load current

$$I_w = I_0 \cos \phi_0 \quad \text{--- (13)}$$

magnetising component of no-load current

$$I_m = I_0 \sin \phi_0 \quad \text{--- (14)}$$

On-load phasor diagram:



(phasor diagram of on load ϕ T/F)

Some portion of no-load phasor diagram remains unchanged in a load phasor diagram. The phasor which remains same in both the cases are the flux (ϕ) and the EMF's E_1 and E_2 which are plotted in the figure a and fig (b).

The secondary load current may be plotted two scale at lagging phase angle find ϕ_2' with respect to E_2 . After plotting the phasor E_2 and I_2 we may proceed to plot the secondary terminal voltage phasor V_2 with the help of eqn.

$$V_2 = E_2 - I_2 Z_2$$

$$= E_2 - I_2 (R_2 + jX_2) \quad \dots (15)$$

The angle between the phasor V_2 and I_2 is known as secondary power factor angle ϕ_2 and the secondary power factor is given by $\cos \phi_2$. Then the primary side current may be plotted with the help of I_0 and I_2' . The no-load current I_0 is plotted in the same way

by taking the resultant of I_m and I_w . However plotting of I_2' requires some understanding. I_2' represents the primary current which neutralize the demagnetizing effect of I_2 .

such that the relationship is given by

$$\frac{I_2'}{I_2} = K$$

$$\Rightarrow I_2' = KI_2 \quad \text{--- (16)}$$

Since I_2' and I_2 opposes each other by the principle, I_2' is to be plotted to scale on the opposite direction of I_2 .

Then the resultant of I_0 and I_2' may be plotted with the help of parallelogram law of phasor addition for obtaining primary current I_1 and satisfying the equation.

$$I_1 = I_0 + I_2' \quad \text{--- (17)}$$

In order to plot the primary voltage phasor V_1 the primary emf phasor E_1 may have to extended backward and then the primary winding voltage drop may be added with it because the expression for V_1 is the phasor sum of.

$$V_1 = E_1 + I_1 Z_1 \quad \text{--- (18)}$$

$$= E_1 + I_1 (R_1 + jX_1) \quad \text{--- (18)}$$

Finally the angle between the phasor V_1 & I_1 is known as primary power factor angle ϕ_1 , and the primary power factor is given by $\cos \phi_1$.

Q. The primary side of a transformer is connected to 230V, 50Hz supplied, if the no-load power consumption is 80 watt, what would be the magnetising current and loss current assume that no-load power factor is 0.8 lagging.

Ans: $I_m = I_0 \sin \phi_0$
 $I_w = I_0 \cos \phi_0$

given that $\cos \phi_0 = 0.8$

$P = V I_0 \cos \phi_0$

$\Rightarrow 80 = 230 \times I_0 \times 0.8$

$\Rightarrow 80 = 184 I_0$

$\Rightarrow \frac{80}{184} = I_0 \Rightarrow I_0 = 0.434 \text{ A}$

$I_m = I_0 \sin \phi_0$

$$\Rightarrow I_m = 0.434 \times \sqrt{1 - 0.64}$$

(magnetising current) $= 0.434 \times 0.6 = 0.2604$

$$I_w = 0.434 \times 0.8$$

$$= 0.3472$$

Voltage and current transformation Ratio:

$$\frac{V_2}{V_1} = \frac{N_2}{N_1} = \frac{E_2}{E_1} = \frac{I_1}{I_2} = k$$

It is clear that the volts per turns is exactly same for both the primary and secondary windings i.e. in any T/F secondary and primary induced emf are related to each other by the number of ratio of number of secondary and primary turns.

k is a constant called voltage transformation ratio of turns ratio.

for step up transform $V_2 > V_1$, In this case voltage transformation ratio ' k ' will be greater than 1 ($k > 1$)

for step down T/F, " $V_2 < V_1$ "

In this case $k < 1$

In an ideal T/F the losses are negligible (iron loss & copper loss). Volt ampere input to the primary and volt ampere output from secondary can be approximately equal to

$$\boxed{\text{Input} - \text{losses} = \text{output}}$$

When we considering ideal gas

$$\boxed{\text{output VA} = \text{Input VA}}$$

$$\Rightarrow V_2 I_2 = V_1 I_1$$

$$\boxed{\Rightarrow \frac{V_2}{V_1} = \frac{I_1}{I_2} = K}$$

$$\Rightarrow \frac{E_2}{E_1} = \frac{N_2}{N_1}$$

DC Machine:

dt. 15.11.19

DC machine is of two types
1) DC generator
2) DC motor

DC Generator:

It converts mechanical energy into electrical energy.

DC generator is of two types

1. Separately excited DC generator
2. Self excited DC generator.

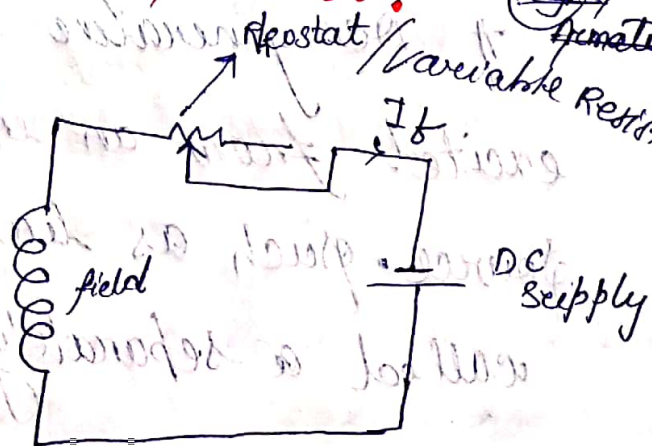
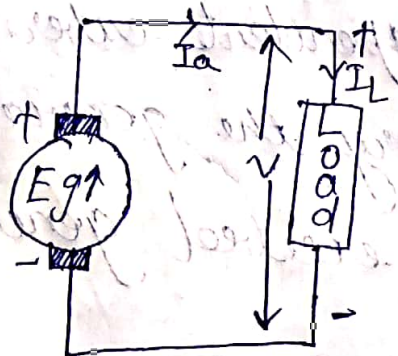
Self excited, also three types

1. series wound DC generator
2. ~~shunt~~ (parallel) wound DC generator,
3. compound wound DC generator.

Compound wound also two types,

1. short shunt
2. long shunt

Separately excited DC generator:



Eg - Generated EMF

$$I_a = I_L = I$$

$$E_g - I R_a - V = 0$$

$$\Rightarrow E_g - I R_a = V$$

$$\Rightarrow V = E_g - I_a R_a$$

E_g is the generated EMF

R_a is armature resistance

I_a is the armature current

V is the terminal voltage.

Power Develop. (P_g)

$$P_g = E_g \times I$$

power delivered to external load

$$P_L = V \times I$$

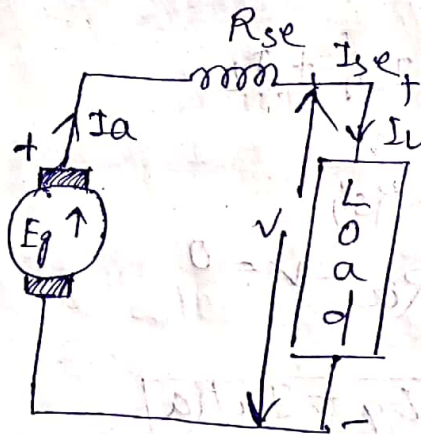
A DC generator whose field winding is excited from an independent external source, such as battery, the generator is called a separately excited generator

Self excited DC-generator:

A DC generator whose field winding is excited by the current supply or by the generator itself is called a self excited generator.

In such machines the field coils are either connected with the armature winding, the field coils may be connected either in series with the armature, or partly in series or partly in parallel with the armature.

Series wound generator:



$$I_a = I_{se} = I_l$$

$$E_g - I_a R_a - I_a R_{se} - V = 0$$

$$\Rightarrow E_g - I_a (R_a + R_{se}) - V = 0$$

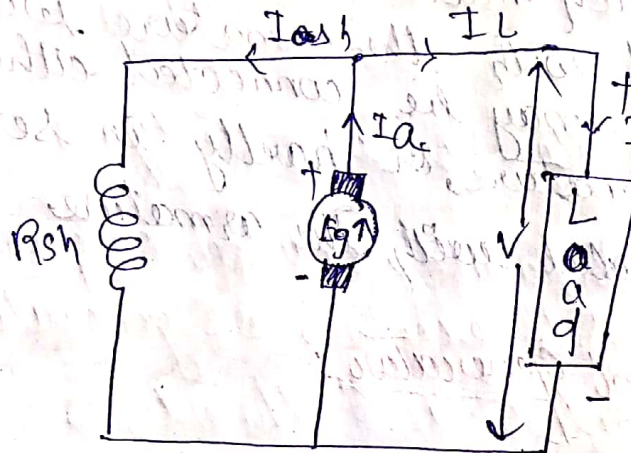
$$\boxed{\Rightarrow V = E_g - I_a (R_a + R_{se})}$$

* The resistance of series field winding R_{se} is very low which is equal to 0.5Ω .

Power developed $P_g = E_g \times I$

power delivered $= P_L = V \times I_L$

shunt
~~shunt~~ wound DC generator:



$$I_a = I_{sh} + I_L$$

$$I_{sh} = \frac{V}{R_{sh}}$$

$$E_g - I_a R_a - V = 0$$

$$\Rightarrow V = E_g - I_a R_a$$

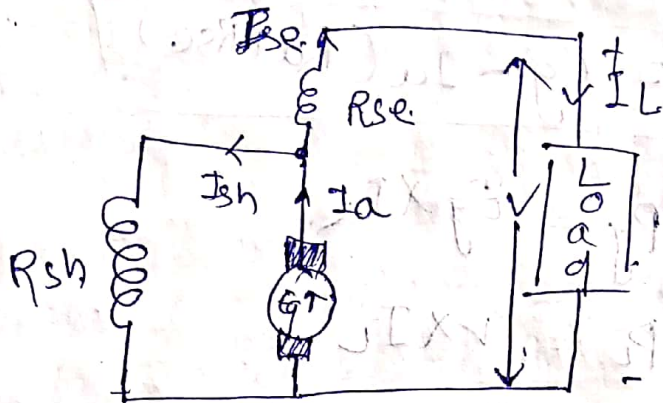
Power developed $P_g = E_g \times I_a$

Power delivered $= P_L = V \times I_L$

* The resistance of shunt field winding R_{sh} naturally very high, which is equal to 100Ω

Compound wound generator:

1. Short shunt



$$I_{se} = I_L$$

$$\Rightarrow I_a = I_{sh} + I_{se}$$

$$\Rightarrow I_{sh} = \frac{V - I_{se} R_{se}}{R_{sh}}$$

$$E_g - I_a R_a - I_{se} R_{se} = V = 0$$

$$\Rightarrow E_g - I_a R_a - I_{se} R_{se} = V$$

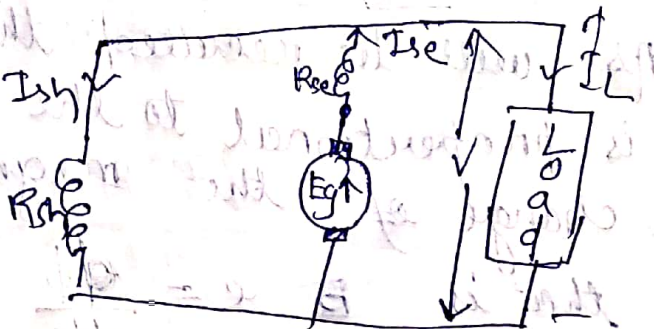
Power developed $P_g = E_g \times I_a$

Power delivered $P_L = V \times I_L$

2. Long shunt:

$$I_a = I_{se} = I_L + I_{sh}$$

$$I_{sh} = \frac{V}{R_{sh}}$$



$$E_g - I_a R_a - I_a R_{se} - V = 0$$

$$\Rightarrow V = E_g - I_a R_a - I_a R_{se}$$

$$\boxed{\Rightarrow V = E_g - I_a (R_a + R_{se})}$$

$$P_g = E_g \times I_a$$

$$P_L = V \times I_L$$

Resistance

Emf E_g of DC Generator:

Let ϕ be the flux per pole in webers
 z = the total number of armature conductors on coil sides on the armature

P = no. of poles

A = number of parallel paths in the armature

N = Rotational speed of the armature in RPM.

(measuring speed
 tachometer)

As will be recalled the induced emf is proportional to the time rate of change of the magnetic flux that is

$$e = \frac{d\phi}{dt}$$

~~using~~ during one revolution of armature in a two pole generator is armature conductor gets the magnetic flux p -times so flux cut by one conductor in one revolution is equals to ' $\pm\phi$ ' weber.

since the number of revolution made by the armature per minute is N so no. of revolutions made per second is $\frac{N}{60}$ and therefore flux cut by each conductor per second = flux cut by one conductor per revolution, into no. of revolution of armature per second,

$$N = T\phi \times \frac{N}{60} \text{ (weber)}$$

The average EMF induced in one conductor will be $e = T\phi \times \frac{N}{60}$

The number of conductors in series between a +ve brush and -ve brush is = $\frac{\text{the no. of conductors divided}}{\text{no. of parallel paths}}$

i.e. No. of Armature conductors per parallel path is

$$= \frac{Z}{A}$$

$$= \frac{Z}{P}$$

$$= \frac{Z}{2}$$

The total emf generated between the terminals $E =$ (Average emf induce in a one conductor) \times (No. of conductors in each circuit or parallel path)

$$= \left(T\phi \times \frac{N}{60} \right) \times \frac{Z}{A}$$

$$E = \frac{P\phi Z N}{60 A}$$

for wave winding = No. of parallel paths $A = 2$

Lap winding = No. of parallel paths $A = P$

Q. A 6 pole lap wound armature has 840 conductors and flux per pole is 0.018 wb. calculate the generated emf when the machine is running at 600 RPM.

Ans: Given data

$$\phi = 0.018 \text{ wb.}$$

$$Z = 840$$

$$N = 600 \text{ RPM}$$

$$E = 6$$

$$E = \frac{T\phi NZ}{60 \times A}$$

$$\Rightarrow 6 = \frac{T \times 0.018 \times 600 \times 840}{60 \times 62}$$

$$\Rightarrow \frac{6 \times 60 \times 2}{0.018 \times 600 \times 840} = T$$

$$\Rightarrow 0.08 = T$$

a. calculate the voltage induced in the armature winding of a 4 pole wave wound DC machine having 728 conductors and running at 1800 RPM. The flux per pole is 35 m web?

$$E = \frac{T \phi N Z}{60 A}$$

$$N = 1800 \text{ RPM}$$

$$\phi = 35 \times 10^{-3}$$

$$Z = 728$$

$$E = \frac{T \phi N Z}{60 A}$$

$$\Rightarrow 4 = \frac{T \times 35 \times 10^{-3} \times 1800 \times 728}{60 \times 2}$$

$$\Rightarrow \frac{4 \times 60 \times 2}{35 \times 10^{-3} \times 1800 \times 728} = T$$

$$\Rightarrow \frac{4800}{458640} =$$

DC Motor:

It converts electrical energy to mechanical energy.

Working principle of DC motor:

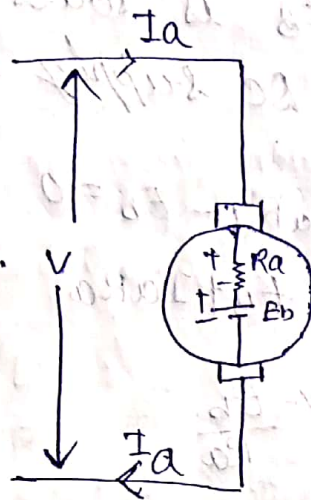
The principle upon which a DC motor works is very simple. If a current carrying conductor is placed in a magnetic field, mechanical force is experienced on the conductor. The direction of which is given by Fleming's left hand rule (also called motor rule) and hence the conductor moves in the direction of force. The magnitude of mechanical force experienced of the conductor is given by $F = BIl$

'B' is the field strength (wb/m^2 or T)

'I' is the current flowing through the conductor (Ampere)

'l' is the length of conductor (m)

Importants of back Emf: E_b



Applying KVL

$$V = I_a R_a + E_b$$

When the motor armature continues to rotate due to motor action the armature conductors cut the magnetic flux and therefore emfs are induced. The direction of this induced emf known as back emf, such that it opposes the applied voltage.

Since the back emf is induced due to the generator action, the magnitude of back emf is, therefore given by the same expression as that for the generated emf in a generator

$$E_b = I_a R_a + E_b$$

$$E_b = \frac{P \phi N Z}{60 A}$$

The armature circuit is equivalent to a source EMF, E_b is series ^{with} a resistance R_a across a DC supply main voltage 'V'.

$$V - I_a R_a - E_b = 0$$

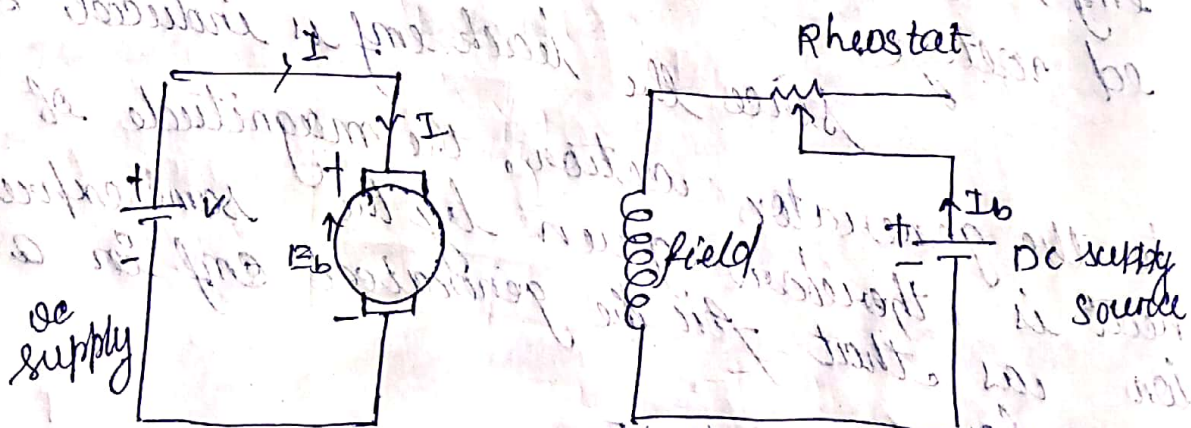
$$\Rightarrow V = E_b + I_a R_a$$

$$I_a = \frac{V - E_b}{R_a}$$

Types of DC motor:

- 1) Separately excited DC motor.
- 2) Shunt excited DC motor.

Separately excited DC Motor:



$$V - I_a R_a - E_b = 0$$

$$\Rightarrow V = I_a R_a + E_b$$

power drawn from supply mains:

$$P = VI$$

mechanical power developed

$P_m =$ Power input to the armature - power loss to armature

$$= VI - I^2 R_a$$

$$= I(V - I R_a)$$

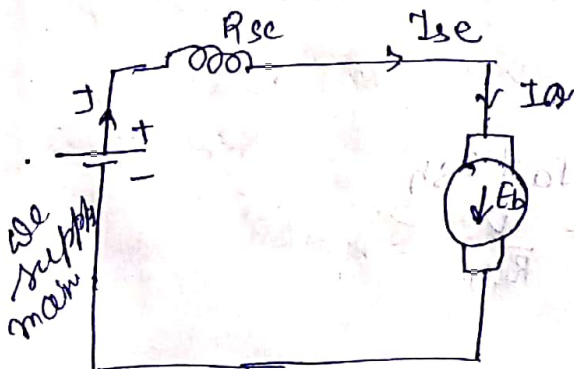
$$= I E_b$$

REMEMBER

$$P_m = E_b I_a$$

Shelf excited DC Motor:

Series wound DC motor:



$$I = I_a$$

$$V - I_a R_{se} - I_a R_a - E_b = 0$$

$$\Rightarrow V = I_a R_{se} + I_a R_a + E_b$$

$$\Rightarrow V = I_a (R_{se} + R_a) + E_b$$

$$V = E_b + I_a (R_{se} + R_a)$$

power drawn from the supply mains = $V I_a$
 mechanical power developed P_m .

→ Power input - losses in armature field

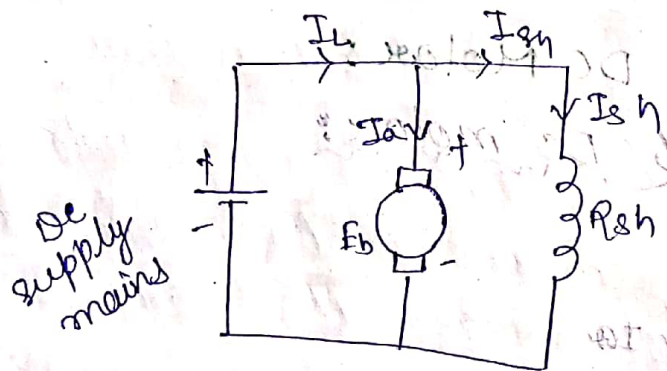
$$\Rightarrow V I_a - I_a^2 (R_a + R_{se})$$

$$\Rightarrow I_a (V - I_a (R_a + R_{se}))$$

$$\Rightarrow I_a E_b$$

$$\Rightarrow E_b I_a - I_a^2 R_a$$

shunt wound DC motor:



$$I_L = I_a + I_{sh}$$

$$I_{sh} = \frac{V}{R_{sh}}$$

$$V - I_a R_a = E_b = 0$$

$$\Rightarrow V = E_b + I_a R_a$$

$$P = V I_L = V (I_a + I_{sh})$$

$$P = V I_a + V I_{sh} = V I_a + \frac{V^2}{R_{sh}}$$

mechanical power developed =
 power input - losses in armature and field

$$VI_a - I_a^2 (R_a + R_{se})$$

$$= VI_L - VI_{sh} - I_a^2 R_a$$

$$= V(I_L - I_{sh}) - I_a^2 R_a$$

$$= VI_a - I_a^2 R_a$$

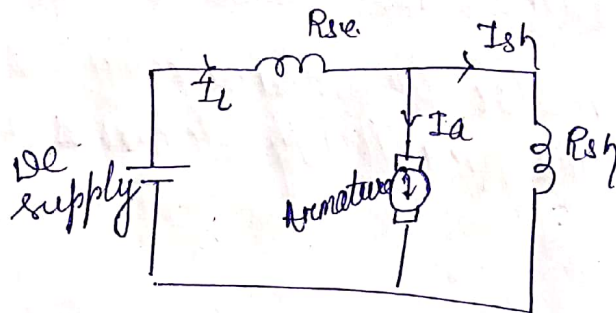
$$= I_a (V - I_a R_a)$$

$$= I_a E_b$$

compound wound DC motor:

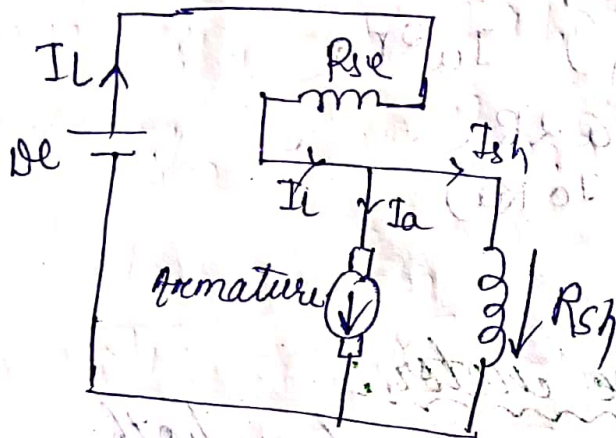
A compound DC motor has both series field coils. compound wound motors are of two types namely cumulative compound wound and differential compound wound motors.

cumulative compound wound motor:



A cumulative compound motor is one in which the field windings are connected in such a way that direction of flow current of flow is same in both of the field windings.

Differential compound wound motor:



In this motor in which the field windings are connected in such a way that the direction of flow of current is opposite to each other in the two field windings.

speed equation

from the emf equation of dc motor we got that $E_b = \frac{P\phi Nz}{60A}$ --- (1)

from the KVL we got the eqn,

$$V - I_a R_a - E_b = 0$$

$$\Rightarrow E_b = V - I_a R_a \text{ --- (2)}$$

Now comparing eqn. no. (1) & eqn. (2)...

$$\frac{P\phi Nz}{60A} = V - I_a R_a$$

$$\Rightarrow N = \frac{(V - I_a R_a) 60A}{P\phi z}$$

$$\Rightarrow N = k \frac{(V - I_a R_a)}{\phi}$$

(since z, A, P are constant for a particular machine)

$$\Rightarrow N \propto k \frac{E_b}{\phi}$$

$$\Rightarrow N = k \frac{E_b}{\phi} \text{ (where } k \text{ is a constant)}$$

In a dc motor if initial values of speed, armature current, back emf or flux per pole are N_1, I_{a1}, E_{b1} and ϕ_1 respectively and corresponding final values are N_2, I_{a2}, E_{b2} and ϕ_2 respectively.

Then $N_1 \propto \frac{E_{b1}}{\phi_1}$

$N_2 \propto \frac{E_{b2}}{\phi_2}$

where $E_{b1} = V - I_{a1}R_a$

$E_{b2} = V - I_{a2}R_a$

$\Rightarrow \frac{N_2}{N_1} = \frac{E_{b2}}{\phi_2} = \frac{E_{b2}}{\phi_2} \times \frac{\phi_1}{E_{b1}}$

$\frac{E_{b1}}{\phi_1} = \frac{E_{b2}}{E_{b1}} \times \frac{\phi_1}{\phi_2}$

REMEMBER

$\Rightarrow \frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}} \times \frac{\phi_1}{\phi_2}$

for DC shunt motor or separately excited DC motor, flux practically remains constant

$\phi_2 = \phi_1$

$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$

REMEMBER

$\frac{N_2}{N_1} = \frac{V - I_{a2}R_a}{V - I_{a1}R_a}$

In the above expression since the applied voltage V is constant and the voltage drop in the armature ($I_a R_a$) is negligible in comparison to the supply voltage V .

Imp: Pt:
Speed of a DC motor remains almost constant.

for a DC series motor, prior to saturation $\phi \propto I_a$

$$\Rightarrow \frac{\phi_1}{\phi_2} = \frac{I_{a1}}{I_{a2}}$$

REMEMBER

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}} \times \frac{I_{a1}}{I_{a2}}$$

FOR DC series motor after saturation:

flux is independent of armature current I_a so $N \propto E_b$

$$\Rightarrow \frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

Armature Torque Equation:

Let T_e electromagnetic torque developed in Nm by the motor running at N RPS, so power developed equals to work done per second = $T_e \omega$ --- (1)

$$\omega = \frac{2\pi n}{60}$$

Electrical equivalent of mechanical power develop by the armature = $E_b I_a$ - (2)

comparing eqn (1) & (2)

$$T_e \omega = E_b I_a$$

$$\Rightarrow T_e \frac{2\pi N}{60} = E_b I_a$$

$$\Rightarrow T_e = \frac{E_b I_a \times 60}{2\pi N}$$

$$\approx \frac{E_b I_a \times 90}{3.14 \times N}$$

$$T_e = 9.55 \frac{E_b I_a}{N} \quad (3)$$

Now substituting the value of $E_b = \frac{P \phi N Z}{60 A}$

$$T_e = 9.55 \times \frac{P \phi N Z}{60 A} \times I_a$$

$$= 0.159 \frac{P \phi Z I_a}{A}$$

Induction Motor:

Introduction to three phase induction motors, Three phase induction motors form the major section almost more than 90% of industrial drives because of its inherent advantages. In the family of AC motors three phase induction motors are self starting and they also have the simplest construction as a result it requires very less maintenance and keeps almost trouble with service. It has also higher efficiency compared to DC and synchronous motors and operates at a reasonable good power factor.

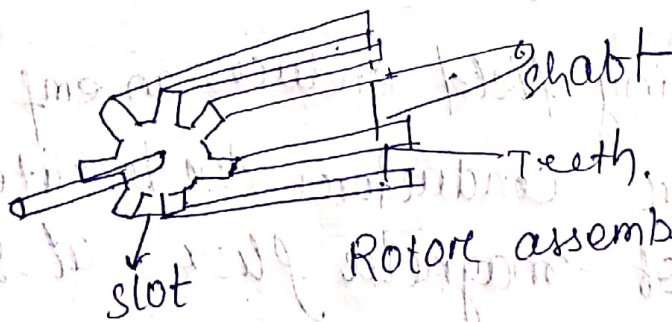
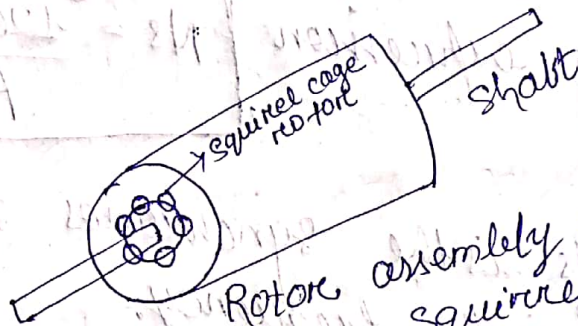
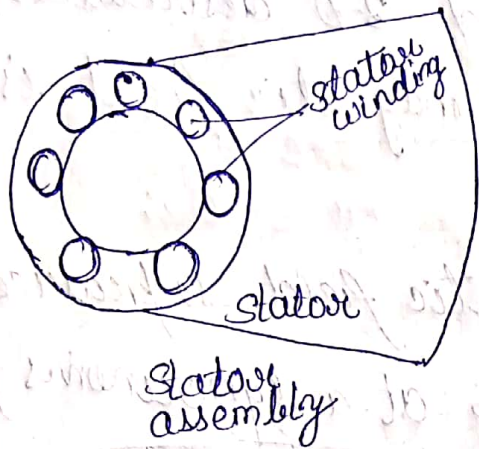
Induction motor have a rotating part called rotor and a stationary part called stator. The stator consist of a cylindrical frame called Yoke. The yoke is used as a support for the stator core. The stator core is slotted hollow cylinder that houses a three phase balanced star connected windings with provision to feed a balanced three phase AC supplied to the stator winding in the

hollow space the stator core the rotor assembly is carefully mounted with the help of an axial-shaft and ball bearing arrangement. The shaft along with the rotor assembly is then rotated by maintaining a uniform air gap throughout.

Depending upon the type of winding used in the rotor three phase induction motors may be classified as

1. Squirrel cage induction motor.
- a. Wound rotor or slip ring induction motor.

A squirrel cage rotor has short circuited conductors round the periphery of the rotor which resemble a squirrel cage on the other hand a wound rotor has a balanced three phase winding similar to stator winding.



The principle operation of 3- ϕ induction motor:

when a balanced 3- ϕ supply is given to a balanced 3- ϕ distributed windings a rotating magnetic field is developed.

The magnetic field so produced revolves in the air gap at a synchronous field given by expression

$$N_s = \frac{120f}{P} \text{ rpm}$$

N_s is the synchronous speed
 f is the frequency.

P is the number of poles in the stator winding.

The rotating field induces an emf in the rotor conductors due to rate of change of magnetic flux. At standstill position of the rotor maximum emf is induced as rate of change of flux linkage is a function of the relative motion between the rotating field

and the rotor conductors.

Relative speed or slip speed = $(N_s - N_r)$ RPM
 $N_r = \text{Rotor speed}$

concept of slip:

slip indicates the relative speed of a motor with respect to the synchronous speed of rotating magnetic field of this stator. Express in % of per unit ratio of N_s

Slip is denoted by a symbol 's' and it has no unit.

$$s = \frac{N_s - N_r}{N_s} \text{ in pu}$$

$$\% \text{ of } s = \frac{N_s - N_r}{N_s} \times 100$$

slip at stand still (constant)

when the motor remains in stand still condition it has a still rotor

hence $N_r = 0$
 $s = 1 \text{ pu}$

Slip & Synchronous speed:

When the motor approaches the synchronous speed the rotor speed becomes equal to the synchronous speed so

$$N_R = N_s$$

$$s = 0 \text{ pu}$$

$$\text{or } s = 0 \%$$