

INTRODUCTION:-

- > Fluid mechanic is the branch of science which deals with behaviour of fluid at rest as usual as in motion.
- > Thus, this branch of science deals with static kinematic and dynamic aspects of fluid.
- > The study of fluid at rest is called fluid static.
- > The study of fluid in motion press force are not considered is called fluid kinematics.
- > If the press force is also considered for fluid in motion that branch of science is called fluid dynamics.

Properties of fluid:-

Density / mass density:-

- > Density or mass density of fluid is defined as the ratio of the mass of the fluid to the volume.
- > Thus, the mass per unit volume is called density.
- > It is denoted by the symbol ρ or ρ .
- > The unit of mass density in SI unit is kg/m^3 .
- > Mathematically mass density is written as ρ .

$$\rho = \frac{\text{mass of fluid}}{\text{volume of fluid}}$$

-> Density of water is 1000 kg/m^3 or 1 gm/cm^3 .

Specific weight / weight density:-

- > Specific weight or weight density of fluid is the ratio between the weight of the fluid in the ratio bet to its volume.
- > Thus weight per unit volume of fluid is called weight density.
- > It is denoted by the symbol w .

$$w = \frac{\text{weight of fluid}}{\text{volume of fluid}}$$

$$= \frac{\text{mass of fluid} \times \text{acceleration due to gravity}}{\text{volume of fluid}}$$

$$= \frac{\text{mass of fluid} \times g}{\text{volume of fluid}}$$

$$= \frac{\text{mass of fluid}}{\text{volume of fluid}} = \rho$$

Specific volume :-

→ Specific volume of fluid is defined as the volume of the fluid occupied by unit mass or volume per unit mass of fluid is called specific volume.

→ Mathematically is expressed as

$$= \frac{\text{volume of fluid}}{\text{mass of fluid}}$$

$$= \frac{1/\text{mass of fluid}}{\text{volume of fluid}}$$

$$= 1/\rho$$

→ Specific volume is the reciprocal of mass density.

→ It is expressed as m^3/kg .

Specific gravity :-

→ Specific gravity is defined as the ratio of weight density of fluid to the weight of standard fluid.

→ For liquid the standard fluid is taken as water.

And for gases the standard fluid is taken as air.

→ Specific gravity is also called as relative density.

→ It is dimensionless quantity and it is denoted by symbol S_g .

→ Mathematically for liquid

$$S_g = \frac{\text{weight density of liquid}}{\text{weight density of water}}$$

Similarly for gases

$$S_g = \frac{\text{weight density of gases}}{\text{weight density of air}}$$

$$\begin{aligned} \text{weight density of liquid} &= S \times \text{weight of water} \\ &= S \times 1000 \times 9.81 \text{ N/m}^3 \\ &= S \times 1000 \text{ kg/m}^3 \end{aligned}$$

Problem-1

Calculate the specific weight density and specific gravity of 1L liquid which weight 7N.

$$A:- \text{1L} = \frac{1}{1000} \text{ m}^3$$

weight per volume 7000 N/m^3

$$\text{density} = w/g$$

$$= \frac{7000}{9.81}$$

$$= 713.5 \text{ kg/m}^3$$

$$\text{specific gravity} = 713.5 \times 1000$$

$$= 0.7135 \text{ kg/m}^3$$

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Problem-2

Calculate the density specific weight and weight of 1L of petrol of specific gravity 0.7.

$$A:- \text{1L} = \frac{1}{1000} \text{ m}^3 = 0.001 \text{ m}^3$$

$$\begin{aligned} S &= 0.7 \times 1000 \\ &= 700 \text{ kg/m}^3 \end{aligned}$$

$$\begin{aligned} \text{specific weight} &= 700 \times 9.81 \\ &= 6867 \text{ kg/m}^3 \end{aligned}$$

$$w = \frac{W}{V}$$

$$6867 = \frac{W}{0.001}$$

$$W = 6867 \times 0.001$$

$$= 6.867 \text{ kg/m}^3$$

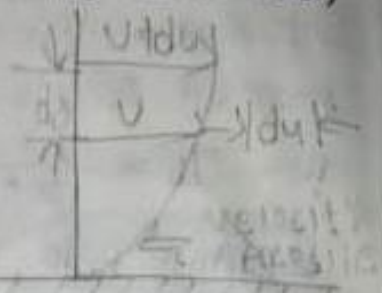
viscosity :-

viscosity is defined as the property of fluid which offers resistance to the movement of layers of fluid over other adjacent layers of fluid.

Example :- oil flows in water.

→ when two layers of fluid, a distance dy apart move one over the other at different velocity u to $u + du$, the viscosity together with relative velocity causes a sheare stress acting between the fluid layers.

→ The top layer causes sheare stress on the adjacent lower layer while the lower layer causes a sheare stress on the adjacent top layer.



This sheare stress is proportional to rate of change of velocity with respect to y . It is denoted by symbol τ .

$$\tau \propto \frac{du}{dy} \quad \tau = \mu \frac{du}{dy}$$

→ μ is the constant of the proportions and it is known as coefficient of dynamic viscosity or only viscosity.

→ $\frac{du}{dy}$ represents the rate of sheare strain or velocity gradient.

$$\mu = \frac{\tau}{\left(\frac{du}{dy}\right)}$$

Unit of viscosity :-

$$\mu = \frac{\tau}{\frac{du}{dy}}$$

$$\mu = \frac{\text{sheare stress}}{\frac{\text{change in velocity}}{\text{change in distance}}}$$

$$\begin{aligned} \mu &= \frac{F/A}{\frac{\text{length}}{\text{time}} \times \frac{1}{\text{length}}} \\ &= \frac{F/l^2}{1/\text{time}} \end{aligned}$$

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$$= \frac{\text{force} \times \text{time}}{l^2}$$

$$\left[\frac{\text{kg} \cdot \text{m} \cdot \text{sec}}{\text{m}^2} \right]$$

(MKS unit of viscosity)

Cgs unit of viscosity

$$\left[\frac{\text{dyne} \cdot \text{sec}}{\text{cm}^2} \right]$$

SI unit of viscosity

$$\left[\frac{\text{N} \cdot \text{sec}}{\text{m}^2} \right]$$

Numerical conversion of unit of viscosity from MKS unit to Cgs.

$$A:- \frac{1 \text{ kg} \cdot \text{m} \cdot \text{sec}}{\text{m}^2} = \frac{9.81 \text{ N} \cdot \text{sec}}{\text{m}^2}$$

$$\text{But } 1 \text{ Newton} = 1 \text{ kg}$$

$$1 \text{ N} = \frac{1000 \text{ g} \times 100 \text{ cm}}{\text{sec}^2}$$

$$= \frac{1000 \times 100 \text{ g} \cdot \text{cm}}{\text{sec}^2}$$

$$= \frac{1000 \times 1000 \text{ dyne}}{\text{sec}^2}$$

$$\left(\frac{\text{m} \cdot \text{m}}{\text{sec}^2} \right)$$

(acceleration)

Therefore

$$\frac{1 \text{ kg} \cdot \text{m} \cdot \text{sec}}{\text{m}^2} = \frac{9.81 \times 100000 \text{ dyne} \cdot \text{sec}}{\text{cm}^2}$$

Newton laws of viscosity:-

It's state that sheare stress of fluid element layers is directly proportion to rate of sheare strain. The constant proportionality is called coefficient of viscosity

$$\left[\mu = \frac{\tau}{\frac{dv}{dy}} \right]$$

→ Fluid is obey the above relation are known as Newtonian fluid whereas as fluid is not obey the above relation are known as Non-Newtonian fluid.

Problem-3

velocity distribution over a plate is given by $u = \frac{2}{3}y - y^2$, in which u is velocity in m./sec at a distance y m above the plate. Determine the shear stress at $y=0$, $y=0.15$ take dynamic viscosity of fluid as 8.63 Poise.

Ans → Given data: $u = \frac{2}{3}y - y^2$

$$\mu = 8.63 \text{ Poise} = \frac{8.63}{10} = 0.863 \text{ NS/m}^2$$

$$y = 0$$

$$y = 0.15$$

$$\tau = \mu \frac{du}{dy}$$

at $y=0$

$$\tau = \mu \frac{du}{dy}$$

$$\frac{d}{dy} \left(\frac{2}{3}y - y^2 \right)$$

$$\frac{2}{3} - 2y$$

$$= \frac{2}{3} - 2 \times 0$$

$$= \frac{2}{3}$$

$$\tau = \mu \frac{du}{dy}$$

$$= 0.863 \times \frac{2}{3}$$

$$= 0.575$$

at $y=0.15$

$$\tau = \mu \frac{du}{dy}$$

$$= 0.863 \times \frac{2/3 - 2 \times 0.15}{0.15}$$

$$= 0.13$$

Problem-4

A plate 0.025mm distance from a fixed plate moves at 60cm/s and requires a force of 2N/m² unit area to maintain the speed. Determine the viscosity between the plate.

A:- given data:- $dy = 0.025 \text{ mm} = 0.025 \times 10^{-3}$

$$\tau \text{ force} = 2 \text{ N/m}^2$$

$$v = 60 \text{ cm/sec} = 0.6 \text{ m/sec.}$$

$$\mu = \frac{\tau}{\frac{dy}{dx}}$$

$$\tau = \mu \frac{dy}{dx}$$

$$dy = 0.6$$

$$\mu = \frac{\tau}{\frac{dy}{dx}}$$

$$= \frac{2}{\frac{0.6}{0.025}}$$

$$= 0.08 \text{ m/sec}^2$$

Problem-5

Find the kinematic viscosity of an oil having density 981 kg/m³. The sheare stress at a point in oil is 0.02452 N/m² and the velocity gradient point 0.2.

$$\text{kinematic} = \nu = \frac{\mu}{\rho}$$

A:- given data:- $\rho = 981 \text{ kg/m}^3$

$$\frac{dy}{dx} = 0.2$$

$$\tau = 0.02452 \text{ N/m}^2$$

Problem-4

A plate 0.025mm distance from a fixed plate moves at 60cm/s and requires a force of 2N/m² unit area 2N/m² to maintain the speed. Determine the viscosity between the plate.

A:- given data:- $dy = 0.025 \text{ mm} = 0.025 \times 10^{-3}$

$$\tau \text{ force} = 2 \text{ N/m}^2$$

$$v = 60 \text{ cm/sec} = 0.6 \text{ m/sec.}$$

$$\mu = \frac{\tau}{\frac{dv}{dy}}$$

$$\tau = \mu \frac{dv}{dy}$$

$$dv = 0.6$$

$$\mu = \frac{\tau}{\frac{dv}{dy}}$$

$$= \frac{2}{\frac{0.6}{0.025}}$$

$$= 0.08 \text{ m/sec}^2$$

Problem-5

Find the kinematic viscosity of an oil having density 981 kg/m³. The sheare stress at a point in oil is 0.02452 N/m² and the velocity gradient at point 0.2.

$$\text{kinematic} = \nu = \frac{\mu}{\rho}$$

A:- given data:- $\rho = 981 \text{ kg/m}^3$

$$\frac{dv}{dy} = 0.2$$

$$\tau = 0.02452 \text{ N/m}^2$$

$$\begin{aligned} \tau &= \frac{\mu}{\rho} \\ &= \frac{1.226}{981} \\ &= 1.24 \times 10^{-3} \text{ m}^2/\text{s} \end{aligned}$$

$$\begin{aligned} \mu &= \frac{\tau}{\frac{dy}{dy}} \\ &= \frac{0.2432}{0.2} \\ &= 1.226 \text{ N/m}^2 \end{aligned}$$

Problem-6

The dynamic viscosity of oil used for lubrication between a shaft and sleeve is 6 Poise. The shaft is diameter 0.4m and rotate at 190 rpm. calculate the power lost in bearing for a sleeve length of 90mm.

The thickness of oil film 1.5m.



Al- given data:-

$$\mu = 6 \text{ Poise} = \frac{6}{10} = 0.6 \text{ N sec/m}^2$$

$$D = 0.4 \text{ m}$$

$$N = 190 \text{ rpm.}$$

$$L = 90 \text{ mm} = 90 \times 10^{-3} \text{ m.}$$

$$t = 1.5 \text{ mm} = 1.5 \times 10^{-3} \text{ m.}$$

$$\tau = \mu \cdot \frac{dy}{dy}$$

$$dy = \mu \cdot \theta$$

$$\mu = \frac{\tau \cdot L}{\theta}$$

$$= \frac{\pi \cdot 0.4 \cdot 190}{60}$$

$$= 3.97 \text{ m/s.}$$

$$dy = 1.5 \times 10^{-3}$$

$$\tau = \mu \frac{du}{dy}$$

$$= 0.6 \frac{3.97}{1.5 \times 10^{-3}}$$

$$= 1588$$

$$F = \tau \times A$$

$$= 1588 \times 0.11$$

$$= 174.68$$

$$T = F \times \frac{D}{2}$$

$$= 174.68 \times \frac{0.4}{2}$$

$$= 34.93$$

$$P = \frac{2\pi NT}{60}$$

$$= \frac{2 \times \pi \times 190 \times 34.93}{60}$$

$$= 694.99$$

$$A = \pi DL$$

$$= \pi \times 0.4 \times 90 \times 10^{-3}$$

$$= 0.11$$

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Problem-7

A newtonian fluid is filled with clearness between a shaft & concentric sleeve the sleeve attendance a speed of 500 m/sec when a force of 40N is applied to sleeve parallel to the shaft determine the speed if a force of 200N is applied.

A:- Given data:- $F = 40N$
 $U = 500m/sec$

$$\tau = \frac{F}{A}$$

$$\tau = \mu \frac{du}{dy}$$

$$\frac{F}{A} = \mu \left(\frac{U}{y} \right)$$

$$F = \frac{\mu U}{y}$$

$$F \propto U$$

$$\frac{du}{dy} = \frac{U}{y}$$

$$\frac{F_1}{V_1} = \frac{F_2}{V_2}$$

$$\frac{40}{60} = \frac{200}{V_2}$$

$$V_2 = \frac{200 \times 60}{40} = 300 \text{ cm/sec}$$

Problem 8

2 large plain surface are 2.4 cm apart the space between the surface is filled with glycerine the force is required to drag a very thin plate of surface area 0.5 sqm between the two large plain surface at a speed of 0.6 m/sec. If i) A thin plate is in the middle of 2 plain surface ii) The thin plate is at a distance of 0.8 cm from one of plain surface. the dynamic viscosity of glycerine = $8.1 \times 10^{-1} \frac{\text{N sec}}{\text{m}^2}$.

Given data:- $dy = 2.4 \text{ cm}$

$$A = 0.5 \text{ sqm}$$

$$dy = 0.6 \text{ m/sec}$$

$$\mu = 8.1 \times 10^{-1} \frac{\text{N sec}}{\text{m}^2}$$

i) $F_1 =$ sheare force on the upper side of thin plate

$F_2 =$ sheare force on the lower side of thin plate

$F =$ Total force required to drag the plate.

$$F = F_1 + F_2$$

$$\tau_1 = \frac{F_1}{A_1}$$

$$\tau_1 = \mu \left(\frac{du}{dy} \right)_1$$

$$du = 0.6 \text{ m/SEC}$$

$$dy = 0.012 \text{ m}$$

$$\tau_1 = 8.1 \times 10^{-1} \left(\frac{0.6}{0.012} \right)_1$$
$$= 40.5 \text{ N/m}^2$$

$$f_1 = \tau_1 \times A_1$$

$$= 40.5 \times 0.5$$

$$= 20.25$$

$$f_2 = \tau_2 \times A_2 = 20.25$$

$$\text{Total stress} = f_1 + f_2$$

$$= 20.25 + 20.25$$
$$= 40.5 \text{ N}$$

ii) f_1 = shear force on the upper side of thin plate.

f_2 = shear force on the lower side of thin plate.

f = total force required to drag the plate.

$$f = f_1 + f_2$$

$$\tau_1 = \frac{f_1}{A_1}$$

$$\tau_1 = \mu \left(\frac{du}{dy} \right)_1$$

$$du = 0.6 \text{ m/SEC}$$

$$dy = 8 \times 10^{-3} \text{ m}$$

$$\tau_1 = 8.1 \times 10^{-1} \left(\frac{0.6}{8 \times 10^{-3}} \right)_1$$

$$= 60.75 \text{ N/m}^2$$

$$f_1 = \tau_1 \times A_1$$

$$= 60.75 \times 0.5$$

$$= 30.375$$

$$\tau_1 = \mu \left(\frac{dy}{dx} \right)_1$$

$$dy = 0.6 \text{ m/sec}$$

$$dx = 0.012 \text{ m}$$

$$\tau_1 = 8.1 \times 10^{-1} \left(\frac{0.6}{0.012} \right)_1$$

$$= 40.5 \text{ N/m}^2$$

$$F_1 = \tau_1 \times A_1$$

$$= 40.5 \times 0.5$$

$$= 20.25$$

$$F_2 = \tau_2 \times A_2 = 20.25$$

$$\text{Total stress} = F_1 + F_2$$

$$= 20.25 + 20.25$$

$$= 40.5 \text{ N}$$

ii) F_1 = shear force on the upper side of thin plate.

F_2 = shear force on the lower side of thin plate.

F = Total force required to drag the plate.

$$F = F_1 + F_2$$

$$\tau_1 = \frac{F_1}{A_1}$$

$$\tau_1 = \mu \left(\frac{dy}{dx} \right)_1$$

$$dy = 0.6 \text{ m/sec}$$

$$dx = 8 \times 10^{-3} \text{ m}$$

$$\tau_1 = 8.1 \times 10^{-1} \left(\frac{0.6}{8 \times 10^{-3}} \right)_1$$

$$= 60.75 \text{ N/m}^2$$

$$F_1 = \tau_1 \times A_1$$

$$= 60.75 \times 0.5$$

$$= 30.375$$

$$dy = 0.6 \text{ m/s}^2$$

$$dy = 1.6 \text{ cm} = \frac{1.6}{100} = 0.016 \text{ m}$$

$$\tau_2 = \mu \left(\frac{dy}{dx} \right)_1$$

$$= 8.1 \times 10^{-1} \left(\frac{0.6}{0.0166} \right)_1$$

$$= 30.375$$

$$F_2 = \tau_2 \times A_2$$

$$= 30.375 \times 0.5$$

$$= 15.1875 \quad F_1 + F_2$$

$$\text{Total Stress} = 30.375 + 15.1875$$

$$= 45.5625 \text{ N}$$

Surface tension :-

Surface tension is defined as the tensile force acting on the surface of liquid in contact with gas or 2 immiscible liquid such that the contact surface behaves like membrane under tension.

∴ The magnitude of this force per unit length of free surface is known as surface tension. It is denoted by σ .

$$\sigma = \frac{F}{L}$$

CGS unit will be kgf/m . and SI unit N/m .

The phenomenon of surface tension is explained consider 3 molecules A, B, C of liquid.

∴ The molecule A is attracted in all directions ^{by} the surrounding molecules of liquid.

FREE SURFACE



$$\tau_1 = \mu \left(\frac{du}{dy} \right)_1$$

$$du = 0.6 \text{ m/SEC}$$

$$dy = 0.012 \text{ m}$$

$$\tau_1 = 8.1 \times 10^{-1} \left(\frac{0.6}{0.012} \right)_1$$
$$= 40.5 \text{ N/m}^2$$

$$F_1 = \tau_1 \times A_1$$

$$= 40.5 \times 0.5$$

$$= 20.25$$

$$F_2 = \tau_2 \times A_2 = 20.25$$

$$\text{Total stress} = F_1 + F_2$$

$$= 20.25 + 20.25$$

$$= 40.5 \text{ N}$$

ii) F_1 = shear force on the upper side of thin plate.

F_2 = shear force on the lower side of thin plate.

F = total force required to drag the plate.

$$F = F_1 + F_2$$

$$\tau_1 = \frac{F_1}{A_1}$$

$$\tau_1 = \mu \left(\frac{du}{dy} \right)_1$$

$$du = 0.6 \text{ m/SEC}$$

$$dy = 8 \times 10^{-3} \text{ m}$$

$$\tau_1 = 8.1 \times 10^{-1} \left(\frac{0.6}{8 \times 10^{-3}} \right)_1$$

$$= 60.75 \text{ N/m}^2$$

$$F_1 = \tau_1 \times A_1$$

$$= 60.75 \times 0.5$$

$$= 30.375$$

The net resultant force acting on molecule A is 0.

i) But the molecule B which is situated near the free surface is acted upon the upward & downward forces which are unbalanced. Thus, net resultant force acting on B is in downward direction.

ii) The molecule C situated free surface of liquid does experience a resultant downward force all the molecules free surface experience a downward force.

iii) Thus the free surface of a liquid act like very thin film under tension on the surface of liquid act as though it is elastic membrane under tension.

Surface tension liquid on "Plate":-

Consider a spherical drawplate of radius r on the entire surface of the drawplate the tensile force due to surface tension will be acting.

σ = surface tension of liquid
 P = Pressure inside the liquid draw plate.

d = dia of draw plate

Let the drawplate is cut into 2 halves the force acting on $\frac{1}{2} = \sigma \times \text{circumference}$.

$$\sigma \times \pi d$$

Pressure force on the area = $P \times \frac{\pi d^2}{4}$



$$\sigma = \frac{F}{L}$$

$$F = \sigma \times \pi d$$

$$P \times \frac{\pi}{4} d^2 = \sigma \times \pi d$$

$$= \frac{4\sigma}{d}$$

Surface tension on hollow bubbles:-

A hollow bubble or soap bubble in air has 2 surfaces in contact with air 1 inside or other outside. Thus 2 surface are subjected to surface tension in such case we have

$$P \times \frac{\pi}{4} d^2 = 2(\sigma \times \pi d)$$

$$P = \frac{2(\sigma \times \pi d)}{\frac{\pi d^2}{4}}$$

$$= \frac{8\sigma}{d}$$

Problem-9

The surface tension of water in contact with air at 20°C is 0.0725 N/m. The pressure inside a drop plate of water is to be 0.02 N/cm² greater than outside pressure calculate the diameter of calculate of drop plate water

A:- ~~surface~~ ^{given} data:- surface tension

$$\sigma = 0.0725 \text{ N/m}$$

$$\text{(outside) } P = 0.02 \text{ N/cm}^2$$

$$= 2 \times 10^{-4} \text{ N/m}^2$$

$$P = \frac{4\sigma}{d}$$

$$0.1032 = \frac{8 \times 0.0725}{\pi \times 0.04}$$

$$P = \frac{4\sigma}{d}$$

$$0.1032 = \frac{4 \times 0.0725}{0.04}$$

$$= 7.25 \text{ N/m}^2$$

$$P = \frac{8\sigma}{\pi d}$$

$$0.1032 = \frac{8 \times 0.0725}{\pi \times 0.04}$$

$$= 4.61 \text{ N/m}$$

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Capillarity :-

Capillarity is defined as a phenomenon of rise or fall of liquid surface in a small tube relative to the adjacent surface of liquid surface in a small tube relative to the adjacent general level of liquid when the tube is held vertically in the liquid.

→ The rise of liquid surface is known as capillary rise when a fall of liquid surface is known as capillary depression.

→ It is a cm or mm of liquid.

→ It's value depends upon the specific weight ~~diameter~~ liquid diameter of tube & surface tension of liquid.

Expression for capillary rise:-

Consider a glass tube of small diameter 'd' opened at both ends and inserted in a liquid say water. The liquid will rise in the tube above the liquid surface.

H = Height of the liquid on tube under a state of equilibrium.

The weight of liquid of height 'h' is balanced by force at the surface of liquid on the tube due to surface tension.

σ = surface tension of liquid

θ = Angle of contact between glass

tube.

The weight of liquid of height 'h' in the tube = area of the tube $\times h \times \rho \times g$

$$= \frac{\pi}{4} d^2 \times h \times \rho \times g$$

where, ρ = density of liquid = $\sigma \times \text{surface force} \times \cos \theta$

$$= \sigma \times \pi d \times \cos \theta$$

For equilibrium $\frac{\pi}{4} d^2 h \rho g = \sigma \pi d \cos \theta$

$$h = \frac{\sigma \pi d \cos \theta}{\frac{\pi}{4} d^2 \rho g}$$

$$= \frac{4\sigma}{\rho g d} \cos \theta$$

Expression for capillary fall:-

If the glass tube is dipped in mercury the level of the mercury in the tube will be lower than general level of the outside liquid as shown in the fig.



Let h = Height of depression in the tube then
 in equilibrium 2 forces are acting
 on the mercury inside the tube

1st one is due to surface tension acting in
 downward direction = ~~$\sigma \pi d \cos \alpha$~~ $\boxed{\sigma \pi d \cos \alpha}$

2nd force is due to hydrostatic force
 acting upward $\rho =$ intensity of pressure at
 depth = $\boxed{H \times \text{area } a}$

$$h = \frac{4\sigma}{\rho g d}$$

$$h = \frac{4\sigma \cos \alpha \cdot \sigma \pi d \cos \alpha}{\rho g d} = \frac{\rho \times \pi \frac{d^2}{4}}{\rho g n \times \frac{\pi}{4} d}$$

value of ~~meniscus~~ ϕ for mercury & glass tube
 is 128° .

Problem-12

Calculate the capillary rise in a glass tube of
 2.5mm diameter when immersed vertically in
 water & mercury takes surface tension
 $\sigma = 0.0725 \text{ N/m}$. For water $\theta = 0.52 \text{ N/m}$

For mercury in contact with air the specific
 gravity of mercury is given as 13.6

of contact = 130° .

A:- given data:- $\sigma_1 = 0.0725 \text{ N/m}$.

$$\sigma_2 = 0.52 \text{ N/m}$$

$$h = \frac{\text{Density of liquid}}{\text{Density of water}}$$

$$= \frac{13.6}{1000}$$

$$= 0.0136$$

capillary rise for water ($\theta = 0$)

$$\frac{4\sigma}{\rho g d}$$

$$= \frac{4 \times 0.0725}{1000 \times 9.81 \times 2.5 \times 10^{-3}}$$

$$= 0.0118 \text{ m} = 1.18 \text{ C.M. (for mercury)}$$

Angle of contact between mercury & glass tube

$$h = \frac{4\sigma \cos \theta}{\rho g d}$$

$$\cos \theta = \frac{4 \times 0.52 \times \cos 130}{1000 \times 9.81 \times 2.5 \times 10^{-3}}$$

$$= 0.081$$

Problem-13

Calculate the capillary effect in mlms in a glass tube of 4mm diameter when emerged in water & mercury at 20°C in contact with air are 0.073575 N/m & 0.51 N/m . The angle of contact for water is 0° & that for mercury is 130° take density of water at 20°C .

A:- given data = $d = 4 \text{ mm} = 0.004 \text{ m}$.

$$\sigma_1 = 0.073575 \text{ N/m}$$

$$\sigma_2 = 0.51 \text{ N/m}$$

for water:

$$h = \frac{4\sigma}{\rho g d}$$

$$= \frac{4 \times 0.073575}{1000 \times 9.81 \times 0.004}$$

$$= 0.075 \text{ m.}$$

for mercury:

$$h = \frac{4\sigma \cos \alpha}{\rho g d}$$

$$= \frac{4 \times 0.51 \times \cos 130}{13600 \times 9.81 \times 0.004}$$

$$= -2.457 \times 10^{-3}$$

problem-14

capillary rise is glass tube is not to exceed 0.2 mm of water determine its minimum size given that surface tension of water in contact with air = 0.0725 N/m.

A:- given data:- $d = 0.2 \text{ mm} = 2 \times 10^{-3} \text{ m}$.

$$\sigma = 0.0725$$

for water

$$h = \frac{4\sigma}{\rho g d}$$

$$= \frac{4 \times 0.0725}{1000 \times 9.81 \times 2 \times 10^{-3}}$$

$$= 0.014 \text{ m.}$$

Problem-15

Find out the minimum size of glass tube that can be used in measuring water, in the capillary rise in tube is restricted in 2mm considered surface tension of water contact as 0.073575.

Given data :- $h = 2 \text{ mm} = 2 \times 10^{-3} \text{ m}$
 $\sigma = 0.073575$

$$h = \frac{4\sigma}{\rho g d}$$

$$2 = \frac{4 \times 0.073575}{1000 \times 9.81 \times d}$$

$$d = \frac{4 \times 0.073575}{1000 \times 9.81 \times 2 \times 10^{-3}}$$

$$= 0.015 \text{ m}$$

Problem-16

An oil of viscosity 5 poise is used for lubrication between a shaft & sleeve the diameter of the shaft is 0.5m. & it rotates at 200 rpm. calculate the power lost in oil for a sleeve length of 100mm the thickness of oil film is 1mm.

A!:- Given data :- $\mu = 5 \text{ poise} = \frac{5}{10} = 0.5 \frac{\text{N} \cdot \text{sec}}{\text{m}^2}$

$$D = 0.5 \text{ m}$$

$$N = 200 \text{ RPM}$$

$$L = 100 \text{ mm} = 0.1 \text{ m}$$

$$dy = 1 \text{ mm} = 1 \times 10^{-3}$$

$$V = \frac{\pi D N}{60}$$

$$v = \frac{\pi \times 0.5 \times 200}{60}$$

$$= 5.23$$

$$\tau = \mu \frac{dy}{dx}$$

$$= \frac{0.5 \times 5.23}{1 \times 10^{-3}}$$

$$= 2615$$

Shear stress $\tau = F \times A$

$$= F \times \pi D L$$

$$= 2617.5 \times \pi \times 0.5 \times 0.1$$

$$= 411.15$$

Top on the shaft

$$T = F \times \frac{D}{2}$$

$$= \frac{411.15 \times 0.5}{2}$$

$$= 102.73$$

Power lossed = $P = T \times \omega$

$$= 102.73 \times \frac{2\pi N}{16}$$

$$= \frac{102.73 \times 2 \times \pi \times 200}{16}$$

$$= 8068.395$$

03.02.20

Intensity of pressure & atmospheric pressure
and it's measurement

consider

Fluid pressure at a point

consider a small area the A in large mass

As fluid is fluid is stationary then the force exerted by the surrounding fluid on the area da in normal tension. Then the ratio $\frac{dF}{da}$ is known as intensity of pressure or simply pressure and the ratio is represented by as P .

Mathematically the pressure at point P in a fluid is $P = \frac{dF}{da}$

If the force is uniformly distributed over an area A then the pressure at point P then the fluid as $P = \frac{F}{A}$

'Intensity of pressure' -

→ It is defined as the force (weight) of a liquid to the area in contact to the fluid.

→ fluid should be static.

$$P = \frac{F}{A} = \frac{W}{A}$$

→ Its unit is N/m^2 or kN/m^2 .

'Atmospheric pressure' -

→ It is the pressure exerted by weight of the atmosphere which at a level which an mean value of, ~~925 Pa~~ 101,325 Pascals

→ It is also known as barometric pressure.

→ The standard pressure is a unit of pressure defined as 101,325 Pa which is equivalent to 760 Hg mm.

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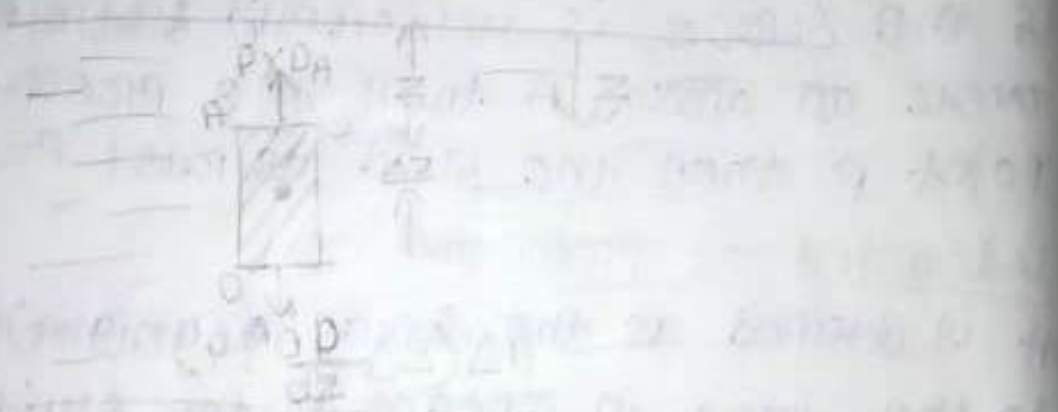
→ It is also known as barometric pressure.

→ The standard pressure is a unit of pressure defined as 101,325 Pa which is equivalent to 760 Hg mm.

Pressure Head :-

Pressure variation in fluid at rest :-

The pressure at any point in a fluid at rest is obtained by hydrostatic law which states that - The increase in rate of pressure in vertically downward direction must be equal to specific weight of fluid at rest. This provided consider a ^{small} fluid element in fig.



The pressure at any point in a fluid at rest is obtained by the hydrostatic law which states that the rate.

$\Delta p = \rho \Delta z \Delta A$ = cross-sectional area of element.

Δz = height of fluid element.

p = pressure on the ~~fluid~~ ^{face} AB.

z = distance of fluid element from free surface.

Weight of the fluid element = density \times volume

$$= \rho \Delta A \Delta z$$

Pressure force on the surface BC & AD are

equal & opposite force equilibrium fluid we have

$$P\Delta A - \left(P + \frac{dP}{dz}\Delta z\right)\Delta A + \rho g \Delta A \Delta z = 0$$

$$P\Delta A - \left(P + \frac{dP}{dz}\Delta z\right)\Delta A + \rho g (\Delta A \Delta z) = 0$$

$$P\Delta A - P\Delta A - \frac{dP}{dz}\Delta z\Delta A + \rho g \Delta A \Delta z = 0$$

$$\Rightarrow -\frac{dP}{dz}\Delta z\Delta A + \rho g \Delta A \Delta z = 0$$

$$\Rightarrow \frac{dP}{dz}\Delta z\Delta A = \rho g \Delta A \Delta z \quad [\text{cancelling } \Delta A \Delta z \text{ on both side}]$$

$$\Rightarrow \frac{dP}{dz} = \rho g$$

$$\Rightarrow \frac{dP}{dz} = \rho g = \omega$$

where $\omega =$ weight density of fluid.

Eqⁿ state that rate of increase of pressure in a vertical direction is equal to weight density of the fluid at that point. This is hydrostatic law.

By integrating the above eqⁿ for liquid, we get.

$$\rho dp = \rho g dz$$

$$p = \rho g z$$

where p is the pressure above atmospheric pressure and z is the height of the point from free surface.

from eqⁿ, we get.

$$z = \frac{p}{\rho g}$$

Pascal's law

Due to Pascal's law the intensity of pressure will be equally transmitted in all directions.

Problem-18

A open tank contains water upto a depth of 2m. above it an oil of specific gravity 0.9 upto a depth of 1m. find the pressure intensity of a liquid. ^{surface} and the bottom of tank.

A:- $h = 2\text{m}$. Given data:- $z_1 = 2\text{m}$.

$$z_2 = 1\text{m}$$

$$S = 0.9$$

$$\gamma_1 = 1000 \text{ kg/m}^3$$

$$S = \frac{\text{density of liquid}}{\text{density of water}}$$

$$0.9 = \frac{\text{density of liquid}}{1000}$$

Intensity at a

$$\text{density of liquid} = 1000 \times 0.9$$

$$\gamma_2 = 900 \text{ kg/m}^3$$

$$P = \gamma g z$$

$$= 900 \times 9.81 \times 1$$

$$= 8829 \text{ N/m}^2$$

Intensity at b

$$P = \gamma g z$$

$$= 1000 \times 9.81 \times 2$$

$$= 19620 \text{ N/m}^2$$

Pascal's law

Due to Pascal's law the intensity of pressure will be equally transmitted in all directions.

Problem-18

A open tank contains water upto a depth of 2m. above it an oil of specific gravity 0.9 upto a depth of 1m. find the pressure intensity of a liquid ^{surface} and the bottom of tank.

A:- $z_1 = 2\text{m}$, $z_2 = 1\text{m}$. given data:- $z_1 = 2\text{m}$,
 $z_2 = 1\text{m}$.

$$S = 0.9$$
$$\gamma_w = 1000 \text{ kg/m}^3$$

$$S = \frac{\text{density of liquid}}{\text{density of water}}$$

$$0.9 = \frac{\text{density of liquid}}{1000}$$

Intensity at a

$$\text{density of liquid} = 1000 \times 0.9$$

$$\gamma_2 = 900 \text{ kg/m}^3$$

$$P = \gamma g z$$

$$= 900 \times 9.81 \times 1$$

$$= 8829 \text{ N/m}^2$$

Intensity at b

$$P = \gamma g z$$

$$= 1000 \times 9.81 \times 2$$

$$= 19620 \text{ N/m}^2$$

the total pressure on the wall area is calculated by integrating the force on small strips:
 pressure intensity on each strip $P = \rho g h / \rho g z$
 area of the strip $dA = b \times dh$

The pressure force on the strip $df = P \times \text{area}$
 $= \rho g h \times b \times dh$

Total ~~pressure~~ ^{force} on the wall surface $= F = \int df$
 $= \int \rho g h \times b \times dh$

$$\int b h \rho g dh = \rho g \int h \cdot b dh = \rho g b \int h dh$$

= moment of surface area ^{about}

about the free surface area of liquid =
 area of surface \times distance of CG
 from the surface

$$= A \bar{h}$$

$$F = A \bar{h} \rho g$$

for water the value of $\rho = 1000 \text{ kg/m}^3$
 $g = 9.81 \text{ m/s}^2$

center of pressure:-

center of pressure is calculated by using
 principle of moment which states that. The
 moment of the resultant force about an axis
 = sum of the moment of the components about
 the same axis. Resultant force F is acting
 at a distance h^* from free surface
 of the liquid as shown in the fig.

Hence, moment of force F about free surface
 of the liquid = $F \times h^*$

Moment of force dA acting on a strip about
 free surface of liquid = $df \times h$ ($df = \rho g h \times b \times dh$)

Since some of moment of all such processes about free surface of liquid = $\int \rho g h x b x d h x h$

$$= \rho g \int b x^2 d h$$

$$= \rho g \int b x^2 d h = \rho g \int b x^2 d h b d h$$

$$= \rho g \int b h^2 d h = \rho g \int h^2 d A$$

$$\int h^2 d A = \int b h^2 d h$$

Moment of inertia = I_0

$$= \rho g I_0$$

$$F x h^* = \rho g I_0 \quad \text{--- (3.2)}$$

$$F = \rho g A \bar{h}$$

$$\rho g A \bar{h} x h^* = \rho g I_0 \quad \text{--- (3.3)}$$

$$h^* = \frac{\rho g I_0}{\rho g A \bar{h}} = \frac{I_0}{A \bar{h}}$$

$$I_0 = I_c + A \bar{h}^2$$




$$h^* = \frac{I_c + A \bar{h}^2}{A \bar{h}} = \frac{I_c}{A \bar{h}} + \bar{h}$$

But the theorem says parallel axis we

$$\text{have } \boxed{I_0 = I_c + A \bar{h}^2}$$

I_c = moment of inertia about to the axis passing through the CG parallel to the free surface.

substituting $\boxed{I_0 = I_c + A \bar{h}^2}$

Types	C.G. from the base	area	Moment of inertia about an axis passing through C.G. and parallel to base (I_c)	Moment of inertia about base (I_b)
	$x = \frac{d}{2}$	bd	$\frac{bd^3}{12}$	$\frac{bd^3}{3}$
	$x = \frac{h}{3}$	$\frac{bh}{2}$	$\frac{bh^3}{36}$	$\frac{bh^3}{12}$
	$x = \frac{d}{2}$	$\frac{\pi d^2}{4}$	$\frac{\pi d^4}{64}$	—

Problem-19

Determine the total pressure on an area of circular plate of diameter 1.5 m, which is placed vertically in such a way that center of plate is 3 m below of water free surface. Find the position of center of pressure.

Given data:- $d = 1.5 \text{ m}$,
 $h = 3 \text{ m}$.

$$\begin{aligned} \text{Area} &= \frac{\pi}{4} d^2 \\ &= 1.76 \end{aligned}$$



Total pressure is given by the eqⁿ.

$$F = \rho g A \bar{h}$$

$$= 1000 \times 9.81 \times 1.76 \times 3 = 51796.8 \text{ N}$$

$$\text{Total pressure} = 51796.8$$

center of pressure

$$h^* = \frac{I_G}{A\bar{h}} + \bar{h}$$

$$I_G = \frac{\pi d^4}{64}$$

$$= \frac{\pi \times 1.5^4}{64}$$

$$= 0.21 \text{ m}^4$$

$$h^* = \frac{I_G}{A\bar{h}} + \bar{h}$$

$$= \frac{0.21}{1.76 \times 3} + 3$$

$$= 3.04 \text{ m}$$

Prob-20

A rectangular plane surface is 2m wide & 3m d it lies vertical plain in water determine the total pressure & position of center of pressure on the plane surface when the plane is ~~is~~ ^{opposed} ~~is~~ ^{edge} ~~is~~ ^{edge}

↳ horizontal

A (coincident of water surface)

B (2.6m below the water surface)

A: given data $a = b = 2 \text{ m}$
 $d = 3 \text{ m}$

A) opposed edge coincide with water surface

Total pressure

$$F = \rho g A \bar{h}$$

$$= 1000 \times 9.81 \times 6 \times \frac{3}{2}$$

$$A = bd$$

$$= 8 \times 3 = 24 \text{ m}^2$$

$$= 2 \times 3$$

= 6 center of pressure

$$h^* = \frac{I_G}{A \bar{h}} + \bar{h}$$

$$I_G = \frac{bd^3}{12}$$

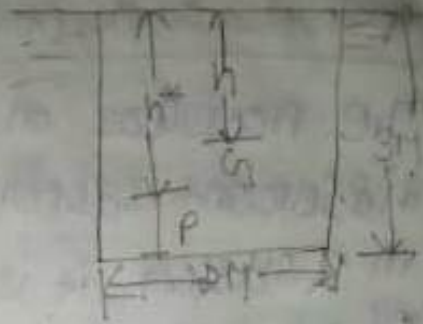
$$= \frac{2 \times 3^3}{12}$$

$$= 4.5 \text{ m}.$$

$$h^* = \frac{I_G}{A \bar{h}} + \bar{h}$$

$$= \frac{4.5}{6 \times 1.5} + 1.5$$

$$= 2 \text{ m}.$$



B) Given data:- $\bar{h} = 2.5 + 1.5 = 4$

$$b = 2 \text{ m}.$$

$$d = 3 \text{ m}.$$

Total pressure

$$F = \rho g A \bar{h}$$

$$= 1000 \times 9.81 \times 6 \times 4$$

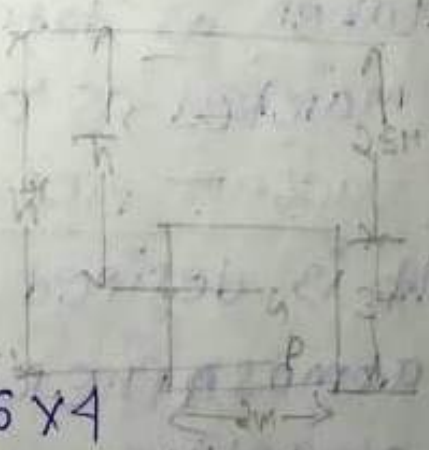
$$= 235440 \text{ N}.$$

Center of pressure

$$h^* = \frac{I_G}{A \bar{h}} + \bar{h}$$

$$= \frac{4.5}{6 \times 4} + 4 = 4.1875 \text{ m}.$$

~~1000~~



Absolute, Gauge, Atmospheric vacuum Pressure 12.02.20

The pressure on a fluid is measured in 2 different system.

In 1 system it is measured above the absolute '0' or concrete vacuum. It is called absolute pressure.

Absolute pressure:-

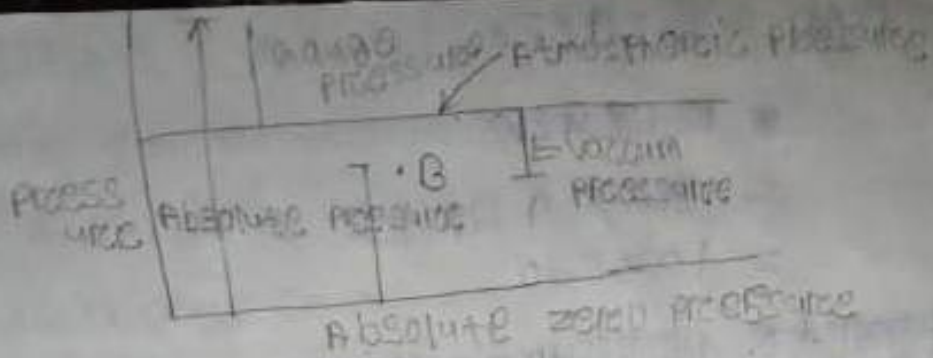
It is defined as the pressure which is measured with reference to absolute vacuum pressure.

Gauge pressure:-

It is defined as the pressure which is measured with the help of pressure measuring instrument atmospheric pressure is taken as datum. Atmospheric pressure is marked as '0'.

Vacuum pressure:-

It is defined as the pressure below the atmospheric pressure. Relation between absolute, gauge & vacuum pressure are shown in fig.



The relationship between absolute, gauge & vacuum pressure is given by mathematically

Absolute pressure = Atmospheric + Gauge pressure

$$P_{ab} = P_{atm} + P_{gauge}$$

Similarly, vacuum pressure = Atmospheric pressure - Absolute pressure

$$P_{vacuum} = P_{atm} - P_{absolute}$$

problem-2)

What are the gauge pressure & absolute pressure at a point 3m. below the free surface of a liquid having density of $1.53 \times 10^3 \text{ kg/m}^3$. Atmospheric pressure is equivalent to 760mm of mercury. The specific gravity of mercury is 13.6 & density of water = 1000.

A:- given data :- $Z_1 = 3\text{m}$.

$$\rho_l = 1.53 \times 10^3 \text{ kg/m}^3$$

$$Z_0 = 760 \text{ mm} = 0.76 \text{ m}$$

$$\text{Density of mercury} = \text{specific gravity} \times \text{density of water}$$

$$= 13.6 \times 1000$$

$$= 13600$$

$$P_{atm} = \rho_0 \times g \times Z_0$$

$$= 13600 \times 9.81 \times 7.5$$

$$= 1000620$$

~~Absolute~~ pressure = $\rho_1 g Z_1$
99480

$$= 1.33 \times 10^3 \times 9.81 \times 3$$

$$P_{gauge} = 45027.9$$

$$\text{Absolute pressure} = P_{atm} + P_{gauge}$$

$$= 1000620 + 45027.9$$

$$= 1045647.9$$

Basic equation of flow & Application & rate of discharge :-

Introduction :-

① Kinematic flow :-

Kinematic is defined as the branch of science which deals with motion of particles without considering the force in motion. velocity at any point and flow field at any time is studied in this branch of fluid mechanics.

Types of fluid flow :-

The fluid flow is classified as :-

i) Steady & unsteady flow

ii) Uniform & Non uniform flow

iii) Laminar & Turbulent flow.

i) compressible & incompressible flow

v) rotational & irrotational flow

vi) 1, 2 & 3 dimensional flow.

ii) Stated & unsteady flow:-

Steady flow is defined as that the type of flow in which fluid characteristics like velocity, pressure & density at a point don't change with time.

$$\text{Mathematically} = \left(\frac{dv}{dt}\right)_{x_0, y_0, z_0} = 0, \left(\frac{dp}{dt}\right)_{x_0, y_0, z_0} = 0$$
$$\left(\frac{d\rho}{dt}\right)_{x_0, y_0, z_0} = 0$$

where $x_0, y_0, z_0 =$ fixed point in the field.

Unsteady flow is a type of flow in which velocity, pressure or density at a point doesn't change with respect to time.

$$\text{Mathematically} = \left(\frac{dv}{dt}\right)_{x_0, y_0, z_0} \neq 0, \left(\frac{dp}{dt}\right)_{x_0, y_0, z_0} \neq 0$$
$$\left(\frac{d\rho}{dt}\right)_{x_0, y_0, z_0} \neq 0$$

iii) Uniform & Non uniform flow:-

Uniform flow is defined as the type of flow in which the velocity at any given time doesn't change with respect to space.

$$\text{Mathematically, } \left(\frac{dv}{ds} \right)_t = 0$$

dv = change in velocity

ds = length of flow in direction 's'.

Non uniform flow is the type of flow in which velocity at given time changes with respect to space.

$$\text{Mathematically, } \left(\frac{dv}{ds} \right)_t \neq 0$$

(ii) Laminare & Turbulant flow :-

Laminare flow is defined as the type of flow in which fluid particles move along well defined path or streamline & streamlines are ~~straight~~ straight & parallel. Thus the particles moves in lamina or layers fluid smoothly over the adjacent layer. This type of flow is called streamline flow or viscous flow.

Turbulent flow is the type of flow in which fluid particles move in a zigzag way due to this movement of fluid particles in zigzag way the eddies formation takes place.

Reynold number :-

ii) ~~complete~~ Reynold Number :-

For a pipe flow the type of flow is determined by non-dimensional number $Re = \left(\frac{VD}{\nu} \right)$ called Reynold's number.

where, $D =$ diameter of pipe.

$v =$ mean velocity of pipe.

$\nu =$ kinematic viscosity.

If Reynold's number ^{less than} < 2000 the flow is called laminar. If it is more than 4000 the flow is turbulent. If the Reynold number lies between 2000 & 4000 the flow may be laminar or turbulent.

iv) compressible & incompressible flow :-

compressible flow is that type of flow in which density of flow changes, stream point to point. In other words density ρ is constant.

Thus mathematically for compressible flow
 $\rho \neq \text{constant}$

In incompressible flow the density is constant for the flow of fluid.

Mathematically, $\rho = \text{constant}$

v) Rotational & Irrotational flow :-

Rotational flow is the type of flow in which the fluid particles while flowing along streamline also rotate in their own

axis.

Irrotational flow is the type of flow in which any fluid particle while flowing along streamline also don't rotate in their own

axis.
1, 2 & 3 dimensional flow :-

1 dimensional flow in which flow parameters such as velocity is a function of time & one space coordinate only. For steady 1 dimensional flow the velocity is in function of 1 space coordinate.

$$\text{Mathematically, } u = f(x), v = 0 \text{ \& } w = 0$$

where, u, v & w are velocity components in x, y, z direction.

2 dimensional flow is the type of flow in which velocity is a function of time & 2 rectangular space coordinates. For steady 2 dimensional flow, the velocity is a function of 2 space coordinates only =

$$\text{Mathematically } u = f_1(x, y), v = f_2(x, y) \text{ \& } w = 0$$

3 dimensional is type of flow in which velocity is a function of time & 3 mutually

perpendicular direction but are steady flow.
Fluid parameters are the function of space
coordinates x, y, z .

mathematically, $u = f_1(x, y, z)$, $v = f_2(x, y, z)$, $w = f_3(x, y, z)$
17.02.20

Rate of flow or discharge (Q):

It is defined as the quantity of fluid flowing
per sec. through a secⁿ of pipe or a channel.
For an incompressible fluid or liquid the
rate of flow or discharge is expressed as
volume of fluid across the secⁿ/sec.
For compressible fluid the rate of ^{flow}
is usually expressed as the weight of
fluid flowing across the secⁿ.

- For liquid's unit of Q are m^3/sec or L/sec .
- For gas the unit's of Q is kgf/sec or N/sec .

Continuity equation:

The equation based on principle of conserva-
tion of mass is called continuity eqⁿ.

Thus, for a fluid flowing through the
pipe at all the cross-section, the quantity
of fluid or secⁿ is constant.

Let, $v_1 =$ Average velocity of cross-section
1-1.

$\rho_1 =$ Density at the secⁿ 1-1.

$A_1 =$ Area of the pipe at secⁿ 1-1.

$\rho_1, \rho_2, A_2 = A_1$ are the follow secⁿ 2-2.

The rate of flow at secⁿ 1-1 = $\rho_1 A_1 v_1$

Then the rate of flow at secⁿ 2-2 = $\rho_2 A_2 v_2$

According to conservation of mass the rate of flow at secⁿ 1-1 = The rate of

$$\text{Secⁿ 2-2 } \Rightarrow \rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

This is applicable to the compressible as well as incompressible fluid is called continuity eqⁿ.

If fluid is incompressible $\rho_1 = \rho_2$ & continuity eqⁿ = $A_1 v_1 = A_2 v_2$

Problem-22

The diameter of a pipe at a secⁿ 1 & 2 are 10 cm & 15 cm. Find the distance through the pipe if the velocity of water flow at the pipe at the secⁿ 1 is 5 m/sec. Then determine the velocity at the secⁿ 2.

Given data: $D_1 = 10 \text{ cm} = 0.1 \text{ m}$

$$v_1 = 5 \text{ m/sec}$$

$$D_2 = 15 \text{ cm} = 0.15 \text{ m}$$

$$A_1 = \frac{\pi}{4} D_1^2$$

$$= \frac{\pi}{4} \times (0.1)^2 = 7.85 \times 10^{-3}$$

$$A_2 = \frac{\pi}{4} D_2^2$$

$$= \frac{\pi}{4} (0.15)^2$$

$$= 0.017$$

Discharge through pipe is $Q = A_1 V_1$

$$= 7.85 \times 10^{-3} \times 5$$

$$= 0.03925$$

$$A_1 V_1 = A_2 V_2$$

$$0.03925 = 0.017 \times V_2$$

$$V_2 = \frac{0.03925}{0.017}$$

$$= 2.308$$

Problem-23

A 30 cm. diameter pipe conveying water, branches into 2 pipes of diameters 20 cm. & 15 cm. respectively. If the average velocity in the 30 cm. diameter pipe is 2.5 m/sec and the discharge in the pipe also determine the velocity in 15 cm. pipe & average velocity in 20 cm. pipe is 2 m/sec.

At given data:-

$$V_1 = 2.5 \text{ m/s}$$

$$D_1 = 30 \text{ cm.} = 0.3 \text{ m.}$$

$$V_2 = 2 \text{ m/s}$$

$$D_2 = 20 \text{ cm.} = 0.2 \text{ m.}$$

$$D_3 = 15 \text{ cm.} = 0.15 \text{ m.}$$

$$V_3 = ?$$

$$A_1 = \frac{\pi}{4} D_1^2$$

$$= \frac{\pi}{4} (0.3)^2 = 0.070$$

$$A_2 = \frac{\pi}{4} D_2^2$$

$$= \frac{\pi}{4} (0.2)^2$$

$$= 0.031$$

$$A_3 = \frac{\pi}{4} D_3^2$$

$$= \frac{\pi}{4} (0.15)^2$$

$$= 0.017$$

discharge in pipe 1 ~~is~~ $Q_1 = Q_2 + Q_3$

$$Q_1 = A_1 V_1$$

$$= 0.070 \times 2.5$$

$$= 0.175$$

$$Q_2 = A_2 V_2$$

$$= 0.031 \times 2$$

$$= 0.062$$

$$Q_1 = Q_2 + Q_3$$

$$0.175 = 0.062 + Q_3$$

$$Q_3 = 0.175 - 0.062$$

$$= 0.113$$

$$Q_3 = A_3 V_3$$

$$0.113 = 0.017 \times V_3$$

$$V_3 = \frac{0.113}{0.017} = 6.647$$

Bernoulli's Equation for Real Fluid

19.02.20

The Bernoulli's eqⁿ was derived on the assumption of that the fluid is (Non-viscous) there force friction less but all the real fluids are viscous and hence offer resistance to flow.

Thus, there are always some losses in fluid flows and hence the application of Bernoulli's eqⁿ the losses have to be taken into consideration.

Thus, the Bernoulli's eqⁿ for real fluids between point 1 & 2 is given as

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2 + h_L$$

where, h_L = loss of energy between 1 & 2.

$\frac{P_1}{\rho g}$ = Pressure gradient for fluid.

$\frac{V_1^2}{2g}$ = velocity gradient.

z_1 = distance

Problem - 24

A pipe of diameter 400mm carries water at velocity of 25 m/sec. The pressure at the point A & B are given by 29.43 N/cm² & 27.563 N/cm². Respective while the datum head at A & B are 28m & 30m. Find the loss of head

between A & B.

A1 - Given data: $V = 25 \text{ m/sec}$
 $D_A = 400 \text{ mm} = 4 \text{ m}$

$$P_A = 29.43 \text{ N/cm}^2$$

$$= 0.2943 \text{ M} = \frac{29.43 \times 10^4}{1000}$$

$$Z_A = 28 \text{ m}$$

$$D_B = 400 \text{ mm} = 4 \text{ m}$$

$$P_B = 22.563 \text{ N/cm}^2$$

$$= 22.563 \times 10^4 \text{ N/m}^2$$

$$Z_B = 30 \text{ m}$$

$$i) E_A = \frac{P_1}{\rho g} + \frac{V_1^2}{2g} + Z_1$$

$$= \frac{29.43 \times 10^4}{1000 \times 9.81} + \frac{(25)^2}{2 \times 9.81} + 28$$

$$= 81.855$$

$$ii) E_B = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + Z_2$$

$$= \frac{22.563 \times 10^4}{1000 \times 9.81} + \frac{(25)^2}{2 \times 9.81} + 30$$

$$= 81.855$$

$$\text{Energy loss } E_L = E_A - E_B$$

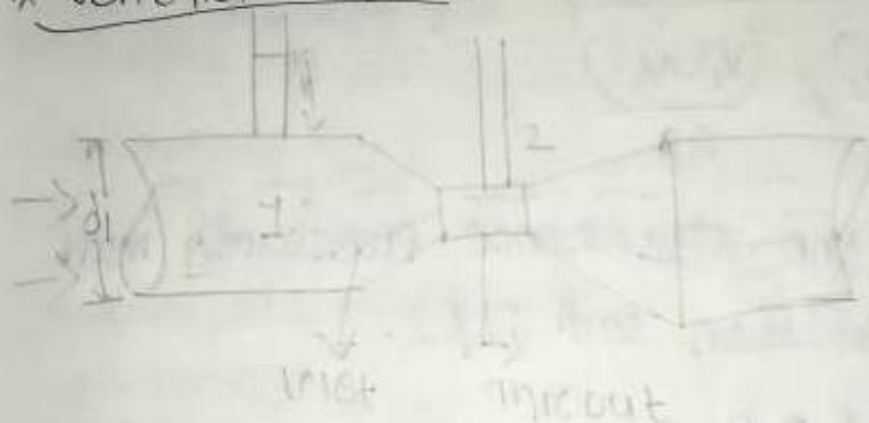
$$= 81.855 - 81.855$$

$$= 0$$

Practical application of Bernoulli's eqⁿ -

Bernoulli's eqⁿ is applied in all problems of incompressible fluid flow where energy considerations are involved but we shall consider its application to the following measuring device.

- * Venturimeter.
- * orifice meter.
- * Pitot tube.
- * Venturimeter :-



It is a device used for measuring rate of flow of fluid flowing through the pipe. It consists of 3 parts . .

→ A short converging part.

→ Throat

→ diverging part.

It is based on principle of venturimeter.

Expression for rate of flow through venturimeter.

d_1 = diameter at inlet or at section 1.

P_1 = Pressure at secⁿ 1.

V_1 = velocity of fluid at secⁿ 1.

a = area of secⁿ 1. $\frac{\pi}{4} d_1^2$

d_1, P_1, V_1 & d_2, P_2, V_2 are corresponding values at secⁿ 2

Applying Bernoulli's eqⁿ at secⁿ 1 & 2 we get

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + Z_2$$

Here $Z_1 = Z_2$

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} = \frac{P_2}{\rho g} + \frac{V_2^2}{2g}$$

$$\frac{(P_1 - P_2)}{\rho g} = \frac{(V_2^2 - V_1^2)}{2g}$$

But $\frac{P_1 - P_2}{\rho g}$ is the difference pressure head between secⁿ 1 & 2.

It is called h .

The substituting the value of $\frac{P_1 - P_2}{\rho g}$ in above eqⁿ we get $h = \frac{V_2^2 - V_1^2}{2g}$

Now applying continuity eqⁿ at secⁿ 1 & 2 $a_1 V_1 = a_2 V_2$

$$V_1 = \frac{a_2 V_2}{a_1}$$

$$h = \frac{V_2^2}{2g} - \frac{V_1^2}{2g}$$

$$h = \frac{V_2^2}{2g} - \frac{(a_2 V_2)^2}{a_1^2 \cdot 2g}$$

$$h = \left[\frac{V_2^2}{2g} \left(1 - \frac{a_2^2}{a_1^2} \right) \right]$$

d_1, P_1, v_1 are corresponding values at secⁿ 1

Applying Bernoulli's eqⁿ at secⁿ 1 & 2 we get

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} + Z_1 = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + Z_2$$

Here $Z_1 = Z_2$

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} = \frac{P_2}{\rho g} + \frac{v_2^2}{2g}$$

$$\frac{(P_1 - P_2)}{\rho g} = \frac{(v_1^2 - v_2^2)}{2g}$$

But $\frac{P_1 - P_2}{\rho g}$ is the difference pressure head ~~between~~ secⁿ 1 & 2.

It is equal to h .

The substituting the value of $\frac{P_1 - P_2}{\rho g}$ in above eqⁿ we get $h = \frac{v_1^2 - v_2^2}{2g}$

Now applying continuity eqⁿ at secⁿ 1 & 2 $a_1 v_1 = a_2 v_2$

$$v_1 = \frac{a_2 v_2}{a_1}$$

$$h = \frac{v_2^2}{2g} - \frac{v_1^2}{2g}$$

$$h = \frac{v_2^2}{2g} - \frac{(a_2 v_2)^2}{a_1^2 \cdot 2g}$$

$$h = \left[\frac{v_2^2}{2g} \left(1 - \frac{a_2^2}{a_1^2} \right) \right]$$

$$h = u \left[\frac{S_u}{S_o} - 1 \right]$$

Case-2

In differential manometer contains a liquid which is lighter than the liquid flowing through the pipe the value of h is given by

$$h = u \left[1 - \frac{S_L}{S_o} \right]$$

S_L = specific gravity of liquid in U-tube.

S_o = specific gravity of liquid flowing through the pipe.

u = difference between liquid lighter U-tube.

Problem 25

A horizontal venturimeter with inlet & throat diameters 30 cm. & 15 cm. respectively is used to measure the flow of water. The reading of differential manometer connected in inlet & throat is 20 cm. of mercury. Determine the rate of flow.

$$C_d = 0.98.$$

Given data: - $d_1 = 30 \text{ cm.}$

$$a_1 = \frac{\pi}{4} (d_1)^2 = 706.85 \text{ cm.}^2$$

$$d_2 = 15 \text{ cm.}$$

$$a_2 = \frac{\pi}{4} (d_2)^2 = 176.71 \text{ cm.}^2$$

$$C_d = 0.98, S_h = 13.6, g_0 = 1.$$

Reading of differential manometer $h = 20$ cm of mercury.

$$h = \mu \left[\frac{S_h}{S_0} - 1 \right]$$

$$= 20 \left[\frac{13.6}{1} - 1 \right]$$

$$= 252$$

$$Q = C_d \times \frac{a_1 a_2}{\sqrt{a_1^2 - a_2^2}} \times \sqrt{2gh}$$

$$= 0.98 \times \frac{706.85 \times 176.71}{\sqrt{(706.85)^2 - (176.71)^2}} \times \sqrt{2 \times 9.81 \times 252}$$

$$= 12576.243$$

27.02.2020

Flow over Notches & weirs :-

Notches :-
In notches is a device used for measuring the rate of flow of a liquid through a small channel or a tank. It may be defined as an opening in the side of a tank or a small channel in such a way that the liquid surface in the tank or channel is below the top edge of the opening.

Weir :-

A weir is a concrete or masonry structure placed in an open channel over which the flow occurs. It generally in the form of vertical wall, with sharp edge at the top running although way across open channel. The notch is a small size while the weir is a bigger size.

Classification of Notches or Weir

The notches is classified as shape of opening :-

- * Rectangular Notche.
- * Triangular Notche.
- * Trapezoidal Notche.
- * Stepped Notche.

The weir are classified according to the shape of opening, the shape of crest & nature of discharge.

according to the shape of opening:-

- * Rectangular weir.
- * Triangular weir.
- * Trapezoidal weir.

discharge through Rectangular Notche or weir



(Section at crest)

consider a rectangular notch or weir provided in channel carrying water

H = Head of water over the crest.

L = length of notch or weir.

for finding discharge of water flowing

Here, the wire or notch is considered an elemental horizontal strip of water, thickness dh & length L , h from the free surface of water shown in the fig.

The area of the strip = $L \times dh$
 The theoretical velocity of water flowing through the strip = $\sqrt{2gh}$

The discharge dQ through the strip is = $C_d \times \text{area of the strip} \times \text{theoretical velocity}$

$$dQ = C_d \times L \times dh \times \sqrt{2gh}$$

The total discharge Q for whole notch of wire is determined by integrating eqn between the limit zero to H .

$$\begin{aligned} Q &= \int_0^H C_d \cdot L \cdot \sqrt{2gh} \, dh \\ &= C_d \cdot L \cdot \sqrt{2g} \int_0^H h^{1/2} \, dh \\ &= C_d \cdot L \cdot \sqrt{2g} \left[\frac{h^{1/2+1}}{1/2+1} \right]_0^H \\ &= C_d \cdot L \cdot \sqrt{2g} \left[\frac{h^{3/2}}{3/2} \right]_0^H \end{aligned}$$

$$= \frac{2}{3} C_d \cdot L \cdot \sqrt{2g} \left[H \right]^{3/2}$$

Problem-26

Find the discharge of water flowing over a rectangular notch 2M. L. when the constant head over the notch is 300mm take $C_d = 0.6$.

A:- given data:- $L = 2M$.

$$H = 300MM = 0.3M.$$

$$C_d = 0.6$$

$$Q = \frac{2}{3} C_d L \sqrt{2g} [H]^{3/2}$$

$$= \frac{2}{3} \times 0.6 \times 2 \times \sqrt{2 \times 9.81} \left[\frac{0.3}{1000} \right]^{3/2}$$

$$= 0.582$$

Problem-27

Determine the h of rectangular weir of $L = 6M$. to built across a rectangular channel. The maximum depth of water on the downstream side of the weir = 1.8M. discharge is 2000 l/sec take $C_d = 0.6$, neglect end construction.

A:- given data:- $L = 6M$.

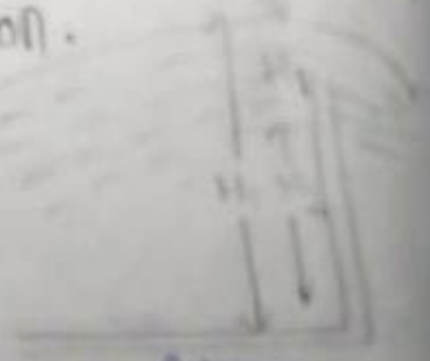
$$C_d = 0.6$$

$$H_1 = 1.8M.$$

$$Q = 2000 \text{ l/sec} = 2m^3/\text{sec}$$

$H =$ height of the water above crest.

$$Q = \frac{2}{3} C_d L \sqrt{2g} [H]^{3/2}$$



$$Q = \frac{2}{3} \times 0.6 \times 6 \times \sqrt{2 \times 9.81} [H]^{\frac{3}{2}}$$

$$= \frac{10.63}{3} [H]^{\frac{3}{2}}$$

~~$$10.63 = \frac{2}{3} [H]^{\frac{3}{2}}$$~~

$$\left[\frac{2}{10.63} \right] = [H]^{\frac{3}{2}}$$

$$\left[\frac{2}{10.63} \right]^{\frac{2}{3}} = H$$

$$H = 0.328$$

$$H_2 = H_1 - H$$

$$= 1.8 - 0.328$$

$$= 1.472$$

26.02.20

Discharge over a triangular notch or weir.

The expression for the discharge over a triangular notch or weir is same. It is derived as
 Let H = Head of the water above V notch.

θ = Angle of notch.

Consider a horizontal strip of water of thickness dh at a depth h from free surface of water shown in the fig.



$$\tan \frac{\theta}{2} = \frac{AC}{BC}$$

$$= \frac{AC}{H-h}$$

$$AC = (H-h) \tan \frac{\theta}{2}$$

width of strip AB

$$= 2AC$$

$$= 2(H-h) \tan \frac{\theta}{2}$$

Area of the strip

$$= 2(H-h) \tan \frac{\theta}{2} \times dh$$

Theoretical velocity of water through strip

$$= \sqrt{2gh}$$

$dQ = cd \times \text{area of the strip} \times \text{velocity}$

$$= cd \times 2(H-h) \tan \frac{\theta}{2} \times dh \times \sqrt{2gh}$$

$$= 2cd \times (H-h) \tan \frac{\theta}{2} \times \sqrt{2gh} \times dh$$

$$Q = \int_0^H 2cd \times (H-h) \tan \frac{\theta}{2} \times \sqrt{2gh} \times dh$$

$$2cd \times \tan \frac{\theta}{2} \int_0^H (H-h) \times \sqrt{2gh} \times dh$$

$$= 2cd \times \tan \frac{\theta}{2} \times \sqrt{2g} \int_0^H (H-h) (h)^{\frac{1}{2}} dh$$

$$= 2cd \times \tan \frac{\theta}{2} \times \sqrt{2g} \left(Hh^{\frac{1}{2}} - h^{\frac{3}{2}} \right) \Big|_0^H$$

$$= 2cd \times \tan \frac{\theta}{2} \times \sqrt{2g} \left[\frac{Hh^{\frac{3}{2}}}{\frac{3}{2}} - \frac{h^{\frac{5}{2}}}{\frac{5}{2}} \right] \Big|_0^H$$

$$= 2cd \times \tan \frac{\theta}{2} \times \sqrt{2g} \left[\frac{2}{3} HH^{\frac{3}{2}} - \frac{2}{5} H^{\frac{5}{2}} \right]$$

$$= 2cd \tan \frac{\theta}{2} \sqrt{2g} \times \frac{2}{3} H^{\frac{5}{2}} - \frac{2}{5} H^{\frac{5}{2}}$$

$$= 2cd \tan \frac{\theta}{2} \sqrt{2g} \times \frac{4}{15} (H^{\frac{5}{2}} - H^{\frac{5}{2}})$$

$$= \frac{8}{15} C_d \times \tan \frac{\theta}{2} \times \sqrt{2g} H^{\frac{5}{2}}$$

$$C_d = 0.6$$

$$\theta = 90$$

$$Q = \frac{8}{15} \times 0.6 \times 1 \times \sqrt{2g} \times H^{\frac{5}{2}}$$

$$= 1.417 H^{\frac{5}{2}}$$

Problem-28

Find a discharge over a triangular notch of angle 60° when head over the V notch is 0.3M. assume $C_d = 0.6$.

A:- Given data = $C_d = 0.6$
 $H = 0.3M.$
 $\theta = 60^\circ$

$$Q = \frac{8}{15} \times 0.6 \times 0.577 \times \sqrt{2 \times 9.81} \times 0.3^{\frac{5}{2}}$$

$$= 0.039 \approx 0.04$$

Problem-29

Water flows over a rectangular weir 1M. wide at a depth of 150MM. & afterwards passes through a triangular right angle weir taking Cd for rectangular & triangular weir as 0.62 & 0.59 respectively. Find the depth over the triangular weir.

A:- Given data:- $L = 1M.$

$$H = 150MM. = 0.15M.$$

$$C_d = 0.62 \text{ (rectangular)} \\ C_d = 0.59 \text{ (triangular)}$$



$$Cd = 0.59$$

H = suppose H_1

$$Q = \frac{2}{3} Cd L \sqrt{2g} [H]^{3/2}$$

$$= \frac{2}{3} \times 0.62 \times 1 \times \sqrt{2 \times 9.81} \times 0.15^{3/2}$$

$$= 0.106$$

$$Q = \frac{8}{15} Cd \times \tan \frac{\theta}{2} \times \sqrt{2g} \times H^{5/2}$$

$$0.106 = \frac{8}{15} \times 0.59 \times 1 \times \sqrt{2 \times 9.81} \times H_1^{5/2}$$

$$0.106 = 1.393 H_1^{5/2}$$

$$\frac{0.106}{1.393} = H_1^{5/2}$$

$$0.076 = H_1^{5/2}$$

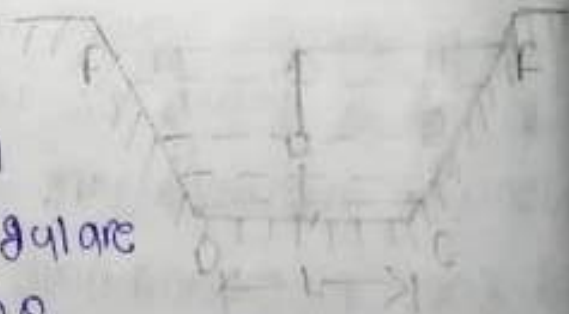
$$H_1 = 0.076^{2/5}$$

$$= \cancel{0.0304} 0.356$$

Discharge over a trapezoidal notch or wire:

A trapezoidal notch or wire is a combination of rectangular & triangular notch or wire thus the total discharge will be equal to some of discharge through rectangular wire or notch & discharge through triangular notch or wire.

Let H = Height over the notch.



L = Length of the crest of the notch.

C_{d1} = Coefficient of discharge for rectangular portion ABCD

C_{d2} = Coefficient of discharge for triangular portion EAD & EBF.

Discharge through rectangular portion ABCD is given by $Q_1 = \frac{2}{3} C_{d1} L \sqrt{2g} [H]^{\frac{3}{2}}$

Discharge through two triangular notches EAD & EBF = discharge through single triangular notch of angle θ

& it is given by $Q_2 = \frac{8}{15} C_{d2} \tan \frac{\theta}{2} \sqrt{2g} H^{\frac{5}{2}}$

Discharge through trapezoidal notch or weir EDCFE = $Q_1 + Q_2$

$$= \frac{2}{3} C_{d1} L \sqrt{2g} [H]^{\frac{3}{2}} + \frac{8}{15} C_{d2} \tan \frac{\theta}{2} \sqrt{2g} H^{\frac{5}{2}}$$

PROBLEM

Find the discharge through a trapezoidal notch which is 1m wide at the top & 0.4m at the bottom & its 300cm in height. The head of water on the notch is 20cm. Assume C_d for rectangular portion = 0.62 while for triangular portion = 0.6.

A:- Given data:- $EF = 1m$.

$$L = 0.4m$$

$$H = 0.2m$$

$$C_{d1} = 0.62$$

$$C_{d2} = 0.6$$



$$\tan \theta = \frac{P}{b} = \frac{FA}{AD} = \frac{0.6}{0.3}$$

$$= 2$$

~~tan = 2~~ $\tan \frac{\theta}{2} = 1$

~~or~~

$$Q_1 = \frac{2}{3} C_d \sqrt{2g} [H]^{3/2}$$

$$= \frac{2}{3} \times 0.62 \times 0.4 \times \sqrt{2 \times 9.81} \times 0.2^{3/2}$$

$$= 0.065$$

$$Q_2 = \frac{8}{15} C_d \tan \frac{\theta}{2} \sqrt{2g} \times H^{5/2}$$

$$= \frac{8}{15} \times 0.6 \times 1 \times \sqrt{2 \times 9.81} \times 0.2^{5/2}$$

$$= 0.025$$

$$0.065 + 0.025$$

$$= 0.09$$

CCA (cross commanded area)

→ The imaginary area for which we are designing the channel is called cross-commanded area.

CCA (culturable commanded area)

→ The area where we cultivate the crops called culturable, commanded area.

a) culturable commanded area

b) unculturable " "

unculturable area

The area where agriculture cannot be done is called unculturable area.

crop period

The period from sowing of crop to harvesting is called crop period.

Intensity of Irrigation

→ Intensity of irrigation is defined as ratio between cultivation area to particular crop of culturable area.

$$I.I = \frac{\text{Area} \times 100}{\text{CCA}} (\%)$$

Hydrological cycle

* Hydrologic cycle is the sequence of cyclic events which correlates the movement of H_2O from the atmosphere to the earth surface and then to large water bodies through sub surface and surface finally going back to the atmosphere.

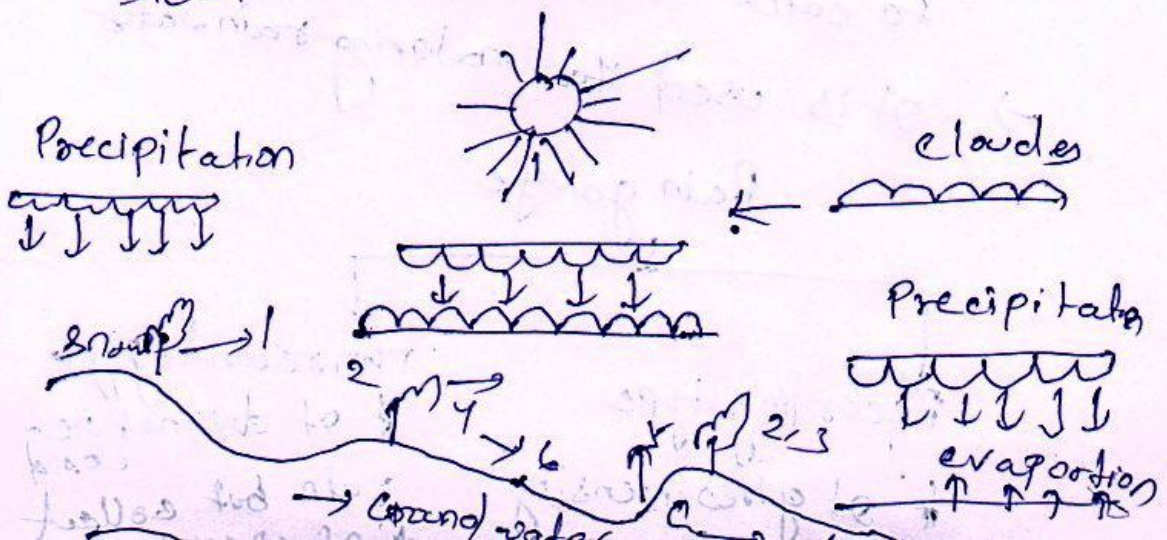
procedure

→ water in the oceans evaporate due to heat energy provided by solar radiation

→ Then water vapor moves upwards and forms clouds

→ While much of the clouds condense fall back to the ocean as rain and part of clouds is driven to the land by wind.

→ Therefore they condense and precipitate on to land by rain, snow, hail sleet.



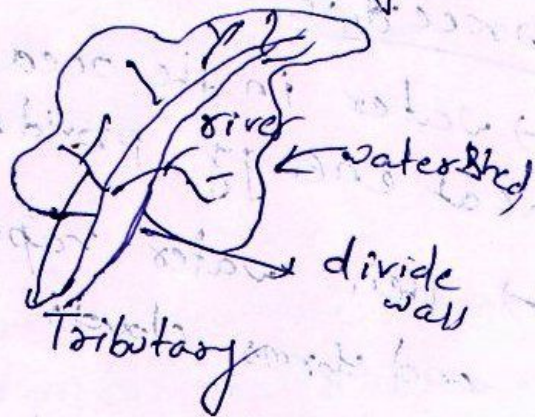
Catchment area

→ The area of land draining water into stream or water course at given location is called catchment area

→ It is called drainage basin

→ In USA it is called watershed

→ It is area is measured by planimeter



Rain gauge

→ It is essentially consists of cylindrical vessel assemble kept in open to contact of rain.

→ The circular opening leads it to catch to collect water.

→ It is used for measuring rain water

Rain gauge

Recording type

* It gives intensity of rain fall

Non recording type

* It does not record rain but collect
* It gives depth of rain fall

Hytograph

A Hyteograph is a graphical representation of the distribution of rainfall

Irrigation

Introduction

Name:- Shatabeli Jay
Branch - civil engg
designation - Assistant
profes

Defination of irrigation

→ The process of artificial application of water to the soil for the growth of agricultural crop is termed as irrigation.

→ It is practically a science of planning and designing a water supply for agricultural land to protect the crops from bad effect of drought or low rainfall.

→ It includes the construction of weirs, dams, barrages for the regular supply of water to the cultivable lands.

Necessity of irrigation

→ insufficient rainfall:- when the seasonal rainfall is minimum i.e. insufficient for crops then irrigation is necessary.

→ uneven distribution of rainfall:- when the rainfall is not distributed evenly through out the crop period, then irrigation is necessary.

→ Development of agricultural crops in desert area:- The desert where rainfall is very low, the irrigation system is required.

Benefits of irrigation

→ Yield of crops:- In the period of low rainfall or drought, the yield of crops may be increased by the irrigation system.

water-distribution efficiency

The effectiveness of irrigation is measured by distribution efficiency.

It is denoted by η_d .

$$\eta_d = \left(1 - \frac{d}{D}\right)$$

Consumptive use or Evapotranspiration (C_u)

→ Consumptive use for particular crop may be defined as the total amount of water used by the plant in transpiration and evaporation from adjacent soils or from plant leaves in a specified time.

→ It is denoted by C_u .

Modul - II (canal irrigation)

Classification of canals

(1) Based on alignment

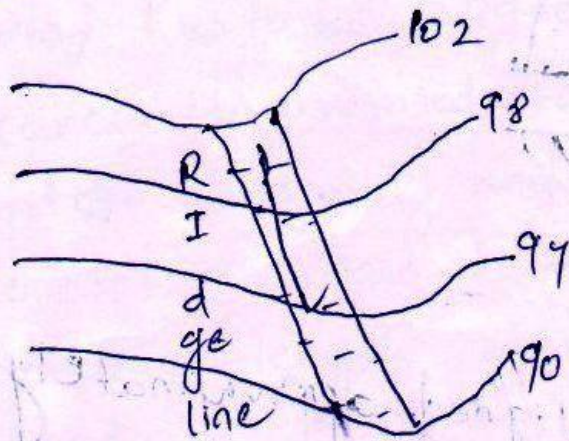
Depending its alignment canals are designated as

(i) Ridge or watershed canal

(ii) contour canals

(iii) side slope canal

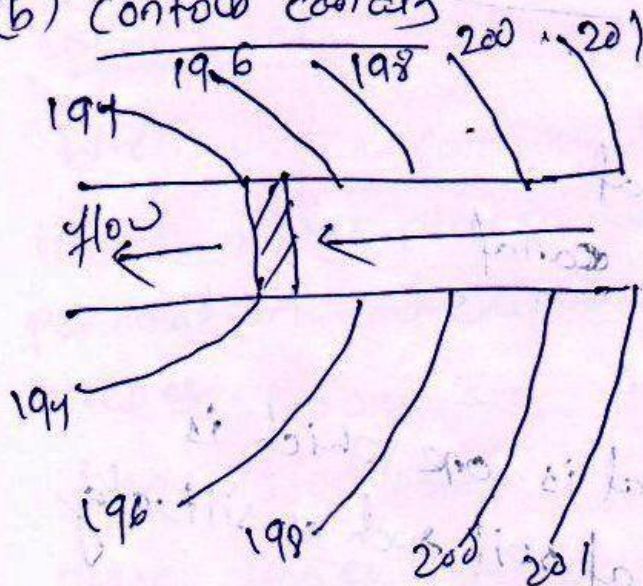
(a) Ridge or water shed canal



→ The canal which is aligned along ridge line (water shed line) is known as ~~ridge~~ ridge or water-shed canal.

→ The advantage of this type of canal is that it can irrigate its area both side of its canal.

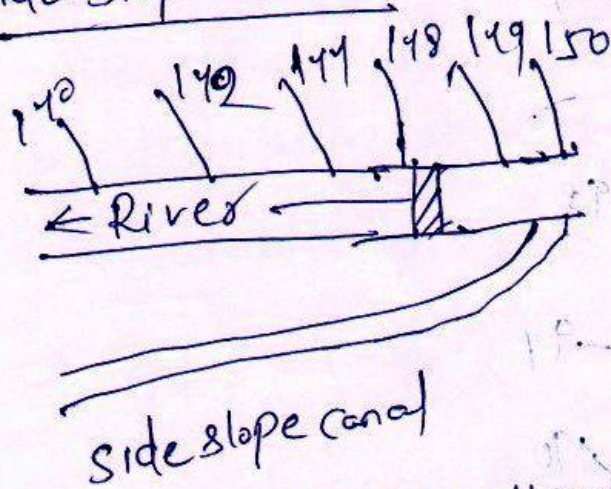
(b) Contour canals



→ The canal which is aligned approximately parallel to the contour lines is known as contour canal.

→ These canal can irrigate only one side.

Side slope canals



- These canals are aligned approximately at right angle to the contour line
- These canals can irrigate only one side

(2) Based on financial output

- (a) productive canal
- (b) protective canal

(3) classification based on boundary surface.

- (a) Alluvial canal
- (b) nonalluvial canal

Alluvial canal

Alluvial canal is one which is excavated in alluvial soil such as silt/clay

nonalluvial canal

The ridge banded canal are those which have

Canal Alignment

A canal has to be aligned in such a way that it covers its proposed to be irrigated with shortest possibility and its cost including the cost of cross-drainage work.

A shorter length of canal ensures less loss of head.

Loss of discharge due to seepage and evaporation so that additional area can be brought into cultivation.

According to alignment canals are classified as following

(i) Ridge canal

(ii) Contour canal

Canal losses

When water continuously flow through a canal losses takes place due to seepage, deep percolation and evaporation.

These losses are sometimes known as transmission losses

These losses are classified into 3 types

(i) Evaporation losses (ii) Transmission losses

(iii) seepage losses

Cross drainage work

1) Aqueduct

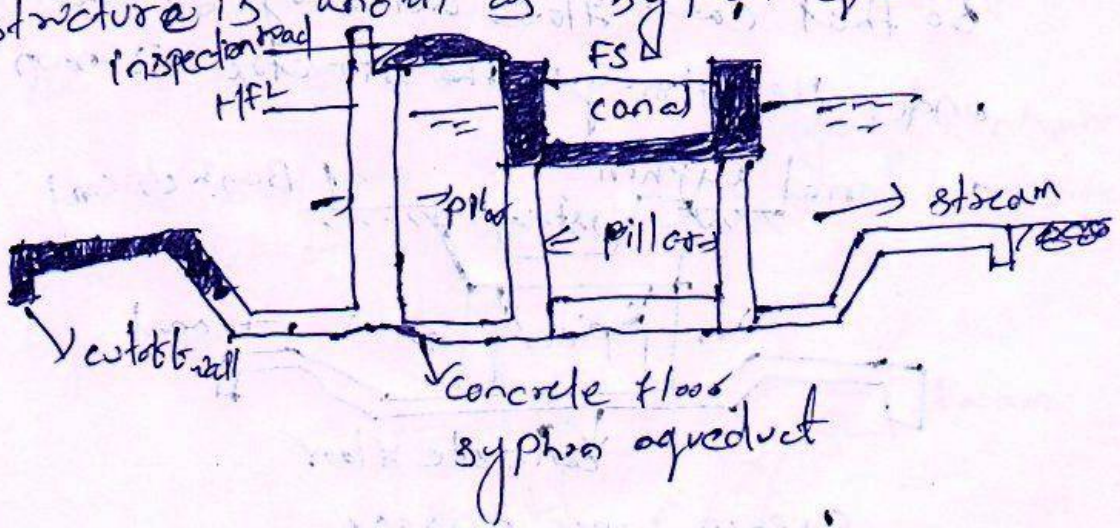
→ In these work the canal is taken over the natural drain such that the drainage water runs below the canal freely.

→ When the HFL of drain is sufficiently below the bottom of canal, so that the drainage water flows freely under gravity, the structure is known as aqueduct.



Syphon Aqueduct

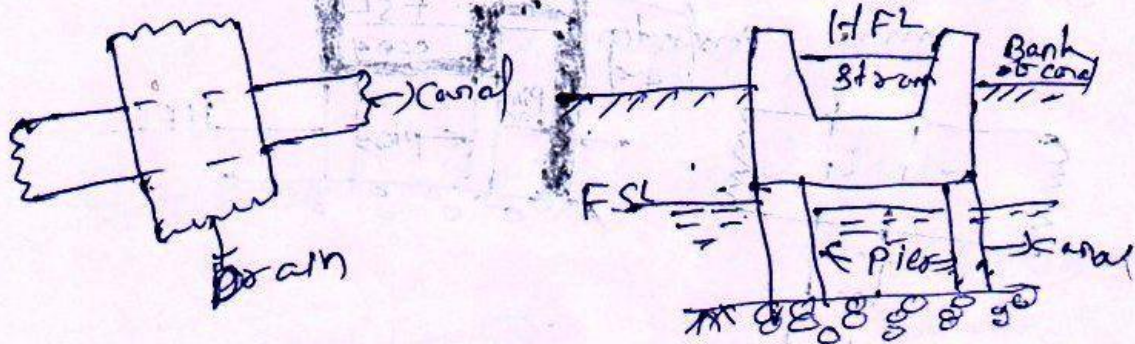
As the HFL of the drain is higher than the canal bed, and the water passes through the aqueduct barrels under syphonic action the structure is known as syphon aqueduct.



Super passage

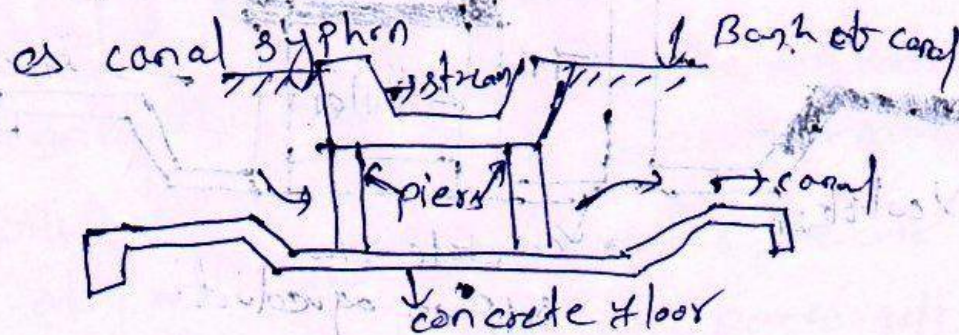
→ In these case, the drain is taken over the canal such that the canal water runs below the drain freely.

→ When FSL of canal is sufficiently below the bottom of the drain through so that canal water flows freely under gravity of structure is called super passage.



Syphon super passage

→ As the FSL of the canal is sufficiently above the bed level of drainage through so that canal flows under syphonic action under the through the structure is known as canal syphon.

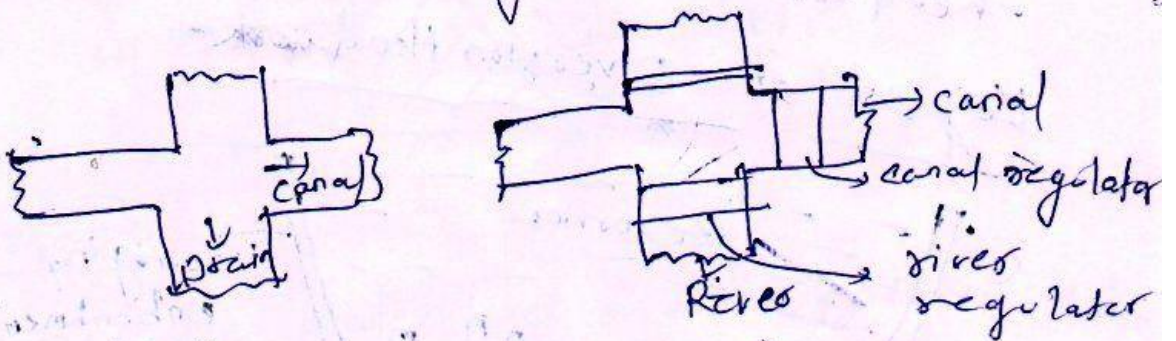


Syphon super passage

level crossing

→ In this type of cross drainage work, the canal water and drain water are allowed to intermingle with each other.

→ A level crossing is generally provided when a large canal and huge drainage approach each other practically at same level.

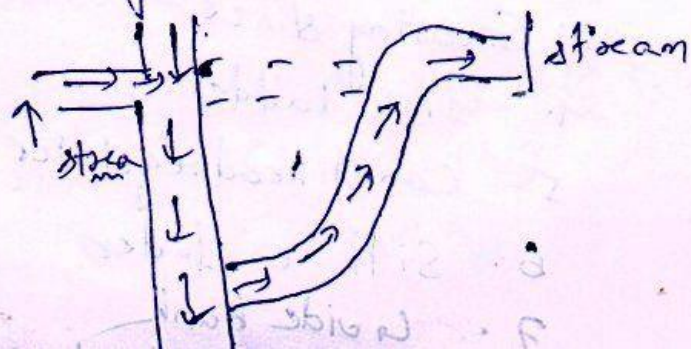


Inlet/outlet

→ An inlet is a structure constructed in order to allow the drainage water to enter the canal and get mixed with canal water.

→ An outlet is provided to discharge the surplus water.

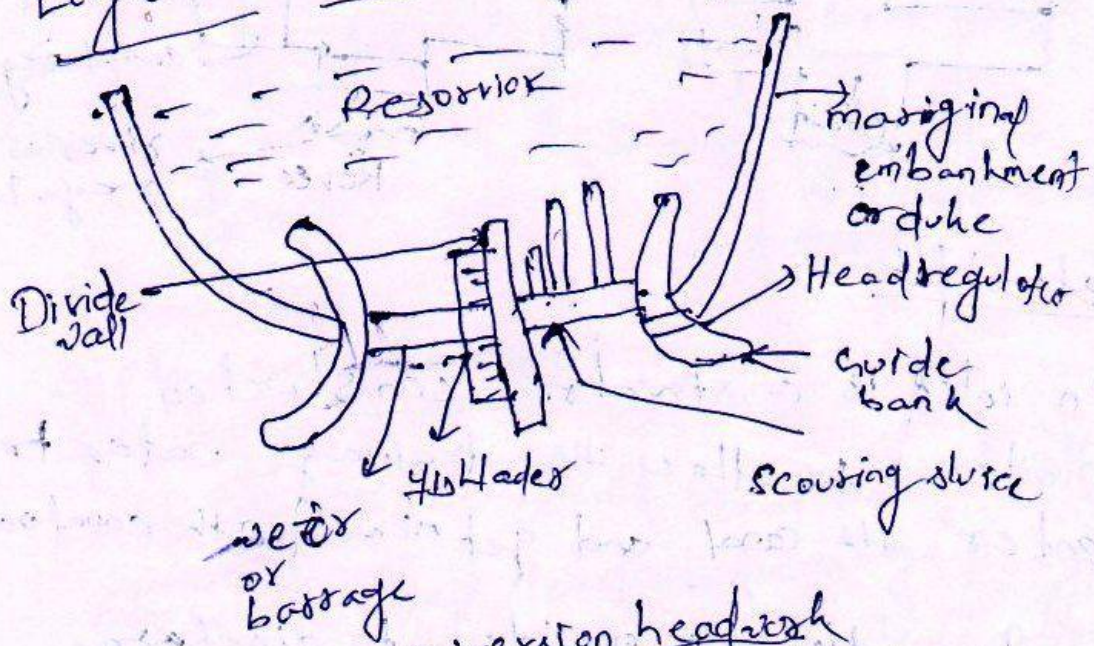
→ The bed and banks of irrigation channel b/w inlet and outlet points should be protected by stone pitching.



Diversion Headwork

→ The ~~water~~ works, which is constructed at the head of the canal in order to divert the river water towards the canal so as to regulate continuous supply of silt free water with a certain minimum head in to canal is known as diversion headwork.

Layout of Diversion Headwork



Components of diversion Headwork

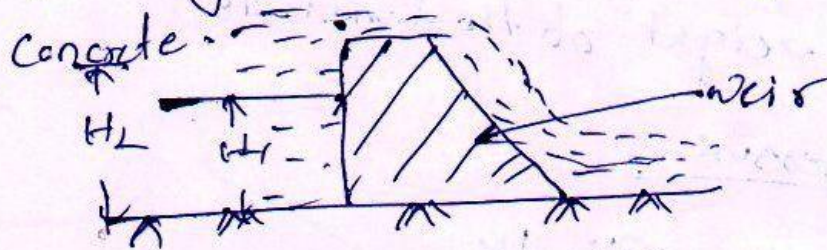
1. weir or barrage
2. Divide wall
3. Scouring sluice
4. Fish ladder
5. Canal headregulator
6. Silt excluder
7. Guide bank

weir

→ when the bed level of canal is at higher than the river level, the water cannot be diverted towards the canal.

→ So as to raise the water level an obstruction is constructed called weir.

→ It may be constructed through masonry or concrete.



Barrage

→ when the water level on the upstream side of the weir is required to be raised to different levels at different times, then the barrage is constructed.

Lane's weighted creep theory

→ Lane on the basis of his analysis carried out on about 200 dams.

→ So he suggested a weightage factor of $\frac{1}{3}$ for the horizontal creep as against 1.0 for vertical creep.

$$\begin{aligned}L_c &= (h_1 + h_2) + \frac{1}{3} S_1 + (h_2 + h_3) + \frac{1}{2} S_2 + (h_3 + h_4) \\ &= \frac{1}{3} (S_1 + S_2) + 2(h_1 + h_2 + h_3) \\ &= \frac{1}{3} S + 2(h_1 + h_2 + h_3)\end{aligned}$$

EARTHEN DAM

- Earthen dam are constructed purely by earthwork in trapezoidal action
- These are most economical and suitable for weak foundation.

→ It can be easily constructed

- Types of earthen Dam

→ homogenous embankment type

→ Zoned embankment type

→ Diaphragm type

→ hydraulic-fill type

→ Rolled fill Dam

Spillways

→ A spillway is a structure constructed at dam site for effectively disposing of surplus water from upstream to down stream

→ The spillways are opening provided at the body of discharge safely excess water or flood water when water level rises above normal level

Types of spillway

(i) straight drop spillway

(ii) ogee spillway

(iii) chute spillway

(iv) side channel spillway

(v) shaft spillway

(vi) siphon spillway

Module-IV

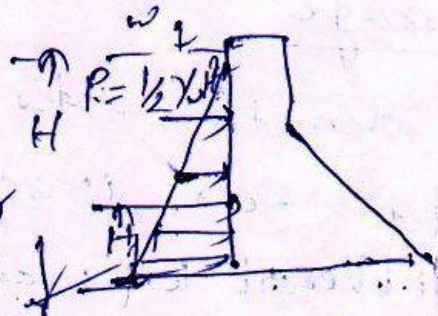
Force acting on gravity dam

- (i) water pressure
- (ii) uplift pressure
- (iii) pressure due to earthquake force
- (iv) silt pressure
- (v) wave pressure
- (vi) weight of the dam itself.

water pressure

→ water pressure (P) is the most major external force acting on a dam

→ The horizontal water pressure exerted by the wt. of the water stored in the upstream side of dam can be estimated from rule of hydrostatic pressure distribution



$$\gamma_w = \text{unit weight} \\ = 9.81 \text{ kN/m}^3$$

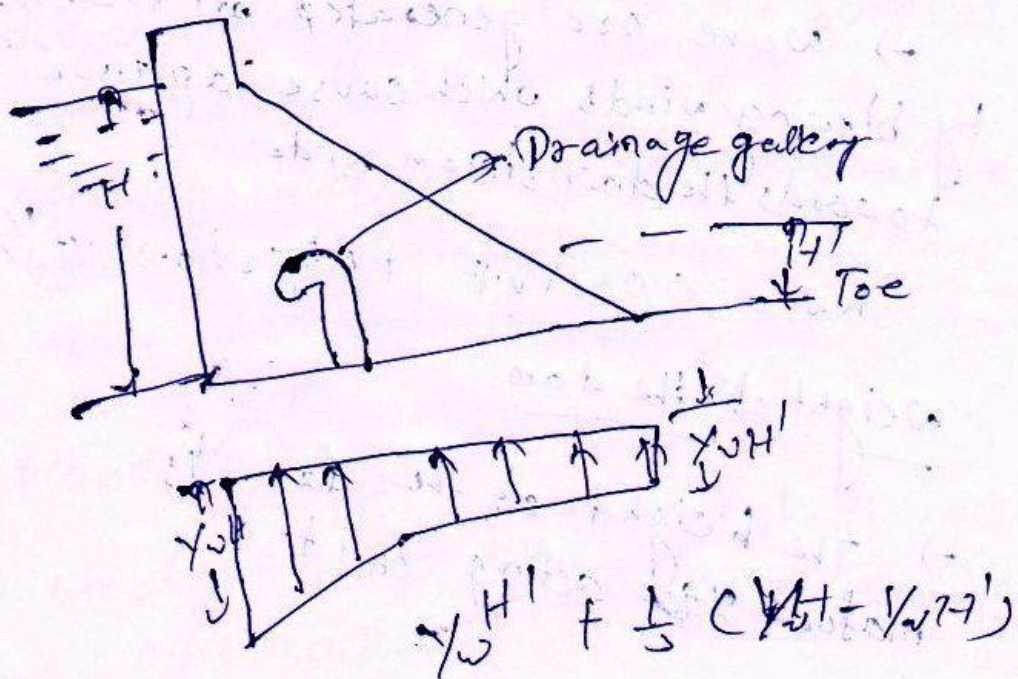
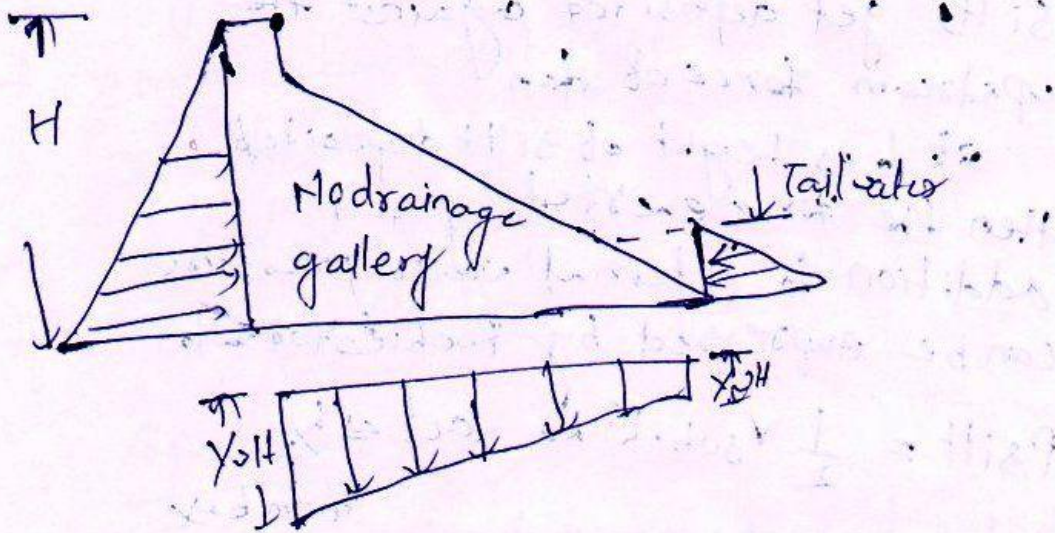
→ $\gamma_w = \text{unit weight of water}$
 $H = \text{depth of water}$

$$\text{Resultant force} = \frac{1}{2} \gamma_w H^2$$

Uplift Pressure

→ water seeping through the pores, cracks and fissures of the foundation material and water seeping through dam and its foundation at the base.

→ such an uplift force vertically reduces the downward weight of the dam hence acts against dam stability.



Earthquake force

→ For dam design allowance must be made for the stresses generated by earthquake

(1) effect of vertical accel (a_v)

(2) effect of horizontal accel (a_h)

Silt pressure

→ Silts get deposited against the upstream face of dam.

→ If h is height of silt deposited then the force exerted by silt in addition to external water pressure can be expressed by Rankine's formula

$$P_{\text{silt}} = \frac{1}{2} v_{\text{sub}} \cdot h^2 \cdot a_h \text{ act as } \frac{h}{3} \text{ from base}$$

wave pressure

→ wave are generated on the surface by blowing winds which cause a pressure towards the downstream side.

$$h_w = 0.032 V V \cdot F + 0.763 + 0.271 (F)^{1/4}$$

weight of the dam

→ The weight of the dam is major force acting on it